

Extended Joint Models for Longitudinal & Time-to-event Data

with applications in Cardiothoracic Surgery

Grigorios Papageorgiou

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**Extended Joint Models
for Longitudinal and Time-to-event Data**
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*Uitgebreide joint models
voor longitudinale en overlevingsdata
met toepassingen in cardiothoracale chirurgie*

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Promotiecommissie:

Promotoren: Prof. dr. D. Rizopoulos
Prof. dr. J.J.M. Takkenberg

Overige leden: Dr. I. Kardys
Prof. dr. R. Selles
Prof. dr. H. Putter

Copromotor: dr. M.M. Mokhles

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To my mother, father and sister, and to Maroula.

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Chapter **1**

General Introduction

It is quite before our birth that we unconsciously register our presence in this world with a short, tiny, barely audible, rhythmic, and most importantly, repeated sound. A sound that will constantly accompany us during our lives. Our heartbeat. As long as the beat repeats steadily and with a balanced pace (not too fast and not too slow), we are going to be okay.

Of course, this will not always be the case. Our heartbeat will often change, transitioning between different states of pace and volume. We all know that it will become faster and louder under intense emotions before returning to its normal state. However, emotions will not be the sole cause of such transitions, and these transitions will not always be temporal. Events can worsen our health and increase the risk of bringing our heartbeat closer to the absorbing state of silence.

Naturally, one then reasonably wonders: If we can deduce so much information from the repeated beat of our hearts by collective experience alone, what secrets will we be able to unravel by scientifically and repeatedly monitoring our heart, its features, and its function? Can we predict the future of our health and prevent us from the paths that lead to states bad for our health?

In this thesis, motivated by a broad range of applications in heart disease, we developed statistical methodology and models that contribute to answering such questions. In the remainder of the introduction, we will briefly introduce the clinical background of the applications that motivated our research: congenital heart disease, heart failure, and tricuspid regurgitation. We will then present the datasets that we use in our applications and their features. Furthermore, we will outline the joint modeling framework and briefly introduce the theoretical background, which forms the basis for the extensions we develop.

1.1 Heart Function & Disease

The heart is a muscular organ located behind and slightly left to the breastbone that consists of two atria and two ventricles. The right atrium receives the blood from the veins and pumps it to the right ventricle, which pumps the blood to the lungs, where it becomes oxygenated. The left atrium receives the oxygenated blood and sends it to the left ventricle. Then the oxygen-rich blood is sent to the rest of the body by the contractions of the left ventricle. Ideally, blood flows unobstructedly from the atria to the ventricles and the rest of the body during the circulation process.

This ideal flow of the blood vastly depends on the function of the heart's four valves

that ensure that blood unrestrictedly flows in the right direction through the heart. The tricuspid valve, located between the right atrium and the right ventricle, ensures that blood does not flow backward to the right atrium, from where the blood will move through the pulmonary valve to the lungs. The mitral valve is responsible for the unidirectional flow between the left atrium and the left ventricle, and finally, the aortic valve ensures that the flow between the left ventricle and the aorta is both unidirectional and unobstructed.

Congenital Heart Disease and the Pulmonary Valve

Congenital heart disease (CHD) is the most common type of congenital disability. As such, it is a major contributor to morbidity and mortality in both children and adults. Around 9 out of 1000 newborns have a structural-developmental heart defect (van der Linde et al., 2011). While CHD refers to a broad spectrum of different defects and symptoms, there have been significant advancements during the past decades in treating these patients, improving their quality of life and life expectancy.

Roughly 20% of CHD involves problems with the right ventricular outflow tract (RVOT) such as pulmonary atresia, pulmonary valve stenosis, tetralogy of fallot, double outlet right ventricle. These patients will undergo RVOT reconstruction, possibly with a pulmonary valve replacement. Pulmonary valve replacement is also required for patients who undergo the Ross procedure (Ross, 1967) during which the healthy pulmonary valve of the patient is used to replace his/her diseased aortic valve, and a valve substitute (usually a homograft, human donor valve, or pericardial valve) is implanted in the pulmonary position.

Patients' heart function is closely monitored echocardiographically after RVOT reconstruction as these patients are at risk of homograft failure. More specifically, the pulmonary valve function might deteriorate over time and suffer from stenosis or pulmonary regurgitation. The former means that the valve is narrower than it should, causing higher pressure as the blood flows through the heart, and the latter means that the valve fails to fulfill its primary task, unidirectional flow of the blood, as some of the blood leaks back to the ventricle. Other complications include endocarditis or children that may outgrow their homograft due to somatic growth. If such issues occur, the patients might need an (additional) pulmonary valve replacement with an allograft/homograft.

Such additional valve replacements are challenging to practicing physicians as the optimal timing for such re-interventions is unknown. Therefore, novel methods to model the progression of pulmonary valve function in relation with patient outcomes would be beneficial to optimize the timing of these interventions.

Left Ventricular Assist Device after Heart Failure

Heart failure is a chronic, progressive condition in which the heart cannot to fulfill the body's needs for blood and oxygen. It is amongst the most common causes of hospitalization, affecting about 40 million people worldwide. Given that it commonly affects the older population and that life expectancy is increasing, it is reasonable to assume that the number of patients with heart failure is expected to increase as well (Baman and F.S., 2020). Therefore effective prevention, treatment, and management of these patients are necessary.

There are several medical and device-based therapies for heart failure. Ventricular assist devices are rapidly emerging as a safe and durable therapy for end-stage heart failure patients (Han et al., 2018). These devices are also used as a bridge while waiting for heart transplantation. Despite the technological improvements of recent years, the burden of serious adverse events for subjects treated with LVAD is still cumbersome.

Common complications of patients treated with LVAD include thrombosis, dialysis, and kidney failure. Biomarkers associated with these complications, such as total bilirubin and creatinine, may shed more light on the inter-relationships between the processes that affect the risk for such complications in LVAD patients. (Antonides et al., 2020; Yalcin et al., 2019,0) Modeling the longitudinal evolution of these biomarkers while quantifying their association with patient outcomes can bridge the knowledge gaps in their interrelationships and improve decision making and treatment for these patients.

Tricuspid Regurgitation after Heart Transplantation

Heart transplantation (HTx) is often necessary to treat end-stage heart disease. Orthotopic heart transplantation (OHT) is considered the best treatment for advanced heart failure, with more than 4.000 performed annually in the world. Tricuspid regurgitation (TR) is considered the most common valvular complication after HTx with an incidence of 84% (Wong et al., 2008).

Causes for TR in patients with a heart transplant include endomyocardial biopsies, allograft rejection, a mismatch between the donor heart size and pericardial cavity dimensions (De Simone et al., 1995; Aziz et al., 1999; Caliskan et al., 2018). The clinical impact of TR after HTx remains still unclear. Post OHT is a dynamic disease with many potential etiologies. Repeated measurements of TR over time and dynamic predictive tools can aid in investigating its association with the risk of post-OHT failure and mortality and better assess its impact.

1.2 Motivating Datasets

Several observational studies and randomized clinical trials motivate the research presented in this thesis. While these studies come from various clinical research disciplines, they share in common that they are longitudinal. That means subjects are followed up over time, and several measures such as biomarkers and clinical endpoints are being monitored.

The datasets that we use in this thesis to motivate and subsequently demonstrate the statistical methods proposed in the thesis are briefly introduced in the following sections.

Pulmonary Gradient Dataset

This dataset comes from a study on 467 congenital heart disease (CHD) patients who underwent a right ventricular outflow tract reconstruction with a pulmonary allograft and were followed up echocardiographically after that at the Department of Cardio-Thoracic surgery of Erasmus University Medical Center. The pulmonary gradient of these patients was monitored repeatedly over time and is believed to be associated with the risk of death. Death is the primary endpoint of this study. However, during follow-up, 65 (13.92%) were reoperated and received a pulmonary allograft. The main interest in this study is to investigate the association between the pulmonary gradient and the risk of death and study the impact of reoperation on this risk and the pulmonary gradient. By doing so, predictive tools can be developed to quantify the potential benefit of reoperation for future patients. Table 1.1 gives a summary of the data.

Table 1.1: Data summary: Continuous variables are presented as median (IQR), categorical variables as counts (frequencies %).

	All	Non reoperated	Reoperated
Number of subjects	467	402 (86.9%)	65 (13.1%)
Number of repeated measurements	8 (5 - 12)	7 (4 - 11)	14 (11 - 16)
Number of Events	34 (7.3%)	32 (8.0%)	2 (3.0 %)
Sex = Male	272 (58.2%)	229 (57.0%)	43 (66.1 %)
Age	20.3 (9.5 - 30.9)	21.5 (9.4 - 31.2)	16 (10.9 - 22.4)

SPRINT Data

This dataset concerns 9361 subjects who participated in the SPRINT study (Group, 2015). Subjects with increased cardiovascular risk, systolic blood pressure of 130mm Hg or higher but without diabetes were randomized to intensive or standard treatment. The composite primary outcome was myocardial infarction, acute coronary syndromes, stroke, heart failure, or death from cardiovascular causes, while systolic blood pressure is the biomarker of interest that was repeatedly measured. During follow-up, 3424(36.6%) experienced serious adverse events (SAEs). In this study, it is of interest to assess the impact of SAEs both in the systolic blood pressure evolution and the risk for the event of interest and exploiting it to derive individualized, dynamic predictions for future patients with different scenarios for the occurrence or not of SAEs.

Women & Pregnancy after RVOT

This dataset concerns 196 women between 18 and 50 years old who underwent Right Ventricular Outflow Tract (RVOT) reconstruction between April 1986 and January 2018 with an allograft at the Cardio-Thoracic Surgery department of the Erasmus Medical Center and confirmed pregnancy during this period. Complete information of 176 (90%) allografts in 165 women were recorded, including 1395 repeated measurements of pulmonary gradient and regurgitation grade from echocardiograms. 51 (30.9%) of these women had 84 completed pregnancies at an average age of $29.1 \pm 3.9(SD)years$ at 8.1 ± 6.1 years since allograft implantation. Tetralogy of Fallot was the most common diagnosis in both groups. After a mean follow-up of 15.2 years (range 0.1 to 30), 7 (13.7%) parous women underwent valve replacement versus 20 (17.5%) nulliparous women. The interest in this study was to investigate the association of Pulmonary Gradient and Pulmonary regurgitation Grade with the risk of pulmonary valve replacement and how pregnancy influences this association.

LVAD after Heart Failure

This dataset includes 232 patients who experienced heart failure and subsequently received a Left Ventricular Assist Device (LVAD) implant during follow-up at the Erasmus University Medical Center in the Netherlands. These patients may suffer multiple complications during follow-up, such as thrombosis, embolic events, and dialysis, which are assumed to increase their risk of dying. To reduce this risk, treating physicians follow these patients closely and collect biomarker measurements for their liver (Total Bilirubin) and kidney (Creatinine) function and may decide to intervene

with an LVAD implant accordingly. LVAD is consequently expected to change their risk of experiencing a complication or dying and the trajectories of their liver and kidney biomarkers. In particular, LVAD takes over the heart function of the patient, and therefore, it is expected to increase the patient's survival chance while waiting for a heart transplant.

On the other hand, however, it might increase the risk of dialysis and/or thrombosis due to acute kidney injury and/or other complications. Muslem et al. (2018). In this study, 49 (21.1%) subjects experienced a complication, of which 23 (10.0%) subsequently died, while 80 (34.5%) subjects died without experiencing such a complication.

Tricuspid Regurgitation after Heart Transplantation

This dataset includes 572 consecutive subjects who underwent biatrial orthotopic heart transplant (OHT) for 32 years between 1984 and 2016 in Erasmus MC. These patients were echocardiographically followed up over time, and their tricuspid regurgitation measurements were recorded as well. This study aims to investigate the evolution of TR over time and its association with the risk of death, as TR is common in patients with OHT.

1.3 Joint Models for Longitudinal and Time-to-Event Data

While the motivating datasets discussed in the previous section concern different populations and aspects of heart disease, they do have many features in common. More specifically, patients are being followed up over long periods generating repeated measurements of biomarkers of interest. During follow-up, it is often the case that important events occurred, such as changes in treatment, reintervention, serious adverse events, etc., that can change the course of the disease and the risk for the clinical endpoint of interest. There is the potential of informative dropout. The repeatedly measured outcomes are assumed to be associated with the time-to-event outcome of interest. The structure of this association and its magnitude are of primary interest.

Each of the features above poses a different challenge in terms of statistical modeling. While, as we will discuss, there are methods to address some of these challenges separately, the joint modeling framework is necessary to address these features in combination.

Analysis of Repeated Measurements

The distinguishing feature of repeatedly measured data is that multiple observations are collected from a single subject (or cluster in the general case). This is in contrast to cross-sectional data, where typically, an observation belongs to a different subject. The key in the distinction between the two comes from the fact that data points are independent of each other by default in the latter case, whereas in the former case, data points within-subjects (clusters) are not. Those measurements coming from the same subject are expected to be more correlated than measurements between subjects.

This (expected) systemic difference in the correlation between observations coming from the same subject against observations from different subjects poses an additional challenge in modeling and analyzing such data. A popular framework for dealing with this challenge is mixed-effects models. The key feature of these models is the introduction of latent effects, the so-called random effects, which are specific to each subject and quantify its deviation from the average of the population, which is described by the so-called fixed effects. In other words, random effects are unobservable to us, characteristics that capture and describe the subject-specific differences that the observable characteristics cannot explain.

Technically, mixed-effects models can be described as follows. Let \mathbf{y}_{ki} denote the $n_{ki} \times 1$ longitudinal response vector for the k^{th} longitudinal outcome taken at time point $t_{kil}, l = 1, \dots, n_{ki}$. Each longitudinal outcome k can be described by a generalized linear mixed model conditional on the vector of random effects \mathbf{b}_{ki} :

$$\left\{ \begin{array}{l} g_k [E\{y_{ki}(t) | \mathbf{b}_{ki}\}] = \eta_{ki}(t) = \mathbf{x}_{ki}^\top(t) \boldsymbol{\beta}_k + \mathbf{z}_{ki}^\top(t) \mathbf{b}_{ki}, \\ \mathbf{b}_{ki} = \begin{bmatrix} \mathbf{b}_{1i} \\ \mathbf{b}_{2i} \\ \vdots \\ \mathbf{b}_{ki} \end{bmatrix} \sim \mathcal{N}(\mathbf{0}, \mathbf{D}), \end{array} \right.$$

where $g_k(\cdot)$ is a general link function appropriate for the k^{th} outcome, \mathbf{x}_{ki} and \mathbf{z}_{ki} are design vectors for the fixed-effects' regression coefficients $\boldsymbol{\beta}_k$ and the random-effects \mathbf{b}_{ki} respectively. The association between the K longitudinal outcomes is built via the random-effects \mathbf{b}_{ki} and $\tilde{\mathbf{b}}_{ki}$ which are assumed to be normally distributed with mean zero and a $q \times q$ general variance-covariance matrix \mathbf{D} .

The formulation discussed above covers the general case of multivariate longitudinal data of different types, such as continuous or categorical. When $k = 1$, this reduces

to the basic mixed-effects models for a single longitudinal outcome.

Missing Data & Dropout

Missing data is a common complication in longitudinal studies as well as cross-sectional studies. There is a variety of reasons for which a data point might be missing from a dataset. Depending on the reason, or using a more technical term, the mechanism that generates the missing data, and whether data are missing in the outcomes of interest or the covariates of interest, the difficulty of addressing the challenges due to missing data might differ. According to the taxonomy introduced by Rubin (1976) and Little and Rubin (2002) this may happen according to three distinct missing data mechanisms:

- **Missing Completely at Random (MCAR):** Missingness depends on neither observed nor unobserved outcomes,
- **Missing at Random (MAR):** Missingness is independent of the unobserved outcomes after conditioning on the observed outcomes, and
- **Missing Not at Random (MNAR):** Conditioning on the observed outcomes cannot disentangle the dependence between the missingness process and the unobserved outcomes.

MCAR is the simplest of the above cases as the missing data can be considered a random sample of the complete dataset, and therefore analyzing the observed data will not generally lead to biased results. Under MAR, this is not the case, and the missingness generating process needs to be explicitly accounted for in the model. However, under specific conditions in (Bayesian) likelihood-based approaches, such as the mixed-effects models previously discussed, missingness can be termed ignorable and valid inferences can be derived by solely analyzing the observed data. Finally, under MNAR, missingness depends on information that is not available, and therefore the missingness process needs to be modeled explicitly and jointly with the outcome of interest. As there are infinite MNAR models and the distinction between MAR and MNAR is impossible (Molenberghs et al., 2008), this is usually conducted in a framework of sensitivity analysis where different scenarios about the missingness process are explored.

To achieve so, three general frameworks exist: pattern mixture models (PMM), selection models (SeM), and shared parameter models (SPM). Their difference comes in how the joint distribution of the outcome and missingness processes are factored

to conditionally independent components. In this thesis, we focus on SPMs under which the outcome and the missingness processes are assumed to be driven by a set of unobserved variables, the so-called random effects. The use of latent variables gives rise to the conditional independence assumption under which the outcome and the missingness processes are independent, given the set of random effects.

Analysis of Time-to-Event Data

Typically in follow-up studies, apart from longitudinal outcomes, the main interest is on a clinical endpoint which is recorded as a time-to-event outcome subject to censoring. Let us denote by T_i^* the true event time for subject i and let $T_i = \min(T_i^*, C_i)$ be the observed event time, which is defined as the minimum value between the true event time T_i^* and the censoring time C_i . Furthermore, let $\delta_i \in (0, 1, 2, 3)$ denote an event indicator which is equal to: 0 under right censoring ($T_i^* > T_i$), 1 when ($T_i^* = T_i$), 2 under left censoring ($T_i^* < T_i$) and 3 under interval censoring in which case an interval of observed event times with limits T_i^L and T_i^U are observed and the true event time lies within the interval ($T_i^L < T_i^* < T_i^U$). In this thesis we will focus on the case of right censoring and assume that $\delta_i = I(T_i^* \leq C_i)$.

Under this notation, time-to-event data may be analyzed using a relative risk model such as a Cox proportional hazards model (Cox, 1972) which is specified as follows:

$$\begin{aligned} h_i(t | \mathbf{w}_i(t)) &= \lim_{\Delta t \rightarrow 0} \frac{\Pr \{t \leq T_i^* < t + \Delta t \mid T_i^* \geq t, \mathbf{w}_i\}}{\Delta t} \\ &= h_0(t) \exp \left[\boldsymbol{\gamma}^\top \mathbf{w}_i(t) \right], \end{aligned}$$

where $h_0(t)$ is the baseline hazard, $\mathbf{w}_i(t)$ are baseline covariates with corresponding regression coefficients $\boldsymbol{\gamma}$.

Note that the baseline covariates $\mathbf{w}_i(t)$ are allowed to be time-varying which refers to the extended formulation for the time-dependent Cox model (Therneau and Grambsch, 2000; Andersen and Gill, 1982). In principle this formulation allows for repeatedly measured outcomes to enter the model as time-dependent covariates and subsequently quantify their association with the hazard for the event of interest. This formulation, however, is only appropriate for exogenous factors (such as time, for example) as it assumes that the observed values are measured without error and remain constant (value carries forward) until the next measurement. This is unlikely to be the case for endogenous covariates (such as heart function), which are measured with error, are subject to biological variation, and their path cannot be fully and deterministically specified between measurements. As a result, the time-dependent Cox model

unsuitable for investigating the association between endogenous repeatedly measured outcomes and the risk for an event of interest.

The Basic Joint Model

Joint models for longitudinal and time-to-event data, which belong to the broad family of shared-parameter models, are not subject to the limitations discussed above, namely MNAR and the endogeneity of time-dependent covariates (Rizopoulos, 2012; Tsiatis and Davidian, 2004; Wulfsohn and Tsiatis, 1997; Rizopoulos and Ghosh, 2011a; Chi and Ibrahim, 2006). The building block of the joint modeling framework is the assumption that both the longitudinal and time-to-event processes are driven by unobserved and shared random-effects conditional on which the two processes are independent. The intuition behind joint models is simple, instead of using the actual observed repeated measurements as time-dependent covariates in a relative risk model, we first estimate the true underlying longitudinal trajectory based on these measurements using a mixed-effects model and use it (or functions thereof) in the relative risk model. Figure 1.1 gives a graphical representation of such a joint model where it is seen that the smooth estimated longitudinal trajectory is associated with the hazard for an event rather than the step function connecting the observed measurements as it would be the case when using a time-dependent Cox model.

Formally, the specification of a joint model is given by:

$$\left\{ \begin{array}{l} g_k [E\{y_{ki}(t) \mid \mathbf{b}_{ki}\}] = \eta_{ki}(t) = \mathbf{x}_{ki}^\top(t) \boldsymbol{\beta}_k + \mathbf{z}_{ki}^\top(t) \mathbf{b}_{ki}, \\ h_i(t \mid \mathcal{M}_i(t), \mathbf{w}_i(t)) = h_0(t) \exp[\boldsymbol{\gamma}^\top \mathbf{w}_i(t) + \sum_{k=1}^K \sum_{l=1}^{L_K} f_{kl}\{\boldsymbol{\alpha}_{kl}, \mathbf{w}_i(t), \mathbf{b}_{ki}, \mathcal{M}_i(t)\}] \\ \mathbf{b}_{ki} = \begin{bmatrix} \mathbf{b}_{1i} \\ \mathbf{b}_{2i} \\ \vdots \\ \mathbf{b}_{ki} \end{bmatrix} \sim \mathcal{N}(\mathbf{0}, \mathbf{D}), \end{array} \right.$$

where $\mathcal{M}_i(t) = \{\mathcal{M}_{1i}(t), \dots, \mathcal{M}_{ki}(t)\}$, and $\mathcal{M}_{ki}(t) = \{\eta_{ki}(s), 0 \leq s < t\}$ denotes the history of the true unobserved longitudinal process up to time t , and $\mathbf{w}_i(t)$ is a vector of exogenous, possibly time-varying, covariates with corresponding regression coefficients $\boldsymbol{\gamma}$. Functions f_{kl} , parameterized by vector $\boldsymbol{\alpha}_{kl}$, specify which components/features of each longitudinal outcome are included in the relative risk model. This for-

mulation covers the case of multiple longitudinal outcomes. In case of a single longitudinal outcome subscript k and the summation over the k outcomes can be dropped.

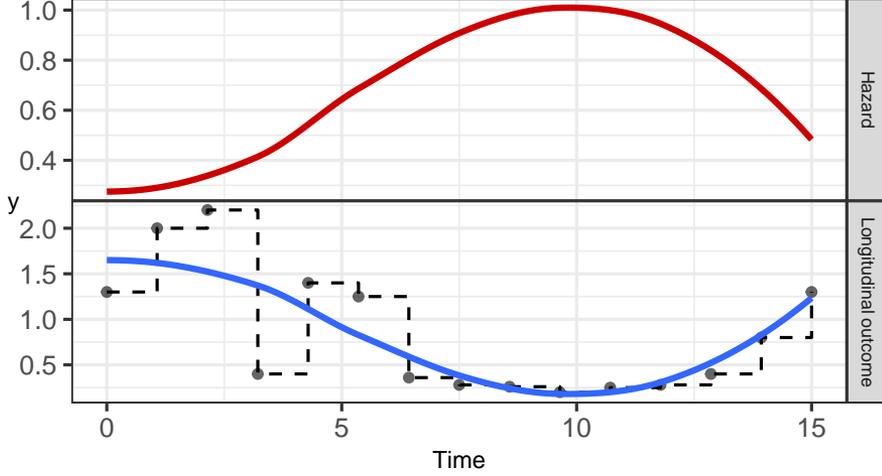


Figure 1.1: Illustration of a basic Joint Model with one longitudinal outcome and one event of interest.

Association Structures

One of the main advantages of joint modeling is that since the longitudinal marker's smooth, true underlying trajectory is used as a time-varying covariate in the relative risk model, there are no limitations in the functional form that can be used to relate the two processes. In its simplest form, function f_{kl} is

$$f\{\alpha, \mathbf{w}_i(t), \mathbf{b}_i, \mathcal{M}_i(t)\} = \alpha\eta_i(t),$$

known as the current value association. Under this structure, it is assumed that the value of the longitudinal marker(s) at time point t is associated with the hazard value for the event of interest at the same time point. Alternatively, one may assume that

$$f\{\alpha, \mathbf{w}_i(t), \mathbf{b}_i, \mathcal{M}_i(t)\} = \alpha\eta'_i(t), \quad \text{with} \quad \eta'_i(t) = \frac{d\eta_i(t)}{dt}$$

, which means that the rate of increase or decrease of the longitudinal marker at time t is associated with the hazard value for the event of interest at the same time point.

This structure is known as the current slope association. Finally, another common association structure that is useful in applications is the area under the curve association, given by:

$$f\{\alpha, \mathbf{w}_i(t), \mathbf{b}_i, \mathcal{M}_i(t)\} = \alpha \int_0^t \eta_i(s) ds.$$

Under this association structure, we assume that the cumulative burden of the longitudinal biomarker values up to time t is associated with the hazard value for the event of interest at the same time point. Figure 1.2 shows a graphical representation of all these three association structures.

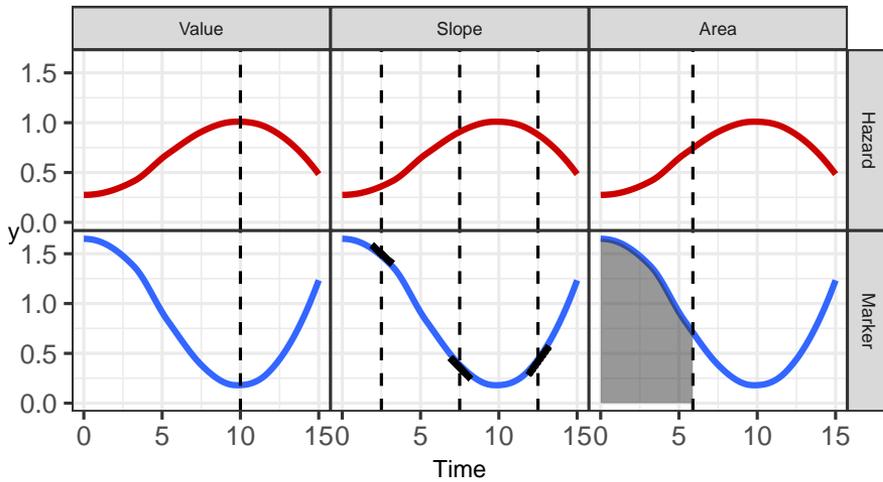


Figure 1.2: Illustration of the current value, current slope and cumulative effect association structures

1.4 Dynamic Predictions

Joint models can be used as the building block for a vital tool to aid personalized medicine in practice: dynamic predictions. The inherently dynamic nature of joint models can be exploited to build dynamic predictive tools that can be updated as new measurements for a specific subject are being gathered. This is of great importance in the field of heart disease (and overall in healthcare and medicine) as physicians need predictive tools tailored to the subject-specific characteristics of each patient to aid and improve their decision-making and facilitate communication of health risks.

More specifically and based on a joint model fitted to data, subject-specific probabilities and predictions for future biomarker levels, may derived for a new subject i' for whom there is a history of biomarker measurements $\mathcal{Y}_{ki'}(t) = \{y_{ki'}(t_{ki'l}); 0 \leq t_{ki'l} \leq t, k = 1, \dots, n_k\}$ for the k^{th} longitudinal outcome and a vector of baseline covariates $w_{i'}$. The biomarker measurements are available up to a time point t and since the biomarker values are endogenous we assume that the event of interest has not occurred up to that point. In this setting, the conditional subject-specific survival probability that subject i^{new} survives at least up to a future time point $u > t$ is given by:

$$\pi_{i'}(u | t) = \Pr \left\{ T_{i'}^* \geq u \mid T_{i'}^* > t, \mathcal{Y}_{1i'}(t), \dots, \mathcal{Y}_{n_{ki'}}(t), w_{i'} \right\},$$

and the prediction for the subject's longitudinal response at u is given by:

$$\omega_{ki'}(u | t) = E \left\{ y_{ki'}(u) \mid T_{i'}^* > t, \mathcal{Y}_{1i'}(t), \dots, \mathcal{Y}_{n_{ki'}}(t), w_{i'} \right\}.$$

Figure 1.3 gives a graphical representation of the concept of dynamic predictions. Both $\pi_{i'}(u | t)$ and $\omega_{ki'}(u | t)$ can be updated as new measurements for subject i' accrue. Estimation of both $\pi_{i'}(u | t)$ and $\omega_{ki'}(u | t)$ is based on the corresponding posterior predictive distributions (Yu et al., 2008; Proust-Lima and Taylor, 2009; Rizopoulos, 2011; Taylor et al., 2013)

1.5 Extensions

Intermediate Events & Adaptive Dynamic Predictions

The accuracy of dynamic predictions from joint models and their evaluation is a topic of active research. Recent work on the topic has revealed that the performance of dynamic predictions from joint models depends on the modeling of subject-specific longitudinal profiles and is sensitive to misspecification (Rizopoulos et al., 2017; Ferrer et al., 2019; Suresh et al., 2017). This is an important observation as longitudinal studies, due to their nature, are susceptible to intermediate events that may occur on any subject during follow-up and directly affect the shapes of their longitudinal trajectories. There are many examples of such intermediate events that may be under the investigator's control. For the pulmonary gradient dataset, some subjects received additional valves during follow-up. In the SPRINT dataset, subjects may have experienced serious adverse events. Pregnancy may or may not affect the evolution of pulmonary valve markers during follow-up. Receiving an LVAD can drastically change the subject's longitudinal trajectory and heart failure or transplantation risk.

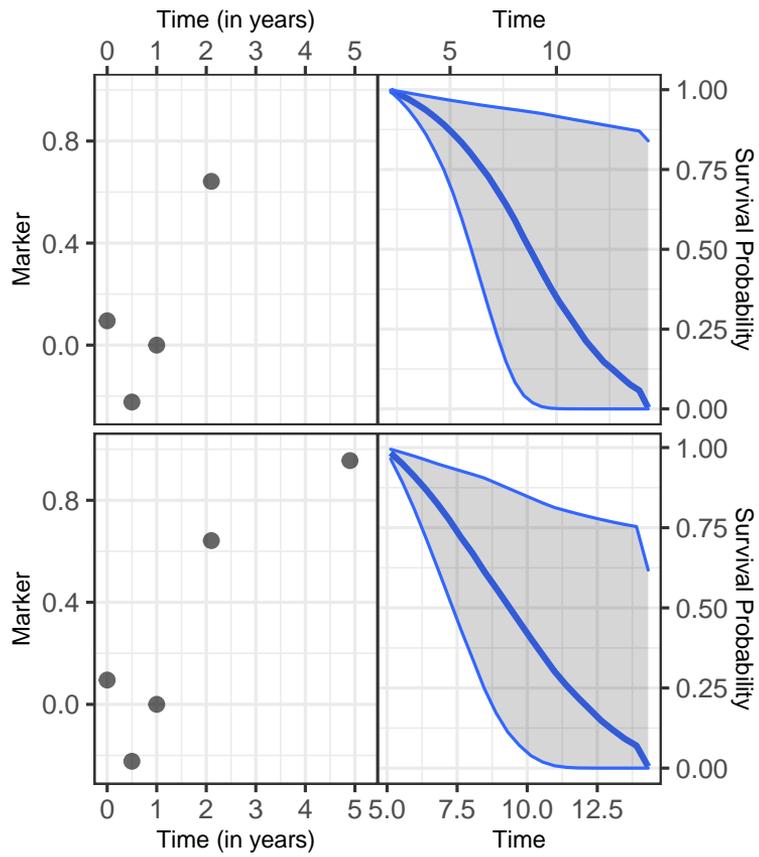


Figure 1.3: Illustration of subject-specific dynamic prediction of conditional survival probabilities after obtaining a new biomarker measurement.

Therefore, it is clear that such intermediate events are common in follow-up studies, and ignoring their occurrence might affect the quality of predictions for such cases. Despite that, there has not been much work in developing predictive tools that can incorporate intermediate events and adapt their prediction accordingly. Recent and interesting work on the topic has been produced by Sène et al. (2016) and Taylor et al. (2005) in the context of prostate cancer but only considered the longitudinal trajectories before the occurrence of the intermediate event.

In this thesis, we propose a different approach to include the occurrence of intermediate events in joint models and exploit them in adaptive dynamic prediction tools. We further propose adapted performance metrics for appropriately evaluating these tools.

Multi-state Models

The basic joint model is formulated for the case of a single longitudinal marker coupled with a single event of interest. In a previous section of this thesis, we presented a generalization that allows for multiple longitudinal markers and a single time-to-event outcome. However, it is very often the case that multiple events of interest may occur that may affect each other, as it is the case in the presence of competing risks (Andrinopoulou et al., 2014). A natural extension in this setting is the so-called multi-state models to which competing risks and single time-to-event outcomes are special cases of (Putter et al., 2007). This generalization allows for the inclusion of multiple disease states of interest and enables us to investigate the transition between such states. Such models can be advantageous in the field of heart failure and LVAD transplantation, where subjects may change between different disease states such as LVAD transplantation, thrombosis, heart failure, etc., and aid in understanding the interrelationship between biomarkers and the transition between such states (Muslem et al., 2018). Joint models for a single longitudinal marker and multi-state processes have been developed by Ferrer et al. (2016) under the frequentist paradigm with applications in the field of prostate cancer. In this thesis, we discuss extensions for the case of multiple biomarkers.

Feature Selection

The specification of the relationship between biomarkers and events of interest is not always straightforward. While clinical background, previous research, and subject-matter knowledge can aid in defining this relationship, it is often the case, especially in exploratory analyses and in the development of prediction models, that this relationship is still unknown. Previous work on the topic has revealed that different features

of longitudinal outcomes might be related to the events of interest (Rizopoulos and Ghosh, 2011b; Mauff et al., 2017). This makes selecting an appropriate association structure complicated in practice and creates a need for tools to aid in this selection when developing such models. The dimensionality of the task is also essential in this framework, as in the case of multiple longitudinal and time-to-event outcomes, the number of possible association structures increases substantially. For this purpose, Bayesian shrinkage priors have been used in the past to automate the selection process (Andrinopoulou and Rizopoulos, 2016). In this thesis, we extend the research on this topic by considering and assessing the performance of global-local shrinkage priors in the context of LVAD transplantation where multiple outcomes are of interest and information about their interrelationships is still unknown.

Missing Data & Sensitivity Analysis

Dropout is very common in longitudinal studies and can create complications in the subsequent analysis of the data depending on the causes of the dropout. As the distinction between MAR and MNAR is intractable, the standard approach in practice is to use an analysis valid under MAR and explore MNAR deviations from it as part of sensitivity analysis. Shared parameter models can theoretically be used for this purpose, but in practice, the SeM and PMM modeling frameworks are preferred because they entail a more straightforward MAR specification. There has been a lot of work recently towards achieving a MAR specification under the SPM framework with the introduction of the Generalized Shared Parameter Model (Creemers et al., 2010; Njagi et al., 2014). In this thesis, we propose an alternative specification which while simpler, can more easily be used in practice with readily available software.

1.6 Research Goals

Motivated by the studies discussed in previous sections, this thesis aims to extend the joint modeling framework in order to answer questions such as:

- **Intermediate Events & Adaptive Dynamic Predictions:**
 - Investigate the association between the evolution of pulmonary gradient and the risk of death. Quantify the impact of re-intervention on the course of heart disease for patients who underwent RVOT reconstruction with a pulmonary valve. Develop a dynamic prediction tool that is adaptive to different scenarios with respect to the decision to re-intervene or not to the patient.

- Assess the impact of SAEs both in the systolic blood pressure evolution and the risk for the event of interest and exploiting it to derive individualized, dynamic predictions for future patients with different scenarios with respect to the occurrence or not of SAEs.
- Investigate how and whether pregnancy as an intermediate event influences the long-term durability of allografts in RVOT.
- **Multi-state Models & Shrinkage:**
 - To investigate the impact of LVAD at different stages after heart failure and understand its association with predictive biomarkers and clinical outcomes.
 - To automate feature selection of biomarkers in the context of multivariate longitudinal and survival data by using Bayesian shrinkage priors.
 - Investigate factors are associated with tricuspid regurgitation after heart transplantation and how tricuspid regurgitation is associated with the risk of death.
- **Missing Data:**
 - To introduce an alternative framework for sensitivity analysis for missing data generating mechanisms in shared parameter joint models.
 - To propose guidelines for dealing with missing data in practice.

1.7 Outline

The rest of this thesis is structured as follows. In **PART I** we discuss the incorporation of intermediate events as time-varying covariates in joint models and their use in deriving dynamic predictions adaptive to different scenarios for the occurrence of these intermediate events. More specifically, in **Chapter 2** we give the technical details of incorporating intermediate events such as reintervention or serious adverse events in joint models and for deriving dynamic predictions from these models. We also discuss measures for validation of the predictive performance of these models, such as the time-varying AUC and the PE. The approach is illustrated in two motivating datasets. In **Chapter 3** we investigate the influence of pregnancy on the durability of allografts in RVOT. We consider pregnancy as an intermediate event, and we quantify its influence on biomarkers for valve replacement such as pulmonary regurgitation and the pulmonary gradient and its association with the risk of valve replacement.

In **PART II** we discuss feature selection of biomarkers in the presence of multiple longitudinal markers and multi-state processes by using Bayesian shrinkage priors. Specifically, in **Chapter 4** we discuss specification and estimation of joint models for multivariate longitudinal outcomes and multiple processes under the Bayesian framework and how to use Bayesian shrinkage priors to automate the selection of the appropriate association structure between biomarkers and transitions between states of interest. In **Chapter 5** we investigate the association between Tricuspid Regurgitation and the risk of dying in patients who underwent Heart Transplantation. We use Bayesian shrinkage priors to select features of tricuspid regurgitation that are associated with the risk of death.

In **PART III** we discuss missing data. In **Chapter 6** we discuss the Missing at Random characterization for the shared parameter models and propose its use for sensitivity analysis in cases with dropout. **Chapter 7** we briefly discuss the subject of missing covariate data in practice and propose useful guidelines on how to deal with missing covariate data in practice.

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Part I

Intermediate Events & Adaptive Dynamic Predictions

**Individualized dynamic prediction of survival with the presence
of intermediate events**

This chapter is based on:

Papageorgiou, G., Mokhles, M.M., Takkenberg, J.J.M. and Rizopoulos, D. (2019),
Individualized dynamic prediction of survival with the presence of intermediate events
Statistics in Medicine, 38: 5623–5640. doi: [https://doi-org.eur.idm.oclc
.org/10.1002/sim.8387](https://doi-org.eur.idm.oclc.org/10.1002/sim.8387)

Abstract

Often, in follow-up studies, patients experience intermediate events, such as reinterventions or adverse events, which directly affect the shapes of their longitudinal profiles. Our work is motivated by two studies in which such intermediate events have been recorded during follow-up. In both studies, we are interested in the change of the longitudinal evolutions after the occurrence of the intermediate event and in utilizing this information to improve the accuracy of dynamic prediction of their risk. To achieve so, we propose a flexible joint modeling framework for longitudinal and time-to-event data, which includes features of the intermediate event as time-varying covariates in both the longitudinal and survival submodels. We consider a set of joint models that postulate different effects of the intermediate event in the longitudinal profile and the risk of the clinical endpoint, with different formulations for the association structure while allowing its functional form to change after the occurrence of the intermediate event. Based on these models, we derive dynamic predictions of conditional survival probabilities which are adaptive to different scenarios with respect to the occurrence of the intermediate event. We evaluate the predictive accuracy of these predictions with a simulation study using the time-dependent area under the receiver operating characteristic curve and the expected prediction error adjusted to our setting. The results suggest that accounting for the changes in the longitudinal profiles and the instantaneous risk for the clinical endpoint is important, and improves the accuracy of the dynamic predictions.

2.1 Introduction

Nowadays there is great interest in the medical field for predictive tools that facilitate precision medicine. In the context of follow-up studies, in which patients are monitored with several longitudinally measured parameters and biomarkers, physicians are interested in utilizing this information for predicting clinical endpoints. In this setting, joint models for longitudinal and survival outcomes provide a flexible framework to study the association between these outcomes and derive dynamic individualized predictions (Wulfsohn and Tsiatis, 1997; Tsiatis and Davidian, 2004; Rizopoulos, 2012).

The evaluation of the accuracy of these predictions obtained from joint models has gathered a lot of attention lately (Rizopoulos et al., 2017; Ferrer et al., 2019; Suresh et al., 2017). An important observation that has been made is that the accuracy of the derived predictions is influenced by the appropriate modeling of the subject-specific longitudinal profiles. In that regard, often in follow-up studies intermediate events occur in some patients that directly affect the shapes of their longitudinal evolutions. These may include events that are either directly in the control of the investigators, such as additional reinterventions, or may be not, such as adverse events that the patients may experience. While such intermediate events are common, very little work has been done in the direction of developing predictive tools that account for them and are adaptive to different scenarios with respect to their occurrence. To our knowledge, only Sène et al. (2016) and Taylor et al. (2005) investigated this topic in the context of prostate cancer recurrence and radiotherapy as an intermediate event. In their approach, however, they only considered the biomarker trajectories up to the occurrence of the intermediate event assuming extrapolation of the longitudinal profile thereafter. That is, changes in the shape of the longitudinal profile due to the occurrence of the intermediate event were not accounted for. Our goal is to show that utilizing the whole longitudinal trajectory, while capturing the changes to its shape due to the occurrence of intermediate events, can considerably improve the accuracy of such predictions.

In our work, we are motivated by two studies in which such intermediate events have been recorded during follow-up. The first study concerns 467 Congenital Heart Diseased (CHD) patients who underwent a Right Ventricular Outflow Tract (RVOT) reconstruction with a pulmonary valve and were followed-up echocardiographically thereafter, at the Department of Cardio-Thoracic surgery of Erasmus University Medical Center. Death is considered as the study endpoint while pulmonary gradient is the biomarker of interest which is believed to be related to the risk of death. During follow-up 65 (13.92%) were reoperated and received a pulmonary allograft. In Figure

2.1 the pulmonary gradient evolutions of 4 randomly selected patients, one from each combination between the reoperation and event status, are shown and it can be seen that when a patient is reoperated the pulmonary gradient drops. The interest in this study lies in the association between the pulmonary gradient and the risk of death but the main focus is to study the impact of reoperation on the risk of death both directly and indirectly (i.e. through its association with the pulmonary gradient) in order to develop predictive tools that can quantify the potential benefit of reoperation for future patients. The second study concerns 9361 subjects who participated in the SPRINT study (Group, 2015). Subjects with increased cardiovascular risk, systolic blood pressure of 130 mm Hg or higher but without diabetes, were randomized to intensive or standard treatment. The composite primary outcome was myocardial infarction, acute coronary syndromes, stroke, heart failure or death from cardiovascular causes while systolic blood pressure is the biomarker of interest which was repeatedly measured. During follow-up 3424 (36.6%) experienced serious adverse events (SAE). In Figure 2.2 the systolic blood pressure evolutions over time of the subjects who experienced SAEs and those who did not are depicted along with a loess curve for the average evolution over time for each group. The interest lies in assessing the impact of serious adverse events both in the systolic blood pressure evolution and the risk for the event of interest and exploiting it to derive individualized dynamic predictions for future patients with different scenarios with respect to the occurrence or not of SAEs. A more detailed description of the datasets is on the online supplementary material Sections S1.1 and S1.2.

In both studies, physicians are interested in obtaining predictions of the respective clinical endpoints. However, to provide predictions of adequate accuracy, it will be required to carefully model the subject-specific longitudinal trajectories. Borrowing ideas from piecewise regression models, we achieve this by explicitly introducing the occurrence of these intermediate events as binary time-varying covariates in the specification of both the longitudinal and survival submodels of the joint model. The regression coefficient associated with this covariate can then capture changes, due to the occurrence of the intermediate event, in both the biomarker trajectory and the hazard for the event of interest. Furthermore, we allow features of the biomarker trajectory, such as the rate of change to differ after the occurrence of the intermediate event. This allows us to estimate the impact of intermediate events as well as their specific features which then can be utilized in deriving dynamic predictions for a future patient under different scenarios: for example how the risk of a patient changes assuming different treatment strategies, such as no reintervention, reintervention now or reintervention at a later time-point.

The rest of the paper is structured as follows. Section 2.2 describes the formulation

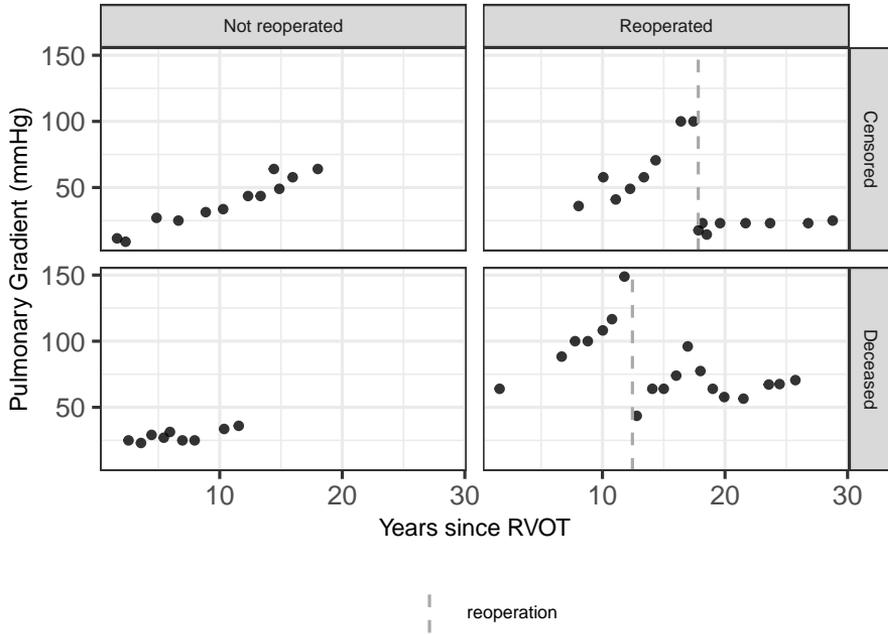


Figure 2.1: Pulmonary Gradient profile of 4 randomly selected patients, one from each of the following categories: Not Reoperated and Censored, Not Reoperated and Deceased, Reoperated and Censored, Reoperated and Deceased. The vertical red dashed lines depict the time of reoperation.

of the joint model in the presence of intermediate events. Section 2.3 presents the individualized dynamic predictions under different scenarios with respect to the occurrence of intermediate events and measures of predictive accuracy. In Section 2.4 we present the results of the analyses of the two motivating studies while in Section 2.5 we show the results of a simulation study. Finally, in Section 2.6 we close with a discussion.

2.2 Joint Model for Longitudinal and Time-to-Event Data with an Intermediate Event

Assuming n individuals under study, let $\mathcal{D}_n = \{T_i, \delta_i, \mathbf{y}_i, \rho_i; i = 1, \dots, n\}$ denote the sample from the target population, where $T_i = \min(T_i^*, C_i)$ denotes the observed event time, which is defined as the minimum value between the true event time T_i^* and the

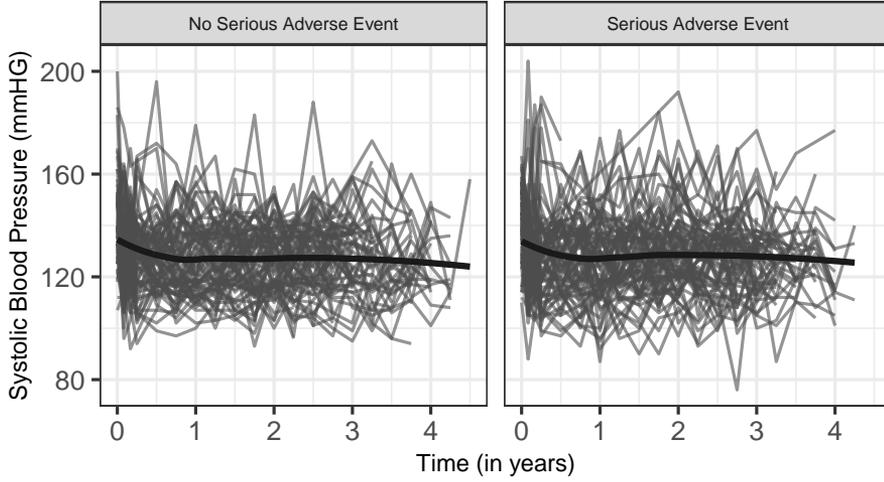


Figure 2.2: Individual evolutions and loess splines curves (solid thick lines) of systolic blood pressure for 80 randomly selected subjects who experienced a Serious Adverse Event and for 80 randomly selected subjects who did not experience a Serious Adverse Event.

censoring time C_i , and $\delta_i = I(T_i^* \leq C_i)$ the event indicator with $I(\cdot)$ being the indicator function which equals 1 if $T_i^* \leq C_i$ and 0 otherwise. Moreover, let ρ_i denote the time to the intermediate event with a corresponding indicator $R_i(t) = I(t \geq \rho_i)$ at any time t during follow-up, which takes the value 1 if a subject experienced the intermediate event and 0 otherwise. Furthermore, let $t_{i+} = \max(0, t_{ij} - \rho_i; j = 1, \dots, n_i)$ denote the time relative to the occurrence of the intermediate event and \mathbf{y}_i be the vector of size $n_i \times 1$ of repeated measurements for the i^{th} subject, with element y_{ij} being the observed value of the longitudinal outcome at time point t_{ij} , $j = 1, \dots, n_i$. We assume \mathbf{y}_i to be a contaminated with measurement error version of the true and unobserved value of the longitudinal outcome at any time t : $\mathbf{y}_i(t) = \boldsymbol{\eta}_i(t) + \boldsymbol{\epsilon}_i(t)$ with $\boldsymbol{\eta}_i(t)$ denoting the true value of the longitudinal outcome at time t and measurement error $\boldsymbol{\epsilon}_i(t) \sim \mathcal{N}(0, \sigma^2 I_{n_i})$. The true level of the longitudinal outcome is then formulated as:

$$\boldsymbol{\eta}_i(t) = \begin{cases} \mathbf{x}_i^\top(t) \boldsymbol{\beta} + \mathbf{z}_i^\top(t) \mathbf{b}_i, & 0 < t < \rho_i \\ \mathbf{x}_i^\top(t) \boldsymbol{\beta} + \mathbf{z}_i^\top(t) \mathbf{b}_i + \tilde{\mathbf{x}}_i^\top(t) \tilde{\boldsymbol{\beta}} + \tilde{\mathbf{z}}_i^\top(t) \tilde{\mathbf{b}}_i, & t \geq \rho_i, \end{cases} \quad (2.1)$$

where $\mathbf{x}_i^\top(t)$ and $\mathbf{z}_i^\top(t)$ are design vectors for the fixed-effects regression coefficients $\boldsymbol{\beta}$ and the random-effects \mathbf{b}_i respectively. Design vectors $\tilde{\mathbf{x}}_i^\top(t)$ and $\tilde{\mathbf{z}}_i^\top(t)$ include any function of the time-varying covariates $R_i(t)$ and t_{i+} , which describe the changes of the longitudinal trajectory after the occurrence of the intermediate event. These changes are then captured by the corresponding fixed-effects regression coefficients $\tilde{\boldsymbol{\beta}}$ allowing for subject-specific variation via the random-effects $\tilde{\mathbf{b}}_i$. The random-effects \mathbf{b}_i and $\tilde{\mathbf{b}}_i$ are assumed to be normally distributed with mean zero and a $q \times q$ variance-covariance matrix \mathbf{D} .

Depending on how the trajectory of the biomarker changes after the occurrence of the intermediate event, the specification of $\tilde{\mathbf{x}}_i^\top(t)$ and $\tilde{\mathbf{z}}_i^\top(t)$ may vary. Let $g\{R_i(t), t_{i+}\} = \tilde{\mathbf{x}}_i^\top(t)\tilde{\boldsymbol{\beta}} + \tilde{\mathbf{z}}_i^\top(t)\tilde{\mathbf{b}}_i$ denote the part of (2.1) which describes the changes in the longitudinal profile after the occurrence of the intermediate event. Then in a setting as the one illustrated in Figure 2.1, for the Pulmonary Gradient dataset, where the longitudinal trajectory is characterized by a seemingly linear evolution before and after the occurrence of the intermediate event, a steep drop at the occurrence of the intermediate event and a potential change in the slope after the occurrence of the intermediate event, function $g\{R_i(t), t_{i+}\}$ could be specified as $R_i(t)(\tilde{\beta}_1 + \tilde{b}_{i1}) + t_{i+}(\tilde{\beta}_2 + \tilde{b}_{i2})$. That is, the steep drop at the occurrence of the intermediate event will be captured by $(\tilde{\beta}_1 + \tilde{b}_{i1})$ and the change in the slope after the occurrence of the intermediate event will be captured by $(\tilde{\beta}_2 + \tilde{b}_{i2})$. On the other hand, in the setting of the SPRINT data where the longitudinal profiles show a nonlinear evolution over time without steep sudden changes, function $g\{R_i(t), t_{i+}\}$ could be specified as $\sum_{k=0}^Q (\tilde{\beta}_k + \tilde{b}_{ik}) B_k(t_{i+}, \mathbf{k})$ where $B_k(t_{i+}, \mathbf{k})$ denotes the k^{th} basis function of a B-spline with knots k_1, \dots, k_Q . In that case the change in the shape of the nonlinear longitudinal trajectory after the occurrence of the intermediate event will be captured by $\sum_{k=1}^Q (\tilde{\beta}_k + \tilde{b}_{ik})$ while there is no need to include $R_i(t)$. Generally, the functional form of $g\{R_i(t), t_{i+}\}$ may vary allowing for a broad range of mixed-effects models that can capture various types of changes in the longitudinal profile after the occurrence of the intermediate event.

Let $\mathcal{H}_i(t, \rho_i) = [\eta_i\{s, \rho_i(s)\}, 0 \leq s \leq t]$ denote the history of the longitudinal outcome up to time t . Note that in the definition of the history of the longitudinal outcome, we explicitly indicate that the true underlying value of the longitudinal outcome is also a function of the time to the intermediate event ρ_i . That is, to highlight that the subject-specific trajectory, $\eta_i(t)$, differs from the occurrence of the intermediate event onwards. Then the effects of the longitudinal outcome and the intermediate event, while adjusting for other covariates, on the risk for an event are quantified by utilizing a relative risk model of the form:

$$h_i\{t \mid \mathcal{H}_i(t, \rho_i), \mathbf{w}_i\} = \begin{cases} h_0(t) \exp \left[\gamma^\top \mathbf{w}_i + f_{t < \rho_i} \{ \mathcal{H}_i(t, \rho_i), \mathbf{b}_i \}^\top \boldsymbol{\alpha} \right], & 0 < t < \rho_i \\ h_0(t) \exp \left[\gamma^\top \mathbf{w}_i + \mathbf{1}\zeta + f_{t \geq \rho_i} \{ \mathcal{H}_i(t, \rho_i), \mathbf{b}_i \}^\top \boldsymbol{\alpha} \right], & t \geq \rho_i, \end{cases} \quad (2.2)$$

where $h_0(t)$ is the baseline risk function and \mathbf{w}_i is a vector of baseline covariates with a corresponding vector of regression coefficients γ . The effect of the intermediate event on the risk is captured by the regression coefficient ζ which quantifies the change in risk from the occurrence of the intermediate event onwards. Furthermore, the hazard of an event for patient i at any time t is associated with the subject-specific trajectory, $\eta_i(t)$, through $f\{\mathcal{H}_i(t, \rho_i), \mathbf{b}_i\}$ which is a function of the history of the longitudinal outcome up to time $\mathcal{H}_i(t, \rho_i)$ and/or the vector of subject-specific effects \mathbf{b}_i . Function $f_{(t, \rho_i)}\{\mathcal{H}_i(t, \rho_i), \mathbf{b}_i\}$ determines the association structure between the longitudinal and the time-to-event processes while the corresponding vector of regression coefficients $\boldsymbol{\alpha}$ quantifies the magnitude of the association. Several functional forms for the specification of the association structure have been used in the literature, such as the current value, current slope and the cumulative effect (Mauff et al., 2017). The functional form of the association structure is an important feature of the joint model formulation, especially with regard to the accuracy of the dynamic predictions (Rizopoulos et al., 2017,0; Andrinopoulou et al., 2017). Hence, to allow for more flexibility we explicitly allow for the functional form of the association structure to differ before and after the occurrence of the intermediate event. In general, any functional form can be used for $f_{t \geq \rho_i}\{\mathcal{H}_i(t, \rho_i), \mathbf{b}_i\}$ and $f_{t < \rho_i}\{\mathcal{H}_i(t, \rho_i), \mathbf{b}_i\}$ including, of course, the case where the association structure remains the same and $f_{t \geq \rho_i}\{\mathcal{H}_i(t, \rho_i), \mathbf{b}_i\} = f_{t < \rho_i}\{\mathcal{H}_i(t, \rho_i), \mathbf{b}_i\}$.

The estimation of the parameters of the proposed joint model is achieved under the Bayesian framework using Markov Chain Monte Carlo (MCMC) algorithms. For more details regarding Bayesian estimation of joint models the reader may refer to Rizopoulos (2016), Ibrahim et al. (2001)] and Brown et al. (2005).

2.3 Individualized Dynamic Predictions with Time-varying Intermediate Events

2.3.1 Dynamic Predictions

Based on the joint model fitted in the sample $\mathcal{D}_n = \{T_i, \delta_i, \mathbf{y}_i, \rho_i; i = 1, \dots, n\}$ from the target population, dynamic predictions for a new subject j from the same population can be derived up to a future time of interest $u > t$ given his/hers biomarker

history $\mathcal{H}_j(t) = [\eta_j\{s, R_j(s)\}, 0 \leq s \leq t]$. Let $\mathcal{Y}_j(t) = \{y_j(t_{jl}); 0 \leq t_{jl} \leq t, l = 1, \dots, n_j\}$ denote the history of observed biomarker values taken up to time t for patient j , then under the Bayesian joint model framework these predictions can be estimated using the corresponding posterior predictive distributions, namely:

$$\begin{aligned}
 \pi_j(u | t) &= Pr\{T_j^* \geq u | T_j^* > t, \mathcal{Y}_j(t), \boldsymbol{\theta}\} \\
 &= \int \frac{S_j\{u | \mathcal{H}_j(u, \mathbf{b}_j), \boldsymbol{\theta}\}}{S_j\{t | \mathcal{H}_j(t, \mathbf{b}_j), \boldsymbol{\theta}\}} p\{\mathbf{b}_j | T_j^* > t, \mathcal{Y}_j(t), \boldsymbol{\theta}\} d\mathbf{b}_j \\
 &= \int \exp\left[-\int_t^u h_j\{s | \mathcal{H}_j(u, \mathbf{b}_j)\} ds\right] p\{\mathbf{b}_j | T_j^* > t, \mathcal{Y}_j(t), \boldsymbol{\theta}\} d\mathbf{b}_j, \\
 &\quad t \leq s \leq u.
 \end{aligned} \tag{2.3}$$

Note that in equation 2.3 and for the remainder of the text, covariates w_j and x_j are suppressed from notation for simplicity and without loss of generality. Expressing the fraction term in (2.3) as $\exp\{-\int_t^u h_i(s) ds\}, t \leq s \leq u$ has two main advantages. First, it reduces the computational time required, since the denominator part $S_j\{t | \mathcal{H}_j(t, \mathbf{b}_j), \boldsymbol{\theta}\}$ does not need to be computed anymore. Second, it improves the precision of numerical integration. The latter benefit is due to the fact that by re-expressing the fraction term in (2.3) as such, an adaptive Gauss-Kronrod scheme can be deployed for the numerical computation of smaller regions of the target interval. This improves the precision of Gaussian quadrature since the quadrature points are spent for smaller regions of the interval.

Incorporating the time-varying covariate $R_i(t)$ in both the longitudinal and relative risk submodels of the joint model allows us to evaluate how the occurrence of the intermediate event of interest at a future time point will influence the individualized risk predictions, for subjects who have not experienced the intermediate event by time t . The main difference of our approach when compared with the approach of Sène et al. (2016), is that we assume that both the instantaneous risk of the primary endpoint and the longitudinal profile change after the occurrence of the intermediate event, whereas they assumed an extrapolated longitudinal profile, instead. More specifically, by assuming an extrapolated longitudinal profile, Sène et al. (2016), were more interested in assessing how predictions change with and without a second treatment whereas we are more interested in studying how individualized risk predictions are influenced by intermediate events, such as reintervention or adverse events, by explicitly allowing for changes in both the longitudinal and survival submodels.

That is, different scenarios regarding the time of the intermediate event may lead to changes in the risk captured via different individual dynamic predictions accordingly. More specifically, for a future time of interest $u > t$ different assumptions can be made: 1) The patient experiences an intermediate event immediately $\rho_i = t$ or at a time point within the time-interval of prediction $t \leq \rho_i \leq u$. 2) The patient does not experience an intermediate event within the time-interval of prediction $\rho_i > u$. The individualized dynamic predictions in (2.4) are then further dependent on the scenario of choice:

$$\pi_j(u | t, \rho_j) = \begin{cases} \int \exp \left\{ - \int_t^u h_j(s | b_j, \rho_j \leq u) ds \right\} \times \\ p \left\{ b_j | T_j^* > t, \mathcal{Y}_j(t, t \leq \rho_j \leq u), \boldsymbol{\theta} \right\} db_j, t \leq \rho_j \leq u \\ \\ \int \exp \left\{ - \int_t^u h_j(s | b_j, \rho_j > u) ds \right\} \times \\ p \left\{ b_j | T_j^* > t, \mathcal{Y}_j(t, t \leq u \leq \rho_j), \boldsymbol{\theta} \right\} db_j, t \leq u < \rho_j. \end{cases} \quad (2.4)$$

In Equation (2.4) the full conditional posterior density of the random effects can be analytically expressed as $\left\{ p \left(T_j^* > t | \rho_j \leq u, b_j \right) \right\} \prod_l \left\{ p \left(y_j | \rho_j \leq u, b_j \right) \right\} p \left(\mathbf{b}_j | \boldsymbol{\theta} \right)$ for $t \leq \rho_j \leq u$ and as $\left\{ p \left(T_j^* > t | \rho_j \leq u, b_j \right) \right\} \prod_l \left\{ p \left(y_j | \rho_j > u, b_j \right) \right\} p \left(\mathbf{b}_j | \boldsymbol{\theta} \right)$ for $t \leq u < \rho_j$, where $\prod_l \left\{ p \left(y_j | \rho_j \leq u, b_j \right) \right\}$ and $\prod_l \left\{ p \left(y_j | \rho_j > u, b_j \right) \right\}$ are multivariate Gaussian joint densities for the longitudinal responses with means $\mathbf{x}_j^\top(t) \boldsymbol{\beta} + R_j(t) \boldsymbol{\beta}_R + t_+ \boldsymbol{\beta}_{t_+} + \mathbf{z}_j^\top(t) \mathbf{b}_j + R_j(t) b_{jR} + t_+ b_{jt_+}$ and $\mathbf{x}_j^\top(t) \boldsymbol{\beta} + \mathbf{z}_j^\top(t) \mathbf{b}_j$ respectively and variance-covariance matrices $\sigma^2 I_{n_j}$. $p \left(\mathbf{b}_j | \boldsymbol{\theta} \right)$ is a multivariate Gaussian density function with mean 0 and variance covariance matrix D .

To estimate $\pi_j(u | t, \rho_j)$ a Monte Carlo scheme is employed, for the integration over the random-effects, where a large set of θ^m ($m = 1, \dots, M$) and b_j^m ($m = 1, \dots, M$) are sampled from their posterior distributions and subsequently used to compute $\pi_j^m(u | t, \rho_j)$. The median value of $\pi_j^m(u | t, \rho_j)$ is the point estimate and the 2.5% and 97.5% percentiles give a 95% credible interval.

2.3.2 Evaluation of predictive performance

To assess the performance of the individualized dynamic predictions described in the previous section, we will work under a similar framework as the one presented in (Rizopoulos et al., 2017). More specifically, we will use the time-dependent area under the receiver operating characteristic curve (AUC) and the expected prediction error (PE), adapted for the presence of intermediate events.

Under the framework presented in Sections 2 and 3.1 a rule can be defined using the individualized dynamic predictions $\pi_j(u = t + \Delta t | t)$ while utilizing the available longitudinal measurements up to t , $\mathcal{Y}_j(t)$. More specifically, a subject j can be termed as either to experience the event $\pi_j(u = t + \Delta t | t) \leq c$ or not $\pi_j(u = t + \Delta t | t) > c$ within a clinically relevant time interval $(t, \Delta t]$, with $c \in [0, 1]$. That is, for a pair of subjects which is randomly chosen $\{i, j\}$ for both of which the measurements up to t are provided, the AUC which is calculated for varying values of c is a measure of the discriminative capability of the assumed model and is given by:

$$\text{AUC}(t, \Delta t) = \Pr \left[\pi_i(t + \Delta t | t) < \pi_j(t + \Delta t | t) \mid \{T_i^* \in (t, t + \Delta t]\} \cap \{T_j^* > t + \Delta t\} \right], \quad (2.5)$$

which intuitively means that we expect the assumed model to give higher probability of surviving longer than the time interval of interest $(t + \Delta t]$ to the subject who did not experience the event (in this case subject j).

However, in the presence of intermediate events, the dynamic predictions change depending on whether a subject experienced the intermediate event or not. That is, the AUC in (2.5) changes to:

$$\text{AUC}(t, \Delta t) = \begin{cases} \Pr \left[\pi_i(t + \Delta t | t, \rho_i > t) < \pi_j(t + \Delta t | t, \rho_i > t) \mid \{T_i^* \in (t, t + \Delta t]\} \cap \{T_j^* > t + \Delta t\} \right], & 0 < t < \rho_i, \rho_j \\ \Pr \left[\pi_i(t + \Delta t | t, \rho_i \leq t) < \pi_j(t + \Delta t | t, \rho_i \leq t) \mid \{T_i^* \in (t, t + \Delta t]\} \cap \{T_j^* > t + \Delta t\} \right], & t \geq \rho_i, \rho_j. \end{cases}$$

Estimation of $\text{AUC}(t, \Delta t)$ is based in counting the concordant pairs of subjects by appropriately distinguishing between the comparable and the non-comparable (due to censoring) pairs of subjects at time t . More specifically, the following decomposition is used:

$$\hat{\text{AUC}}(t, \Delta t) = \hat{\text{AUC}}_1(t, \Delta t) + \hat{\text{AUC}}_2(t, \Delta t) + \hat{\text{AUC}}_3(t, \Delta t) + \hat{\text{AUC}}_4(t, \Delta t).$$

Term $\hat{\text{AUC}}_1(t, \Delta t)$ refers to the pairs of subjects who are comparable,

$$\Omega_{ij}^{(1)}(t) = \begin{cases} [\{T_i \in (t, t + \Delta t]\} \cap \{\delta_i = 1\} \cap \{0 < t < \rho_i\}] \cap [\{T_j > t + \Delta t\} \cap \{0 < t < \rho_j\}], \\ 0 < t < \rho_i, \rho_j \\ [\{T_i \in (t, t + \Delta t]\} \cap \{\delta_i = 1\} \cap \{t \geq \rho_i\}] \cap [\{T_j > t + \Delta t\} \cap \{t \geq \rho_j\}], \\ t \geq \rho_i, \rho_j, \end{cases}$$

where $i, j = 1, \dots, n$ with $i \neq j$. We can then estimate and compare the survival probabilities $\pi_i(t + \Delta t | t, t \geq \rho_i)$ and $\pi_j(t + \Delta t | t, t \geq \rho_j)$ for subjects i and j who did not experienced the intermediate event and $\pi_i(t + \Delta t | t, 0 < t < \rho_i)$ and $\pi_j(t + \Delta t | t, 0 < t < \rho_j)$ for subjects who experienced the intermediate event. Then $\hat{AUC}_1(t, \Delta t)$ is the proportion of concordant subjects out of the set of comparable subjects at time t :

$$\hat{AUC}_1(t, \Delta t) = \frac{\sum_{i \in \mathcal{A}} \sum_{j \neq i \in \mathcal{A}} I\{\hat{\pi}_i(t + \Delta t | t, t < \rho_i) < \hat{\pi}_j(t + \Delta t | t, t < \rho_j)\} \times I\{\Omega_{ij}^{(1)}(t)\}}{\sum_{i \in \mathcal{A}} \sum_{j \neq i \in \mathcal{A}} I\{\Omega_{ij}^{(1)}(t)\}} + \frac{\sum_{i \in \mathcal{B}} \sum_{j \neq i \in \mathcal{B}} I\{\hat{\pi}_i(t + \Delta t | t, t \geq \rho_i) < \hat{\pi}_j(t + \Delta t | t, t \geq \rho_j)\} \times I\{\Omega_{ij}^{(1)}(t)\}}{\sum_{i \in \mathcal{B}} \sum_{j \neq i \in \mathcal{B}} I\{\Omega_{ij}^{(1)}(t)\}},$$

where $\mathcal{A} = \{i, j : t < \rho_i; i, j = 1, \dots, n\}$ and $\mathcal{B} = \{i, j : t \geq \rho_i; i, j = 1, \dots, n\}$. The remaining terms, $\hat{AUC}_2(t, \Delta t)$, $\hat{AUC}_3(t, \Delta t)$ and $\hat{AUC}_4(t, \Delta t)$ refer to the pairs of subjects who due to censoring cannot be compared, namely

$$\Omega_{ij}^{(2)}(t) = \begin{cases} [\{T_i \in (t, t + \Delta t)\} \cap \{\delta_i = 0\} \cap \{0 < t < \rho_i\}] \cap [\{T_j > t + \Delta t\} \cap \{0 < t < \rho_j\}], \\ 0 < t < \rho_i, \rho_j \\ [\{T_i \in (t, t + \Delta t)\} \cap \{\delta_i = 0\} \cap \{t \geq \rho_i\}] \cap [\{T_j > t + \Delta t\} \cap \{t \geq \rho_j\}], \\ t \geq \rho_i, \rho_j, \end{cases}$$

$$\Omega_{ij}^{(3)}(t) = \begin{cases} [\{T_i \in (t, t + \Delta t)\} \cap \{\delta_i = 1\} \cap \{0 < t < \rho_i\}] \cap [\{T_i < T_j \leq t + \Delta t\} \cap \\ \{0 < t < \rho_j\} \cap \{\delta_j = 0\}], 0 < t < \rho_i, \rho_j \\ [\{T_i \in (t, t + \Delta t)\} \cap \{\delta_i = 1\} \cap \{t \geq \rho_i\}] \cap [\{T_i < T_j \leq t + \Delta t\} \cap \\ \{t \geq \rho_j\} \cap \{\delta_j = 0\}], t \geq \rho_i, \rho_j, \end{cases}$$

$$\Omega_{ij}^{(4)}(t) = \begin{cases} [\{T_i \in (t, t + \Delta t)\} \cap \{\delta_i = 0\} \cap \{0 < t < \rho_i\}] \cap [\{T_i < T_j \leq t + \Delta t\} \cap \\ \{0 < t < \rho_j\} \cap \{\delta_j = 0\}], 0 < t < \rho_i, \rho_j \\ [\{T_i \in (t, t + \Delta t)\} \cap \{\delta_i = 0\} \cap \{t \geq \rho_i\}] \cap [\{T_i < T_j \leq t + \Delta t\} \cap \\ \{t \geq \rho_j\} \cap \{\delta_j = 0\}], t \geq \rho_i, \rho_j, \end{cases}$$

which contribute to the overall AUC after being appropriately weighted with the probability that they would be comparable:

$$\begin{aligned} \hat{\text{AUC}}_m(t, \Delta t) = & \frac{\sum_{i \in \mathcal{A}} \sum_{j \neq i \in \mathcal{A}} I\{\hat{\pi}_i(t + \Delta t | t, t < \rho_i) < \hat{\pi}_j(t + \Delta t | t, t < \rho_j)\} \times I\{\Omega_{ij}^{(m)}(t)\} \times \hat{\nu}_{ij}^{(m)}}{\sum_{i \in \mathcal{A}} \sum_{j \neq i \in \mathcal{A}} I\{\Omega_{ij}^{(m)}(t)\} \times \hat{\nu}_{ij}^{(m)}} \\ & + \frac{\sum_{i \in \mathcal{B}} \sum_{j \neq i \in \mathcal{B}} I\{\hat{\pi}_i(t + \Delta t | t, t \geq \rho_i) < \hat{\pi}_j(t + \Delta t | t, t \geq \rho_j)\} \times I\{\Omega_{ij}^{(m)}(t)\} \times \hat{\nu}_{ij}^{(m)}}{\sum_{i \in \mathcal{B}} \sum_{j \neq i \in \mathcal{B}} I\{\Omega_{ij}^{(m)}(t)\} \times \hat{\nu}_{ij}^{(m)}}, \end{aligned}$$

with $m = 2, 3, 4$ and

$$\hat{\nu}_{ij}^{(2)} = \begin{cases} 1 - \hat{\pi}_i(t + \Delta t | T_i, t < \rho_i), & i \in \mathcal{A} \\ 1 - \hat{\pi}_i(t + \Delta t | T_i, t \geq \rho_i), & i \in \mathcal{B}, \end{cases}$$

$$\hat{\nu}_{ij}^{(3)} = \begin{cases} \hat{\pi}_j(t + \Delta t | T_j, t < \rho_j), & j \in \mathcal{A} \\ \hat{\pi}_j(t + \Delta t | T_j, t \geq \rho_j), & j \in \mathcal{B}, \end{cases}$$

$$\hat{\nu}_{ij}^{(4)} = \begin{cases} \{1 - \hat{\pi}_i(t + \Delta t | T_i, t < \rho_i)\} \times \hat{\pi}_j(t + \Delta t | T_j, t < \rho_j), & i, j \in \mathcal{A} \\ \{1 - \hat{\pi}_i(t + \Delta t | T_i, t \geq \rho_i)\} \times \hat{\pi}_j(t + \Delta t | T_j, t \geq \rho_j), & i, j \in \mathcal{B}. \end{cases}$$

The expected error of predicting future events can be used to assess the accuracy of individualized dynamic predictions. Similarly as for the AUC, to account for the dynamic nature of the longitudinal outcome, we focus our interest in predicting events that occur at a time point $u > t$ given the information available up to time t , $\mathcal{Y}_j(t)$. Let $N_j(t) = I(T_i^* > t)$ denote the event status of subject j at time t . Using the square loss function the expected prediction error then is:

$$\text{PE}(u | t) = E \left[\{N_j(u) - \pi_j(u | t)\}^2 \right], \quad (2.6)$$

where the expectation is taken with respect to the distribution of the event times. Adapting the above to the framework of intermediate events, (2.6) can be re-expressed as:

$$\text{PE}(u | t) = \begin{cases} E \left[\{N_j(u) - \pi_j(u | t, \rho_i > t)\}^2 \right], & 0 < t < \rho_i \\ E \left[\{N_j(u) - \pi_j(u | t, \rho_i \leq t)\}^2 \right], & t \geq \rho_i, \end{cases}$$

where for each case the corresponding individualized dynamic predictions showed in (2.4) are used. The estimate of $\text{PE}(u | t)$ as proposed Henderson et al. (2002) and adjusted for the presence of intermediate events is given by:

$$\begin{aligned}
 \hat{\text{PE}}(u | t, \rho_i) = & \{n(t, t < \rho_i)\}^{-1} \sum_{i \in \mathcal{A}, T_i \geq t} I(T_i \geq u) \{1 - \hat{\pi}_i(u | t, t < \rho_i)\}^2 + \\
 & \delta_i I(T_i < u) \{0 - \hat{\pi}_i(u | t, t < \rho_i)\}^2 + \\
 & (1 - \delta_i) I(T_i < u) \left[\hat{\pi}_i(u | T_i, t < \rho_i) \{1 - \hat{\pi}_i(u | t, t < \rho_i)\}^2 \{1 - \hat{\pi}_i(u | T_i, t < \rho_i)\} \times \right. \\
 & \left. \{0 - \hat{\pi}_i(u | t, t < \rho_i)\}^2 \right] + \{n(t, t \geq \rho_i)\}^{-1} \sum_{i \in \mathcal{B}, T_i \geq t} I(T_i \geq u) \{1 - \hat{\pi}_i(u | t, t \geq \rho_i)\}^2 + \\
 & \delta_i I(T_i < u) \{0 - \hat{\pi}_i(u | t, t \geq \rho_i)\}^2 (1 - \delta_i) I(T_i < u) \\
 & \left[\hat{\pi}_i(u | T_i, t \geq \rho_i) \{1 - \hat{\pi}_i(u | t, t \geq \rho_i)\}^2 \times \right. \\
 & \left. \{1 - \hat{\pi}_i(u | T_i, t \geq \rho_i)\} \{0 - \hat{\pi}_i(u | t, t < \rho_i)\}^2 \right],
 \end{aligned}$$

where $n(t, t < \rho_i)$ and $n(t, t \geq \rho_i)$ denote the number of subjects still at risk at time t , who have not/have experienced the intermediate event respectively.

2.4 Analysis of Pulmonary Gradient and SPRINT trial data

2.4.1 Pulmonary Gradient dataset

The Pulmonary Gradient dataset was introduced in Section 1. Our goal, is to investigate the association between the pulmonary gradient and the risk of death, how reoperation as an intermediate event changes the evolution of the pulmonary gradient and the instantaneous risk for death, and then to utilize this information to derive individualized dynamic predictions under different scenarios with respect to a future time of reoperation.

In Figure 2.1, the evolutions of pulmonary gradient for reoperated and non reoperated patients are depicted, where it is shown that for the case of reoperated patients the profiles are characterized by a linear increasing trend which drops at the moment of reoperation and then continues to increase whereas for the case of non reoperated patients the profiles show a linear increasing trend. Therefore, for this outcome, we assumed a linear mixed-effects submodel including a linear effect of time, a drop at the moment of reoperation and a change in slope after the occurrence of reoperation in both the fixed-effects and random-effects parts of the model while correcting for baseline differences in age and sex. A preliminary analysis suggested that assuming nonlinear effects of time did not improve the fit of the model to the data. Hence, we used the following specification for the mixed-effects model:

$$PG_i(t) = \begin{cases} (\beta_0 + b_{i0}) + (\beta_1 + b_{i1}) \times t_i + \beta_4 Age_i + \beta_5 Sex_i + \epsilon_i(t), & 0 < t < \rho_i \\ (\beta_0 + b_{i0}) + (\beta_1 + b_{i1}) \times t_i + (\tilde{\beta}_2 + \tilde{b}_{i2}) \\ \times R_i(t) + (\tilde{\beta}_3 + \tilde{b}_{i3}) \times t_{i+} + \beta_4 Age_i + \beta_5 Sex_i + \epsilon_i(t), & t \geq \rho_i. \end{cases}$$

where $PG_i(t)$ are the measurements of pulmonary gradient, $R_i(t)$ is a binary time-dependent indicator of reoperation and $t_{i+} = \max(0, t_{ij} - \rho_{ij}; j = 1, \dots, n_i)$ is the time relative to reoperation.

To investigate the association between the pulmonary gradient and the risk of death, we postulated relative risk submodels with different parametrizations for the pulmonary gradient. The baseline hazard was expressed as a B-splines function. We also corrected for age and sex and assumed reoperation to have a direct effect on the hazard. Based on a preliminary analysis we assessed various formulations for the association structure. However, only functional forms including the slope of the pulmonary gradient were found to be stronger. Assuming a different functional form after the occurrence of reoperation did not improve the fit of the model to the data. Therefore, we present the joint models that include the slope of the pulmonary gradient along with the joint model that assumes an association with the current value of the pulmonary gradient for the sake of comparison, since it is the most common form of the association structure:

$$M1 : h_i(t) = h_0(t) \exp\{\gamma_1 Age_i + \gamma_2 Sex_i + \zeta R_i(t) + \alpha_1 \eta_{PG_i}(t)\},$$

$$M2 : h_i(t) = h_0(t) \exp\{\gamma_1 Age_i + \gamma_2 Sex_i + \zeta R_i(t) + \alpha_1 \eta_{PG_i}(t) + \alpha_2 \frac{d}{dt} \eta_{PG_i}(t)\},$$

$$M3 : h_i(t) = h_0(t) \exp\{\gamma_1 Age_i + \gamma_2 Sex_i + \zeta R_i(t) + \alpha_2 \frac{d}{dt} \eta_{PG_i}(t)\}.$$

Table 2.1 summarizes the parameter estimates and the 95% credibility intervals of the longitudinal submodel that was used for the Pulmonary Gradient dataset. Table 2.2 summarizes the parameter estimates and the 95% credibility intervals of the survival submodels based on the three joint models fitted to the Pulmonary Gradient dataset. As shown in Table 2, the association of the pulmonary gradient with the instantaneous risk of death was weak regardless the functional form of the association structure. The strongest association in magnitude was found when using the slope parametrization both before and after the occurrence of the intermediate event.

Despite the weak magnitude of the association, reoperation was found to have a strong effect on the longitudinal evolution of pulmonary gradient. The fitted joint

Table 2.1: Estimated coefficients and 95% credibility intervals for the parameters of the longitudinal submodel fitted to the Pulmonary Gradient dataset.

	Est.	95% CI
β_0	23.41	(20.677; 26.068)
β_1	0.99	(0.797; 1.178)
$\tilde{\beta}_2$	-12.83	(-18.735; -6.647)
$\tilde{\beta}_3$	-0.02	(-0.994; 1.198)
β_4	-0.13	(-0.226; -0.033)
β_5	-4.01	(-6.671; -1.306)
σ	10.52	(10.262; 10.8)

Table 2.2: Estimated hazard ratios and 95% credibility intervals for the parameters of the survival submodels based on the three joint models fitted to the Pulmonary Gradient dataset. Age at baseline is measured in years, α_1 and α_2 are measured in the units of the pulmonary gradient (mmHg) when referring to the current value association and in (mmHg/time) when referring to the current slope association.

	Value		Value + Slope		Slope	
	HR	95% CI	HR	95% CI	HR	95% CI
γ_1	1.05	(1.03; 1.078)	1.06	(1.03; 1.083)	1.06	(1.03; 1.08)
γ_2	0.51	(0.223; 1.073)	0.52	(0.235; 1.099)	0.51	(0.25; 1.061)
ζ	0.34	(0.056; 1.399)	0.32	(0.042; 1.406)	0.31	(0.042; 1.255)
α_1	1.01	(0.992; 1.031)	1.01	(0.983; 1.032)	1.32	(0.783; 1.919)
α_2			1.17	(0.624; 1.987)		

models can be used to show how individualized dynamic predictions can be derived for a new subject, under different scenarios with respect to the timing of reoperation in the future. For this illustration, we will use model M3 since the slope parametrization was found to have a stronger effect on the instantaneous risk of death. In Figure 2.3 the individual prediction of survival for a subject with 7 measurements of pulmonary gradient, so far, are shown under the assumptions of no reoperation in the future versus reoperation immediately and after four years respectively. As shown in Figure 2.3, reoperation improves the survival probability for the new subject regardless its timing. When the reoperation is not assumed to be immediate, the survival curves

overlap up to the point of reoperation and then separate, depicting the improvement on the survival probability for this subject due to reoperation.

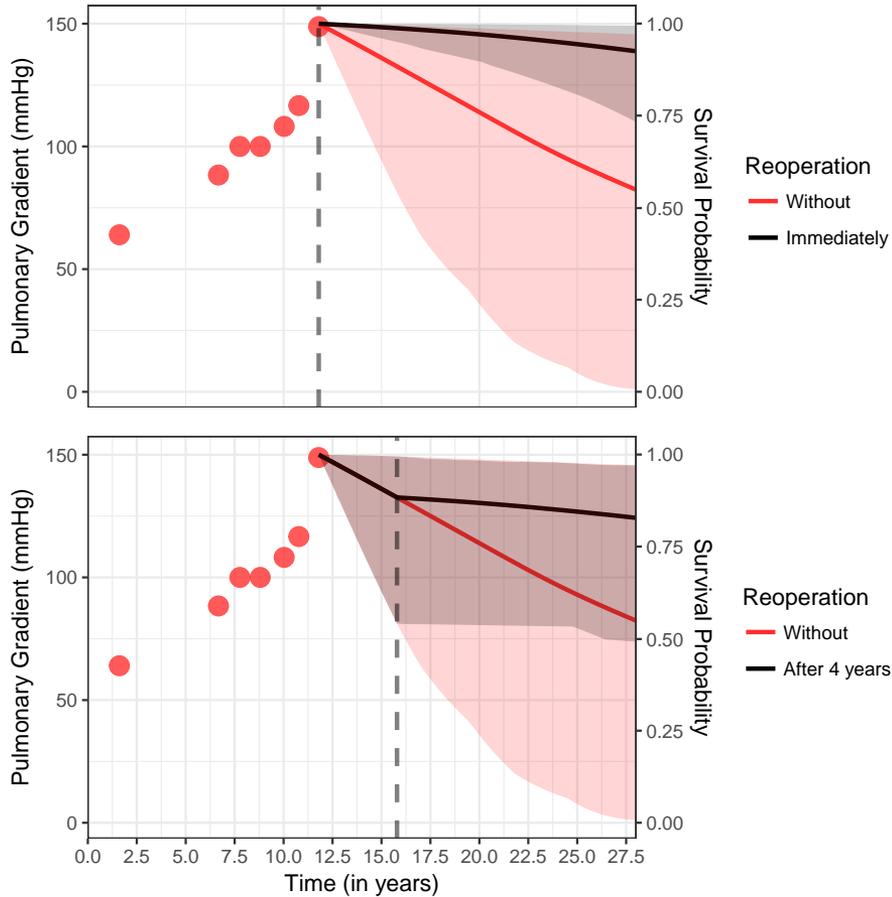


Figure 2.3: Survival Probabilities for a new subject under different scenarios with respect to the timing of reoperation. The vertical gray dashed line depicts the time of reoperation.

2.4.2 SPRINT dataset

The SPRINT dataset was also introduced in Section 1. Our goal, is to investigate how serious adverse events during follow-up change the evolution of the systolic blood pressure and the instantaneous risk for the composite endpoint, and then to utilize this

information to derive individualized dynamic predictions under different scenarios with respect to the occurrence of serious adverse events in the future.

In Figure 2.2, a random sample of the evolutions of systolic blood pressure for patients who experienced and who did not experience serious adverse events are depicted. For both sets of patients, the profiles show diverse nonlinear trends which we assume to change after the occurrence of serious adverse events. Therefore, for this outcome, we assumed a nonlinear mixed-effects submodel using natural cubic splines with 3 knots for the effect of time, and the effect of time relative to the occurrence of serious adverse events in both the fixed-effects and random-effects parts of the model while adjusting for differences in treatment. More specifically, the following specification for the mixed-effects model was used:

$$SBP_i(t) = \begin{cases} (\beta_0 + b_{i0}) + \left(\sum_{k=0}^3 (\beta_{(k+1)} + b_{i(k+1)}) B_k(t, \mathbf{k}) \right) + \beta_5 \text{Treatment}_i + \\ \left(\sum_{k=0}^3 \beta_{(k+6)} B_k(t, \mathbf{k}) \right) \times \text{Treatment}_i + \epsilon_i(t), 0 < t < \rho_i \\ (\beta_0 + b_{i0}) + \left(\sum_{k=0}^3 (\beta_{(k+1)} + b_{i(k+1)}) B_k(t, \mathbf{k}) \right) + \beta_5 \text{Treatment}_i + \\ \left(\sum_{k=0}^3 \beta_{(k+6)} B_k(t, \mathbf{k}) \right) \times \text{Treatment}_i + \\ \left(\sum_{k=0}^3 (\tilde{\beta}_{(k+10)} + \tilde{b}_{i(k+10)}) B_k(t_+, \mathbf{k}) \right) + \\ \left(\sum_{k=0}^3 \tilde{\beta}_{(k+14)} B_k(t_+, \mathbf{k}) \right) \times \text{Treatment}_i + \epsilon_i(t), t \geq \rho_i. \end{cases}$$

where $SBP_i(t)$ are the measurements of systolic blood pressure and $t_{i+} = \max(0, t_{ij} - \rho_{ij}; j = 1, \dots, n_i)$ is the time relative to the occurrence of serious adverse event.

To investigate the association between the systolic blood pressure and the composite endpoint, we postulated relative risk submodels with different parametrizations for the systolic blood pressure. The baseline hazard was expressed as a B-splines function. We also corrected for treatment and assumed the occurrence of serious adverse event to have a direct effect on the hazard. The functional forms we used for the association structure were the current value, slope, area, both the current value and slope, as well as more elaborate ones assuming that the value, slope, and area all have an effect on the hazard and assuming that after the occurrence of the serious adverse event the effect of the current slope on the hazard changes. The joint models are given in detail below:

$$M4 : h_i(t) = h_0(t) \exp\{\gamma_1 \text{Treatment}_i + \zeta R_i(t) + \alpha_1 \eta_{SBP_i}(t)\},$$

$$M5 : h_i(t) = h_0(t) \exp\{\gamma_1 \text{Treatment}_i + \zeta R_i(t) + \alpha_2 \frac{d}{dt} \eta_{SBP_i}(t)\},$$

$$M6 : h_i(t) = h_0(t) \exp\{\gamma_1 \text{Treatment}_i + \zeta R_i(t) + \alpha_1 \eta_{SBP_i}(t) + \alpha_2 \frac{d}{dt} \eta_{SBP_i}(t)\}.$$

$$M7 : h_i(t) = h_0(t) \exp\{\gamma_1 \text{Treatment}_i + \zeta R_i(t) + \alpha_3 \int_0^t \eta_{SBP_i}(s) ds\}.$$

$$M8 : h_i(t) = h_0(t) \exp\{\gamma_1 \text{Treatment}_i + \zeta R_i(t) + \alpha_1 \eta_{SBP_i}(t) + \alpha_2 \frac{d}{dt} \eta_{SBP_i}(t) + \alpha_3 \int_0^t \eta_{SBP_i}(s) ds\}.$$

$$M9 : h_i(t) = h_0(t) \exp\{\gamma_1 \text{Treatment}_i + \zeta R_i(t) + \alpha_1 \eta_{SBP_i}(t) + \alpha_2 \frac{d}{dt} \eta_{SBP_i}(t) + \alpha_3 R_i(t) \times \frac{d}{dt} \eta_{SBP_i}(t)\}.$$

Table 2.3 summarizes the parameter estimates and the 95% credibility intervals of the longitudinal submodel that was used for the SPRINT dataset. Tables 2.4 and 2.5 summarize the parameter estimates and the 95% credibility intervals of the survival submodels based on the six joint models fitted to the SPRINT dataset. As shown in Tables 2.4 and 2.5, the association of the pulmonary gradient with the instantaneous risk of composite endpoint was weak in magnitude but significant in the cases of value and slope association and area association.

Similarly, as for the Pulmonary Gradient Dataset, in Figure 2.4 we illustrate how the individualized subject-specific predictions for the composite endpoint of interest change under different scenarios for the timing of the occurrence of a serious adverse event. More specifically, we illustrate the cases of an immediate occurrence of the adverse event and an occurrence after a year using the joint model that postulates effects of both the current value and current slope of the systolic blood pressure trajectory on the instantaneous risk of the composite endpoint. In both cases, the occurrence of the serious adverse event worsens the survival probability considerably.

Finally, as an illustration of the use of the predictive performance measures, as they were presented in Section 3, we refer the reader to the online supplementary material S2 where we present a comparison in terms of the AUC and the PE for the SPRINT data where the extrapolation method (that is ignoring the longitudinal data observed after the occurrence of the intermediate event) and the proposed model are compared.

Table 2.3: Estimated coefficients and 95% credibility intervals for the parameters of the longitudinal submodel fitted to the SPRINT dataset.

	Est.	95% CI
β_0	137.95	(137.549; 138.32)
β_1	-1.33	(-1.808; -0.851)
β_2	-0.40	(-0.873; 0.05)
β_3	-8.39	(-9.302; -7.505)
β_4	1.01	(0.574; 1.407)
β_5	-0.57	(-1.116; 0.021)
β_6	-13.45	(-14.125; -12.778)
β_7	-11.10	(-11.734; -10.456)
β_8	-25.93	(-27.184; -24.583)
β_9	-9.51	(-10.094; -8.938)
$\tilde{\beta}_{10}$	0.06	(-0.954; 1.088)
$\tilde{\beta}_{11}$	-0.06	(-1.282; 1.181)
$\tilde{\beta}_{12}$	-1.82	(-3.097; -0.389)
$\tilde{\beta}_{13}$	-0.62	(-2.402; 1.268)
$\tilde{\beta}_{14}$	1.84	(0.423; 3.333)
$\tilde{\beta}_{15}$	0.35	(-1.321; 2.107)
$\tilde{\beta}_{16}$	5.06	(2.983; 6.847)
$\tilde{\beta}_{17}$	1.48	(-1.028; 3.808)
σ	11.22	(11.164; 11.266)

2.4.3 Software

The R package **JMbayes** was extended to appropriately account for the occurrence of intermediate events and deriving individualized dynamic predictions under different scenarios with respect to the occurrence of the intermediate event. These changes are already integrated in the package both on CRAN and in the development version on GitHub. However, since the specification of such models can be very application-specific, in terms of special features which need to be accounted for due to the occurrence of the intermediate event, the datasets need to be appropriately prepared before their use with the functions of package **JMbayes**. The reader may refer to the online Supplementary Material Section S3, for a step by step tutorial on how to fit joint models with the occurrence of intermediate events and derive predictions thereafter.

Table 2.4: Estimated hazard ratios and 95% credibility intervals for the parameters of the joint models fitted to the SPRINT dataset. α_1 , α_2 and α_3 are measured in the units of 20 times systolic blood pressure (20mmHg) when referring to the current value association, in (10mmHg/time) when referring to the current slope association and in (20mmHg \times t) when referring to the area under the curve association.

	Value		Slope		Area	
	HR	95% CI	HR	95% CI	HR	95% CI
γ_1	0.91	(0.59; 0.859)	0.72	(0.59; 0.859)	0.81	(0.69; 0.97)
ζ	1.86	(1.592; 2.379)	1.93	(1.592; 2.379)	1.88	(1.567; 2.236)
α_1	1.34	(0.940; 1.310)	1.11	(0.940; 1.310)	1.07	(1.000; 1.143)

Table 2.5: Estimated hazard ratios and 95% credibility intervals for the parameters of the joint models fitted to the SPRINT dataset. α_1 , α_2 and α_3 are measured in the units of 20 times systolic blood pressure (20mmHg) when referring to the current value association, in (10mmHg/time) when referring to the current slope association and in (20mmHg \times t) when referring to the area under the curve association.

	Value + Slope		Value + Slope + Area		Value + Slope Interaction	
	HR	95% CI	HR	95% CI	HR	95% CI
γ_1	0.9	(0.743; 1.093)	0.9	(0.768; 1.054)	0.9	(0.737; 1.116)
ζ	1.89	(1.536; 2.294)	1.87	(1.649; 2.154)	1.58	(1.203; 2.065)
α_1	1.390	(1.166; 1.646)	1.32	(1.173; 1.471)	1.37	(1.118; 1.671)
α_2	1.100	(1.012; 1.206)	1.09	(1.049; 1.130)	1.05	(0.964; 1.158)
α_3	1.02	(0.985; 1.059)	1.84	(0.985; 2.571)		

Finally, all the analyses presented in Section 4, were performed using R version 3.5.1 and package **JMbayes**.

2.5 Simulation Study

2.5.1 Design

To evaluate the performance of the proposed models and to compare, in terms of predictive accuracy, the dynamic predictions that account for the whole biomarker trajectory against the cases where extrapolation or a simple time-dependent Cox model

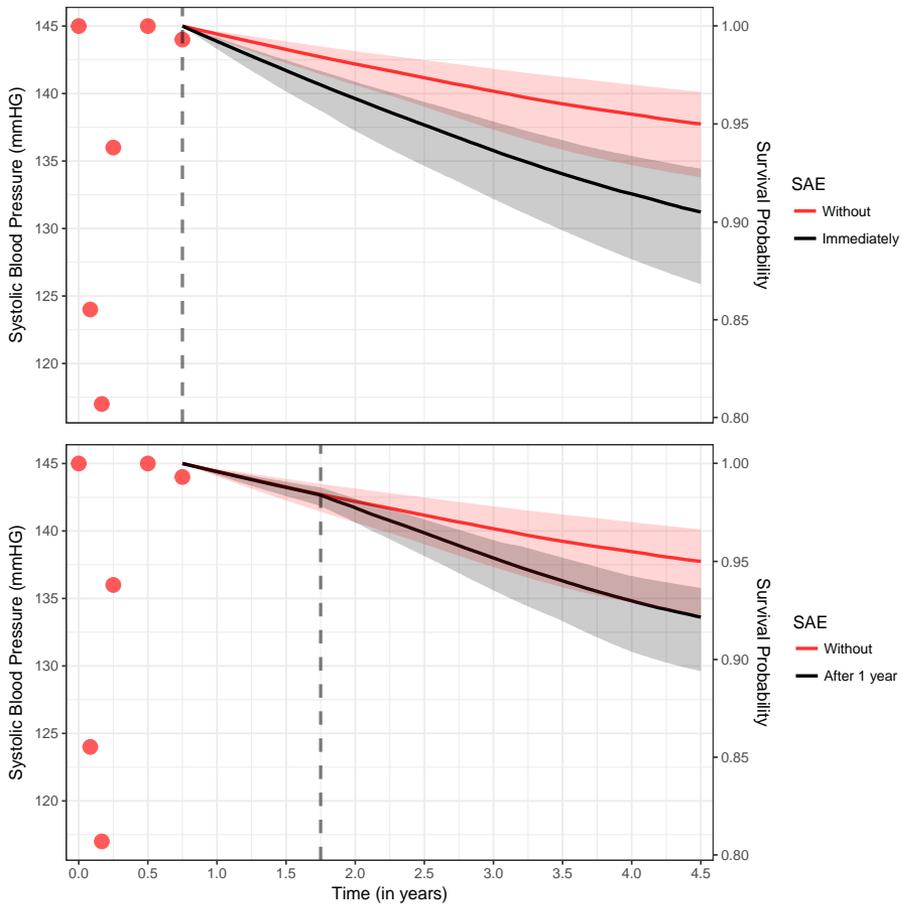


Figure 2.4: Survival Probabilities for a new subject under different scenarios with respect to the occurrence of serious adverse event (SAE). The vertical gray dashed line depicts the time of serious adverse event.

without accounting for the longitudinal data are assumed, we performed a simulation study. The main goal of the simulation study is to show the benefit in the accuracy of the individualized dynamic predictions when assuming that the intermediate event changes both the risk for the event of interest and the longitudinal trajectory against the case of assuming that the intermediate event only changes the risk for the event of interest while the longitudinal trajectory is extrapolated and the case where the longitudinal data are not taken into account. We assumed 2000 patients and then randomly selected follow-up visits. Each visit time t_{ij} was simulated from a uniform

distribution between 0 and 30. We assumed a total number of 20 measurements per subject. The final number of measurements, however, varies depending on when a subject experienced the clinical event or was censored. To mimic a realistic situation, the timing of the intermediate event was assumed to depend on the value of the biomarker trajectory. Specifically, if the biomarker exceeded a specific value then re-intervention took place at the next visit. For the cases that this value was not reached, the patient was assumed to never have experienced the intermediate event. For simplicity, we assumed a linear mixed-effects model and a survival submodel without any baseline covariates.

For the continuous longitudinal outcome, we simulated the data from a linear mixed-effects models similar to the model that we used for the pulmonary gradient dataset:

$$y_i(t) = \eta_i(t) + \epsilon_i(t) = (\beta_0 + b_{i0}) + (\beta_1 + b_{i1})t_i + (\tilde{\beta}_2 + \tilde{b}_{i2})R_i(t) + (\tilde{\beta}_3 + \tilde{b}_{i3})t_{i+} + \epsilon_i(t),$$

where $\epsilon_i(t) \sim \mathcal{N}(0, \sigma^2 I_{n_i})$ and $\mathbf{b}_i = (b_{i0}, b_{i1}, \tilde{b}_{i2}, \tilde{b}_{i3})^\top \sim \mathcal{N}(0, \mathbf{D})$. More specifically, we adopted a linear effect for time, a "drop" effect that occurs at the time of reoperation and an effect for the change in the slope from the time of reoperation onwards for both the fixed and the random part. Time t was simulated from a uniform distribution between 0 and 30. Based on this model for the continuous outcome we assumed three different scenarios:

- Scenario 1: $\beta_1 = 20.7$, $\beta_2 = 1.6$, $\tilde{\beta}_3 = -15.5$, $\tilde{\beta}_4 = -0.76$,
- Scenario 2: $\beta_1 = 20.7$, $\beta_2 = 1.6$, $\tilde{\beta}_3 = -15.5$, $\tilde{\beta}_4 = 0$,
- Scenario 3: $\beta_1 = 20.7$, $\beta_2 = 1.6$, $\tilde{\beta}_3 = 0$, $\tilde{\beta}_4 = -0.76$.

The assumed longitudinal trajectories for each of the three scenarios are depicted in Figure 2.5.

More specifically, in the first scenario, we assume that the longitudinal profile drops at the occurrence of the intermediate while the slope changes after its occurrence. In the second and third scenarios, the slope does not change after the occurrence of the intermediate event and the longitudinal profile does not drop respectively.

For the survival outcome we assumed a relative risk model of the form:

$$h_i(t) = h_0(t) \exp\{\gamma \mathbf{1} + R_i(t) \zeta + \alpha_1 \eta_i(t)\},$$

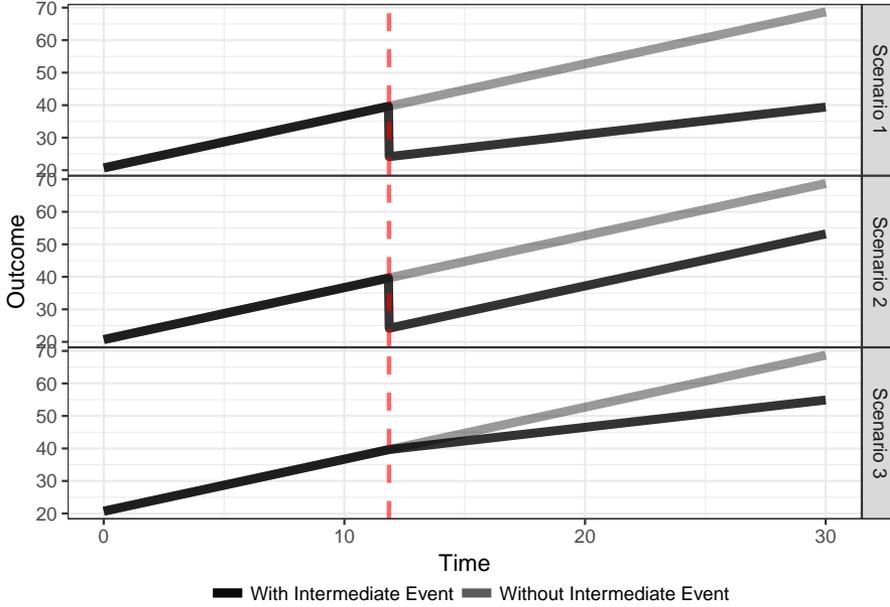


Figure 2.5: Assumed average longitudinal evolutions under the three simulation scenarios for subjects who experienced an intermediate event and for subjects who did not. The vertical red dashed line depicts the occurrence of the intermediate event.

where $\mathbf{1}$ is a vector of ones for the intercept term with a corresponding regression coefficient γ while the baseline risk was simulated from a Weibull distribution $h_0(t) = \xi t^{\xi-1}$ with $\xi = 20.4$. The censoring process was assumed to follow an exponential distribution with mean equal to 22.6. For the time-dependent Cox model, the following relative risk model was used instead:

$$h_i(t) = h_0(t) \exp\{\gamma \mathbf{1} + R_i(t) \zeta\},$$

where no association with the longitudinal outcome is assumed.

2.5.2 Results

Under the settings described in the previous Section, 500 datasets were simulated for each of the three scenarios. All the datasets were split in half to a training and test part with 1000 subjects each. For all the scenarios, to account for the whole trajectory of the biomarker, the joint model which consists of the submodels shown in Section 2.5.1 was fitted to the part of the simulated datasets which were kept for training. On the

other hand, for the extrapolation method the observations after reintervention were omitted from the analysis of the longitudinal outcome and the following mixed-effects model was fitted to the data up to reintervention time:

$$y_i(t) = \eta_i(t) + \epsilon_i(t) = (\beta_0 + b_{i0}) + (\beta_1 + b_{i1})t_i + \epsilon_i(t),$$

while for the survival process the same model was used. For the time-dependent Cox model, no longitudinal model was used and we only accounted for a change in the instantaneous hazard after the occurrence of the intermediate event as discussed in the previous section.

To assess the performance of the three approaches we used the models that were fitted on the training data to calculate the time-dependent AUCs and the prediction errors based on the test data. Both the time-dependent AUCs and the prediction errors were calculated at 3 different time-intervals starting at: $t = 20$, $t = 22$ and $t = 24$ respectively and assuming a clinically relevant time interval of two years $\Delta t = 2$. The time-intervals were selected on the basis of when the most events occur in the simulated data.

In Figures 2.6 and 2.7 we present the results of the simulation study depicted by boxplots. Specifically, the boxplots in each row represent different scenarios: non-zero effects, zero change in slope and zero "drop" at time of reintervention and in each column a different time-interval for prediction. In all the scenarios and time-intervals, both the AUC and PE are better when assuming that the intermediate event changes both the risk for the event of interest and the longitudinal trajectory. The simple time-dependent Cox model performs considerably worse than the other approaches. Moreover, there is a slight increase in the difference between the WT and Extrapolation methods for both predictive measures as the time-interval is set at later time-points. That is, the more information used the greater the difference between the two methods tends to become. Moreover, the relative performance of the two approaches does not differ between the three scenarios as well as for the different follow-up times. Therefore, the results support the argument that accounting for the changes in the longitudinal trajectories due to the occurrence of the intermediate event improve the predictive accuracy when compared to the approach that the longitudinal profile remains unaffected by its occurrence.

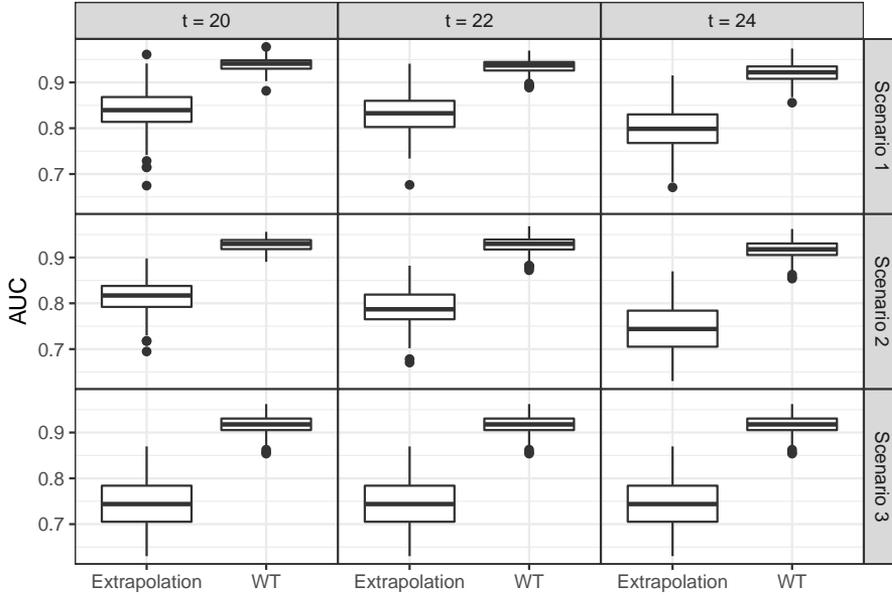


Figure 2.6: AUCs for the individualized dynamic predictions, evaluated using the testing part of the 500 datasets for two different joint models. 1) Extrapolation: Assuming that the longitudinal profile does not change after the occurrence of the intermediate event, 2) WT (Whole Trajectory): Assuming that the longitudinal profile changes after the occurrence of the intermediate event.

2.6 Discussion

Using the joint modeling framework we developed tools for deriving individualized dynamic predictions that are adaptive to different scenarios regarding intermediate events, such as treatment changes or the occurrence of adverse events. We proposed a range of joint models for longitudinal and time-to-event data which can accommodate special features due to the occurrence of intermediate events in both the longitudinal and survival submodels. That is, by incorporating features, such as the ones described in (2.1) and (2.2) a broad range of flexible joint models is sketched which accounts for the impact of an intermediate event by allowing for: 1) a direct effect of the intermediate event on the risk of the clinical endpoint through the time-varying binary covariate $R_i(t)$, 2) a direct effect of the intermediate event on the longitudinal trajectory through $g\{R_i(t), t_{i+}\}$ and 3) an indirect effect of the intermediate event on the the risk of the clinical endpoint through the association between the two outcomes

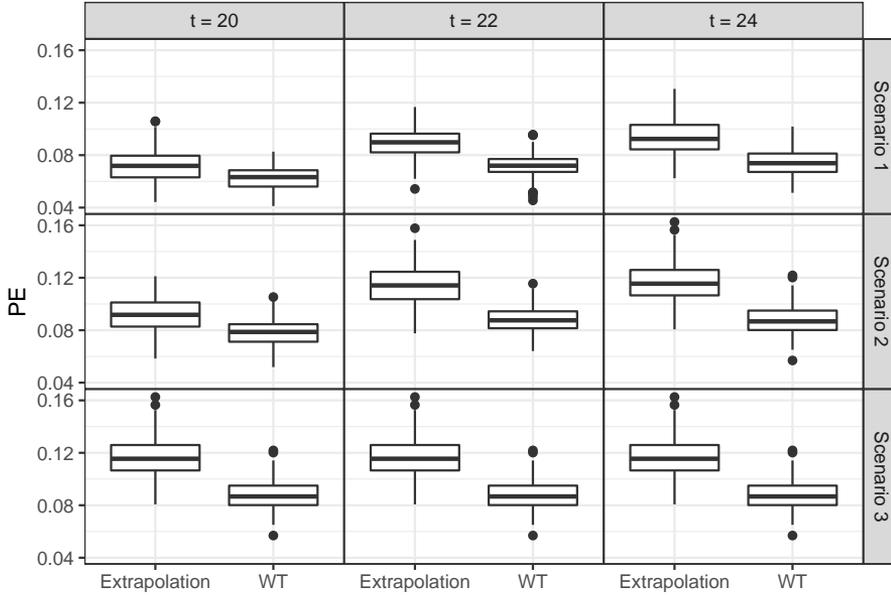


Figure 2.7: PEs for the individualized dynamic predictions, evaluated using the testing part of the 500 datasets for two different joint models. 1) Extrapolation: Assuming that the longitudinal profile does not change after the occurrence of the intermediate event, 2) WT (Whole Trajectory): Assuming that the longitudinal profile changes after the occurrence of the intermediate event.

which is defined by $f_{(t, \rho_i)}\{\mathcal{H}_i(t, \rho_i), \mathbf{b}_i\}$ and is allowed to differ before and after the intermediate event. All these features allow for great flexibility in the specification of the joint model which when utilized accordingly can lead to accurate predictions.

In the same line as recent observations with regard to dynamic predictions from joint models, we have seen that the accuracy of the predictions is influenced by intermediate events occurring during follow-up. Such events will need to be appropriately modeled as time-varying covariates in both the longitudinal and survival submodels. As illustrated in our simulation study, doing so, improves the predictive accuracy of the individualized dynamic predictions.

The focus of the applications presented in this paper, was to illustrate how joint models can be utilized to provide individualized dynamic predictions under different scenarios with respect to the occurrence of intermediate events. It should be noted, however, that in the analysis of the Pulmonary Gradient dataset, presented in Section 4.1, models M1, M2 and M3 assume that reoperation has a proportional effect on the

hazard at any time point. This is a strong assumption since clinically it would make sense to assume that reoperation increases the hazard shortly after its occurrence before its beneficial effect takes place. However, model diagnostics based on Schoenfeld residuals did not point to a violation of this assumption. Since the focus of this application was to illustrate the exploitation of joint models in deriving individualized dynamic predictions which are adaptive to different scenarios with respect to the occurrence of reoperation, we did not further explore the impact of this assumption. We do believe, however, that a more flexible model, such as a joint model that considers a multi-state survival process with reoperation as a potential state would allow for such assumptions to be incorporated which sets a potential direction for further research. Furthermore, it should also be noted that potential interaction effects between time and baseline characteristics such as age and sex, were not explored in the modelling of the pulmonary gradient for parsimony, but they could be added.

It is also essential to discuss to what extent the proposed models can be used to draw inference on potential outcomes following different scenarios on the future occurrence of intermediate events. It is, therefore, crucial to note that the focus of this paper was prognostic modelling and the development of a prediction tool that can quantify potential changes in the outcome under different scenarios concerning the occurrence of future intermediate events. Consequently, the adaptive individualized prediction tools we developed can be used to answer questions such as: "What is the expected change in the survival probability of a patient if he/she gets reoperated in a year from now given the information available on the patient so far?". Such questions should not be confused with inferential statements of causal nature such as: "A reoperation on this patient a year from now will cause his/her risk to change by this quantity". For such statements to be possible, a set of essential assumptions including positivity, consistency and exchangeability should be satisfied, similar to the assumptions that any statistical model must fulfil to be used for causal inference. An informative reference on the topic, specifically for the case of longitudinal data and time-varying treatments can be found in Hernán and Robins (2019) (Chapters 19-21).

Another interesting point of discussion for such applications is whether the proposed models are susceptible to time-dependent confounding. Indeed, in the framework of a randomised clinical trial, the target treatment effect would no longer be protected if a specific selection of patients (e.g. severe cases) experienced the intermediate event post-randomization. This complicates the interpretation of the treatment effect coefficient. Therefore, it should be noted that in the applications presented, in this paper, we worked under the assumption that the intermediate event depends only on previous measurements of the marker and does not carry any further informa-

tion. Under this assumption, including the intermediate event in the specification of both the mixed-effect sub-model and the relative risk sub-model, is sufficient and the process that generates the intermediate event does not have to be explicitly modeled.

The joint model formulation we presented allows to utilize the quantification of the effects the intermediate event imposes on the risk for the clinical endpoint of interest. As such, it can be utilized to derive individualized dynamic predictions for new subjects who did not experience the intermediate event and quantify how its occurrence at any future time point will influence their risk predictions. Such a predictive tool can provide valuable information to the physicians and assist in their decision making process for potential treatment changes. Based on such predictions further prognostic tools can potentially be developed. For example in settings where the timing of a future treatment is important, having both benefits and disadvantages when applied either too late or too early, such dynamic predictions that are adaptive to the timing of the intermediate event can become the basis for methodology that can be used to predict the optimal time for the future treatment. Unfortunately, the applications at hand did not allow for exploring such a possibility, but this is a clear direction for future research. Moreover, in our paper we only consider the joint analysis of one longitudinal and one survival outcome. While the extension of the proposed models to their multivariate counterparts is straightforward, such multivariate joint models have not been explored in the literature in the context of intermediate events that may occur during follow-up and alter the course of the disease for the patient. Therefore, individualized dynamic predictions based on even more complex joint models, such as with multiple longitudinal biomarkers or with multi-state processes instead of a single time-to-event outcome might lead to improved accuracy depending on the application.

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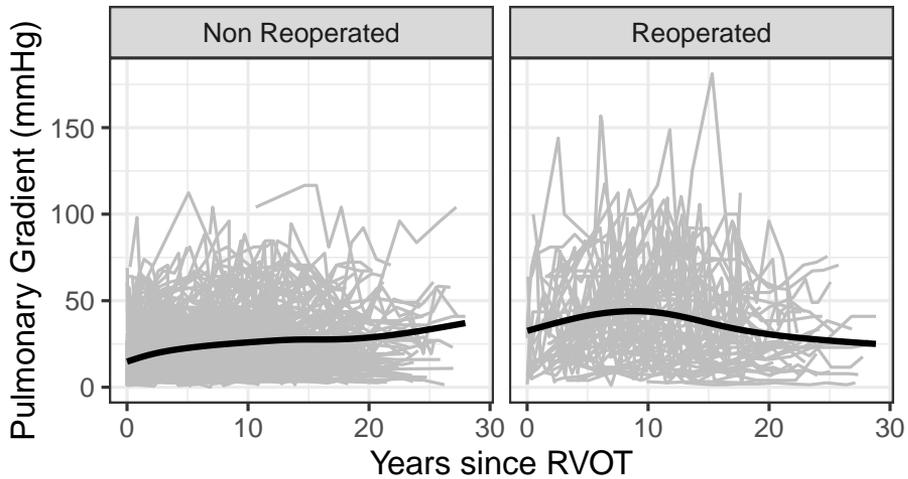


Figure 2.8: Individual trajectories of observed pulmonary gradient values over time for non reoperated subjects (left panel) and reoperated subjects (right panel) along with a smooth curve (red line).

Appendix

2.A Data Description

2.A.1 Pulmonary Gradient Data

Table 2.6: Data description: Continuous variables are presented as median (IQR), categorical variables as counts (frequencies %).

	All	Non reoperated	Reoperated
Number of subjects	467	402 (86.9%)	65 (13.1%)
Number of repeated measurements	8 (5 - 12)	7 (4 - 11)	14 (11 - 16)
Number of Events	34 (7.3%)	32 (8.0%)	2 (3.0 %)
Sex = Male	272 (58.2%)	229 (57.0%)	43 (66.1 %)
Age	20.3 (9.5 - 30.9)	21.5 (9.4 - 31.2)	16 (10.9 - 22.4)

Table 2.7: Data description: Continuous variables are presented as median (IQR), categorical variables as counts (frequencies %).

	All	No SAE	SAE
Number of subjects	9068	5644 (62.2%)	3424 (37.8%)
Number of repeated measurements	15 (13 - 17)	15 (13 - 17)	14 (12 - 17)
Number of Events	535 (5.9%)	20 (0.3%)	515 (15.0 %)
Treatment = Intensive	4552 (50.2%)	2804 (49.7%)	1748 (51.0%)

2.A.2 SPRINT Data

2.B Predictive performance comparison between extrapolation method and joint models with intermediate events in the SPRINT data

To illustrate the use of the predictive performance measures presented in Section 3, we hereby present a comparison in terms of the time-dependent area under the receiver operating characteristic curve (AUC) and the expected prediction error (PE) for the SPRINT data.

More specifically, we are interested to compare the joint model used for the analysis of the SPRINT data which postulates effects of both the current value and current slope of the systolic blood pressure trajectory on the instantaneous risk of the composite endpoint (as presented in Section 4.2) against the corresponding model that ignores the longitudinal data after the occurrence of the serious adverse event (Extrapolation method). Specifically, for the extrapolation method the following model was used for the evolution of the systolic blood pressure:

$$SBP_i(t) = (\beta_0 + b_{i0}) + \left(\sum_{k=0}^3 (\beta_{(k+1)} + b_{i(k+1)}) B_k(t, \mathbf{k}) \right) + \beta_5 \text{Treatment}_i + \left(\sum_{k=0}^3 \beta_{(k+6)} B_k(t, \mathbf{k}) \right) \times \text{Treatment}_i + \epsilon_i(t),$$

while for the instantaneous risk the same model was used for both methods.

To compare the two approaches, we randomly split the data in half to a training and test part. Then we fitted the models to the training part and evaluated the AUC and PE for both models using the test part. The evaluation was done at 6 time-intervals:

$t = 2.5$, $t = 2.75$, $t = 3$, $t = 3.25$, $t = 3.5$, and $t = 3.75$ assuming a clinically relevant time interval of a quarter of a year $\Delta t = 0.25$.

The results are shown in table 2.8. In the specific application the two approaches are virtually similar. This can be explained by the fact that the occurrence of a serious adverse event did not have a strong effect on the evolution of systolic blood pressure. However, even in this case both approaches achieve similar performance in terms of predictive accuracy.

Table 2.8: Evaluation of Predictive Performance between WT and Extrapolation Methods for the SPRINT data

t	WT		Extrapolation	
	AUC	PE	AUC	PE
2.50	0.66088	0.00362	0.65809	0.00363
2.75	0.79924	0.00417	0.79290	0.00418
3.00	0.54684	0.00606	0.56923	0.00607
3.25	0.42924	0.00368	0.46713	0.00369
3.50	0.62177	0.00421	0.63544	0.00423
3.75	0.68023	0.00570	0.66712	0.00571

2.C Sample R Code

In this section we provide a sample **R** code for fitting the joint models proposed in the paper and then utilizing them to derive predictions under different scenarios for the occurrence of intermediate events. As an illustrative example we use one of the 500 datasets generated for the simulation study, presented in the paper, under scenario 1. Under this scenario we assume that the trajectory of the longitudinal outcome immediately changes (drops) at the occurrence of the intermediate event while the rate of increase (slope) also changes after the occurrence of the intermediate event, implying two special features of the longitudinal outcome that need to be considered.

To start with the code, the **R** package **JMbayes** needs to be installed and loaded.

```
# For the remainder the R symbol 'dat' will be used to refer to the dataset
# Replace NAs for Interm.Evnt.Time with 1e+6
dat$Interm.Evnt.Time <- ifelse(is.na(dat$Interm.Evnt.Time),
                              1e+5, dat$Interm.Evnt.Time)
```

Here we chose a large unrealistic value of 100000 years that is impossible to occur in reality. Table 2.9 shows how the data for the 2nd subject changed.

Table 2.9: Example Dataset

ID	time	Y	Interm.Evnt.Time	Tstart	Tstop	Event
1	0.000	22.043	12.846	0.000	1.179	0
1	1.179	20.319	12.846	1.179	4.793	0
1	4.793	23.387	12.846	4.793	8.202	0
1	8.202	26.034	12.846	8.202	9.105	0
1	9.105	24.857	12.846	9.105	12.846	0
1	12.846	27.046	12.846	12.846	16.821	0
1	16.821	17.251	12.846	16.821	17.200	0
1	17.200	18.261	12.846	17.200	17.223	0
1	17.223	19.069	12.846	17.223	18.753	0
2	0.000	23.424	100000.000	0.000	2.401	0
2	2.401	24.342	100000.000	2.401	4.210	0
2	4.210	26.170	100000.000	4.210	4.451	0
2	4.451	25.781	100000.000	4.451	6.419	0
2	6.419	29.663	100000.000	6.419	7.265	1

Now we can proceed to compute and include in the dataset the time-varying covariates of interest: $R_{(t)}$ and t_{i+} which correspond to the intermediate event indicator and the time relative to the occurrence of the intermediate event, respectively. To do so in **R** we run the following code:

```
# Compute the intermediate event indicator
dat$Int.Evnt.Index <- as.numeric(dat$time >= dat$Interm.Evnt.Time)
# Compute Time relative to the intermediate event
dat$time.relative <- pmax(0, dat$time - dat$Interm.Evnt.Time)
```

Table 2.10 shows the updated data on the subset of the data that includes the two subjects we use in the example. We see that the two time-varying covariates are now included in the dataset. For subject 1, for all the time points following the occurrence of the intermediate event, the two time-varying covariates change accordingly whereas for subject 2 they are zero since the occurrence of the intermediate event was not observed during follow-up.

Table 2.10: Example Dataset

ID	time	Y	Interm.Evnt.Time	Tstart	Tstop	Event	Int.Evnt.Index	time.relative
1	0.000	22.043	12.846	0.000	1.179	0	0	0.000
1	1.179	20.319	12.846	1.179	4.793	0	0	0.000
1	4.793	23.387	12.846	4.793	8.202	0	0	0.000
1	8.202	26.034	12.846	8.202	9.105	0	0	0.000
1	9.105	24.857	12.846	9.105	12.846	0	0	0.000
1	12.846	27.046	12.846	12.846	16.821	0	1	0.000
1	16.821	17.251	12.846	16.821	17.200	0	1	3.975
1	17.200	18.261	12.846	17.200	17.223	0	1	4.354
1	17.223	19.069	12.846	17.223	18.753	0	1	4.377
2	0.000	23.424	100000.000	0.000	2.401	0	0	0.000
2	2.401	24.342	100000.000	2.401	4.210	0	0	0.000
2	4.210	26.170	100000.000	4.210	4.451	0	0	0.000
2	4.451	25.781	100000.000	4.451	6.419	0	0	0.000
2	6.419	29.663	100000.000	6.419	7.265	1	0	0.000

Now that the data are ready, we can proceed to fitting the joint model. This is no different than fitting any other joint model with package **JMbayes** apart from including in the model specification the newly introduced time-varying covariates. Hence we first fit separately the Cox relative risk and mixed-effects submodels and then we pass the corresponding objects to function `jointModelBayes()` to obtain the final joint model fit:

```
# Fit time-dependent Cox model
cox.fit <- coxph(Surv(Tstart, Tstop, Event) ~ Int.Evnt.Index + cluster(ID),
  data = dat)
# Fit the mixed-effects model
mix.fit <- lme(Y ~ time + Int.Evnt.Index + time.relative,
  random = ~ time + Int.Evnt.Index + time.relative | ID,
  data = dat)
# Fit the Joint model
joint.fit <- jointModelBayes(mix.fit, cox.fit, timeVar = "time")
```

After obtaining the joint model fit, we can proceed in deriving dynamic predictions under different scenarios for the occurrence of the intermediate event for new subjects. In Table 2.11 the data for a new subject which has not experienced the intermediate event are shown.

Table 2.11: Example Dataset

ID	time	Y	Interm.Evnt.Time	Int.Evnt.Index	time.relative
New	0.5548873	15.86804	NA	NA	NA
New	1.3547850	26.81457	NA	NA	NA
New	2.1550550	13.02823	NA	NA	NA
New	6.5422016	29.46144	NA	NA	NA
New	7.5409739	23.48326	NA	NA	NA

For the code illustration this data are assumed to be included in a `data.frame` called `newdata`. Since this subject has not experienced the intermediate event, all the relevant information regarding the occurrence of the intermediate event are shown as missing observations. Again in order to derive predictions under different scenarios regarding the occurrence of the intermediate event we need to manipulate the data accordingly. We will illustrate how the data need to be changed for investigating three different scenarios regarding the occurrence of the intermediate event:

1. No occurrence of the intermediate event,
2. immediate occurrence of the intermediate event,
3. occurrence of the intermediate event after 1 year.

For the first case (no occurrence of the intermediate event) we will use the same trick as before. That is we will specify the time of the intermediate event as an arbitrarily large number and then calculate the intermediate event indicator and time relative to the occurrence of the intermediate event accordingly.

```
# Create a copy of newdata and call it newdata 1
newdata1 <- newdata
# Specify arbitrarily large number for Interm.Evnt.Time
newdata1$Interm.Evnt.Time <- 1e+05
# Compute Int.Evnt.Index and time.relative
newdata1$Int.Evnt.Index <- as.numeric(newdata$time >= newdata$Interm.Evnt.Time)
newdata1$time.relative <- pmax(0, newdata$time - newdata$Interm.Evnt.Time)
```

The changes in `newdata1` are shown in Table 2.12.

Table 2.12: Example Dataset

ID	time	Y	Interm.Evnt.Time	Int.Evnt.Index	time.relative
New	0.5548873	15.86804	1e+05	0	0
New	1.3547850	26.81457	1e+05	0	0
New	2.1550550	13.02823	1e+05	0	0
New	6.5422016	29.46144	1e+05	0	0
New	7.5409739	23.48326	1e+05	0	0

In a similar manner we create datasets `newdata2` and `newdata3` for scenarios 2 and 3 respectively. The only notable difference here, is that we add a new row in the dataset for which we only specify the covariates associated with time and the intermediate event accordingly but we specify the longitudinal outcome as missing for the specific row, since no data are available.

```
# DATA FOR SCENARIO 2
# create copy of newdata1 and call it newdata2
newdata2 <- newdata1
# Specify the time of the intermediate event to be equal
# to the last observed time point plus
# an arbitrarily small value
newdata2$Interm.Evnt.Time <- newdata2$time[nrow(newdata2)] + 0.00001
# create additional row
new.row <- newdata2[nrow(newdata2), ]
new.row$time <- newdata2$Interm.Evnt.Time[1]
new.row$Y <- NA
# attach new row to the dataset
newdata2 <- rbind(newdata2, new.row)
# compute time-varying covariates
newdata2$Int.Evnt.Index <- as.numeric(newdata2$time >= newdata2$Interm.Evnt.Time)
newdata2$time.relative <- pmax(0, newdata2$time - newdata2$Interm.Evnt.Time)

# DATA FOR SCENARIO 3
# create copy of newdata1 and call it newdata3
newdata3 <- newdata1
# Specify the time of the intermediate event to be equal
# to the last observed time point
# plus 1
newdata3$Interm.Evnt.Time <- newdata3$time[nrow(newdata3)] + 1
# create additional row
new.row <- newdata3[nrow(newdata3), ]
new.row$time <- newdata3$Interm.Evnt.Time[1]
```

2. INDIVIDUALIZED DYNAMIC PREDICTION OF SURVIVAL WITH THE PRESENCE OF INTERMEDIATE EVENTS

```
new.row$Y <- NA
# attach new row to the dataset
newdata3 <- rbind(newdata3, new.row)
# compute time-varying covariates
newdata3$Int.Evnt.Index <- as.numeric(newdata3$time >= newdata3$Interm.Evnt.Time)
newdata3$time.relative <- pmax(0, newdata3$time - newdata3$Interm.Evnt.Time)
```

The changes in `newdata2` and `newdata3` are shown in Tables 2.13–2.14, respectively. Finally, the predictions under the different scenarios can be obtained by applying function `survfitJM()` to the fitted models and datasets we just created:

```
# Predictions for scenario 1
preds.1 <- survfitJM(object = joint.fit, newdata = newdata1, idVar = "ID")
# Predictions for scenario 2
preds.2 <- survfitJM(object = joint.fit, newdata = newdata2, idVar = "ID")
# Predictions for scenario 3
preds.3 <- survfitJM(object = joint.fit, newdata = newdata3, idVar = "ID")
```

Table 2.13: Example Dataset

ID	time	Y	Interm.Evnt.Time	Int.Evnt.Index	time.relative
New	0.5548873	15.86804	7.540984	0	0
New	1.3547850	26.81457	7.540984	0	0
New	2.1550550	13.02823	7.540984	0	0
New	6.5422016	29.46144	7.540984	0	0
New	7.5409739	23.48326	7.540984	0	0
New	7.5409839	NA	7.540984	1	0

2.D Data Availability Statement

The data used for the Pulmonary Gradient analysis are available on request from the corresponding author. The data are not publicly available due to privacy or ethical restrictions. The data used for the SPRINT trial are available from BioLINCC.

Table 2.14: Example Dataset

ID	time	Y	Interm.Evnt.Time	Int.Evnt.Index	time.relative
New	0.5548873	15.86804	8.540974	0	0
New	1.3547850	26.81457	8.540974	0	0
New	2.1550550	13.02823	8.540974	0	0
New	6.5422016	29.46144	8.540974	0	0
New	7.5409739	23.48326	8.540974	0	0
New	8.5409739	NA	8.540974	1	0

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**Influence of pregnancy on long-term durability of allografts in
right ventricular outflow tract**

This chapter is based on:

Romeo, J.L.R.* , Papageorgiou, G* , Takkenberg, J.J.M., Roos-Hesselink, J.W., van Leeuwen W.J., Cornette J.M.J., Rizopoulos, D., Bogers A.J.J.C. and Mokhles, M.M. (2020), Influence of pregnancy on long-term durability of allografts in right ventricular outflow tract *The Journal of Thoracic and Cardiovascular Surgery*, 159: 1508–1516.E1. doi: <https://doi.org/10.1016/j.jtcvs.2019.08.083>

* both authors contributed equally

Abstract

Background

There is very limited published evidence about the influence of pregnancy on allograft durability in right ventricular outflow tract (RVOT) position. We present the first study using mixed and joint modeling.

Methods

This retrospective study compared clinical and valve related outcomes of all consecutive female hospital survivors in their fertile life phase (18–50 years) based on pregnancy. Serial echocardiographic measurements of pulmonary gradient and regurgitation were analyzed for their association with valve replacement using joint models for longitudinal and time-to-event data. Occurrence of first pregnancy was included as a time-dependent intermediate event in both the longitudinal and survival analyses of the joint model in order to assess its impact on the hemodynamic and clinical outcome.

Results

In total, 196 consecutive women in their fertile life-phase with an allograft were included. Complete information of 176 (90%) allografts in 165 women was available including 1395 echocardiograms. Of these women, 51 (30.9%) women had 84 completed pregnancies at an average age of 29.1 ± 3.9 (SD) years; 8.1 ± 6.1 years since allograft implantation. Tetralogy of Fallot was the most common diagnosis in both groups. After a mean follow up of 15.2 years (range 0.1–30), 7 (13.7%) parous underwent valve replacement, versus 20 (17.5%) nulliparous. During this follow up, the mean allograft gradient in parous (24.2 mmHg) and nulliparous (21.0 mmHg) was comparable ($p=.225$). One mmHg increase in pulmonary gradient increased the instantaneous risk of pulmonary valve replacement (PVR) by a ratio of 1.051 ($p<.001$), regardless of pregnancy. Similarly, development of moderate or severe regurgitation increased the risk of PVR ($p=.038$), regardless of pregnancy. Pregnancy was not associated with a change in the allograft gradient ($p=.258$), regurgitation grade ($p=.774$) or hazard of PVR ($p=.796$) during follow-up.

Conclusions

Pregnancy is not associated with impaired allograft durability in women with good cardiac health.

3.1 Introduction

Congenital heart disease (CHD) is present in 8-10 per 10.000 live births and often predisposes towards increased morbidity and earlier mortality, compared to the normal population (van der Bom et al., 2012; Gilboa et al., 2016; O’Leary et al., 2016; Hoffman and Kaplan, 2002) [1-4]. The prevalence of CHD in young adulthood is expected to increase due to constantly improving surgical and clinical treatment options enabling patients to reach their fertile life phase (van der Bom et al., 2012; Gilboa et al., 2016; van der Linde et al., 2011)[1, 2, 5]. In this regard, clinicians are confronted with a growing population of adults with congenital heart disease (ACHD). Approximately 20% of all CHD involves the right ventricular outflow tract (RVOT). Pulmonary valve replacement (PVR) has, therefore, become the most frequently performed procedure in ACHD comprising approximately 10% of all procedures (T.S.o.T.S., 2017)[6]. Suitable valve alternatives for RVOT reconstruction, however, are still scarce. The allograft is generally preferred over biological or mechanical prostheses for its excellent hemodynamic capabilities, durability and independence from anticoagulation which could be especially beneficial for childbearing women (Mokhles et al., 2011; Wong et al., 1993; Steinberg et al., 2017; van Hagen et al., 2015)[7-10]. Structural valve deterioration (SVD) remains the main caveat of the allograft however, ultimately indicating repeated valve intervention (Romeo et al., 2018b)[11]. As pregnancy induces hormonal changes and an important hemodynamic burden by increasing circulating volume, heart rate and bloodpressure (Stout and Otto, 2007; Basquin et al., 2010)[12, 13] it could potentially affect allograft durability. During the life long care and follow up of female ACHD, the wish and possibilities of pregnancy along with potential risks and long term outcome must be considered and actively addressed; ideally prior to pregnancy (Stout, 2005)[14]. This information could also be used in pregnancy heart team meetings on women considering pregnancy and requiring valve surgery, as recommended by the most recent guidelines (Class 1 recommendation) (Regitz-Zagrosek et al., 2018)[15]. This is the first report about the influence of pregnancy on long term function and durability of allograft conduits in RVOT position in women of childbearing age, using repeated measurement analysis.

3.2 Methods

3.2.1 Study design

All consecutive patients who underwent RVOT reconstruction between April 1986 and January 2018 with an allograft at the Cardio-Thoracic Surgery department of the

Erasmus Medical Center were included and screened for pregnancies. The Erasmus Medical Center is a tertiary referral center specialized in (congenital) cardiac surgery. All female patients older than 18 years at the time of this study and younger than 50 years at moment of surgery were retrospectively included. A detailed questionnaire was sent out to all women who confirmed pregnancy and gave informed consent. A supplementary telephone interview was conducted for additional information. The Medical Ethics Commission reviewed and approved this study (MEC 17-158) after which written informed consent was acquired prior to onset of this study.

3.2.2 Operation technique

Allograft implantation was performed with standard cardiopulmonary bypass with moderate- or normothermia on a beating heart after median sternotomy. In case of concomitant intracardiac procedures the aorta was cross-clamped after which myocardial protection was achieved with crystalloid cardioplegia (St. Thomas' solution). Allografts were interposed between the right ventricle and pulmonary artery with running polypropylene 5.0 sutures. Our center exclusively uses cryopreserved allografts for RVOT reconstruction, preferring pulmonary allografts over aortic ones. Our institutional policy does not indicate any anticoagulation for homografts postoperatively after adequate mobilization.

3.2.3 Definitions

For this study, pregnancies were considered when reaching beyond >20 weeks of gestation. Parous and nulliparous women were thus defined as respectively having or having not experienced a pregnancy and delivery beyond 20 weeks of gestation. Gestational age was based on first trimester ultrasound and last menstrual period. After pulmonary valve replacement, follow up by a cardiologist was regularly performed in all women during outpatient visits after one and six months and annually thereafter. Cardiac and valve related outcomes were reported according to the guidelines for reporting mortality and morbidity after cardiac valvular interventions (Akins et al., 2008)[16]. All interventions were discussed during weekly multidisciplinary meetings involving (congenital) cardiologist, cardiac surgeons and radiologists. The primary endpoint of this study was pulmonary valve replacement (PVR) either surgically or percutaneously.

3.2.4 Echocardiographic

Allograft function was repeatedly assessed using standardized transthoracic echocardiograms during outpatient visits. Peak pulmonary gradient (mmHg) and regurgita-

tion grade were assessed from a multi-window perspective according to the guidelines for the assessment of valve stenosis and regurgitation (Baumgartner et al., 2009; Lancellotti et al., 2010; Cleuziou et al., 2015)[17-19]. Peak pulmonary gradient was calculated with the modified Bernoulli equation from the peak transvalvular speed (m/s) and pulmonary regurgitation was graded qualitatively as non-significant (i.e. no regurgitation, trace or mild) or significant (moderate or severe).

3.2.5 Statistics

Baseline characteristics and measurements are summarized using descriptive statistics. Continuous measurements are summarized using means \pm standard deviations or medians with range. Qualitative measurements are summarized as absolute counts with percentages. All statistical tests were two-sided with a p-value lower than 0.05 considered as significant. Kaplan-Meier plots were used to describe cumulative freedom from valve replacement and mortality. Serial echocardiographic measurements of pulmonary gradient and regurgitation were analyzed using a bivariate non-linear mixed-effects model, with a linear mixed-effects regression sub-model for the pulmonary gradient, and a mixed-effects logistic regression sub-model for pulmonary regurgitation. Both longitudinal sub-models were adjusted for the effects of age, donor sex, allograft diameter and type of allograft (i.e. aortic or pulmonary). The effect of pregnancy was determined by including a nonlinear effect of time using natural cubic splines from the onset of pregnancy in the sub-models of both pulmonary gradient and regurgitation grade. For the random effects structure we used a nonlinear effect of time as well as a nonlinear effect of time from the onset of pregnancy using natural cubic splines. A time-dependent Cox model was used for the instantaneous risk of valve replacement. The value of both the pulmonary gradient and regurgitation, as estimated by the joint mixed-effects model, were included in the Cox model in order to determine their association with the instantaneous risk for valve replacement. The occurrence of a first pregnancy was entered in the model as a binary time-varying variate. Furthermore, interaction terms between the current value of the longitudinal trajectories of pulmonary gradient and regurgitation were included to investigate potential changes in the magnitude of the association between the hemodynamic outcomes and the instantaneous risk for valve replacement due to the occurrence of first pregnancy. The effect pregnancy on allograft function over time was thus assessed in three manners: 1. The effect of pregnancy on the longitudinal evolution of pulmonary gradient and regurgitation grade. 2. The effect of pregnancy as an independent covariate in a conventional proportional hazards model. 3. The interaction effect of pregnancy and the evolutions of both pulmonary gradient and the regurgitation grade in the joint model. I.e. does the occurrence of pregnancy alter the relationship between

both markers and PVR? Statistical analyses were performed with SPSS (IBM Corp. Released 2012. IBM SPSS Statistics for Windows, Version 24.0. Armonk, NY: IBM Corp.) and R (R Core Team (2018). R: A language and environment for statistical computing. R Foundation for Statistical Computing, Vienna, Austria. URL <https://www.R-project.org/>).

3.3 Results

During the study period, 280 consecutive female patients underwent allograft implantation. Overall hospital mortality was 3.2% (n=9). We excluded 11 (3.9%) patients who were over 50 years at the time of surgery, 48 (17.4%) patients who had not reached 18 years and 16 (5.7%) patients who were lost to follow up due to return to their country of origin immediately post-surgery. Of the 196 allografts eligible for inclusion, 176 (90%) had complete clinical and echocardiographic follow-up (Table 1). None of the patients who underwent repeated PVR had multiple pregnancies during the follow-up time of different allografts. Compared to nulliparous women, parous women had less often right ventricular hypertrophy (12% vs 26%, $p=.046$) at time of surgery. Other baseline characteristics were comparable (Table 3.1).

3.3.1 Pregnancy outcome

The cardiac and obstetric course and fetal outcomes of all pregnancies have been extensively described previously (Romeo et al., 2018a)[20]. In short, parous women were in overall good cardiac and clinical health prior to pregnancy with an average pulmonary gradient of 19 mmHg, non-significant regurgitation in 83.3% and significant regurgitation in 16.7%. Mean age at last menstruation was 29.6 ± 4.3 years, which was 8.6 ± 6.6 years after allograft implantation. Two women were identified who became pregnant despite explicit contraindications on cardiac grounds. The first had a severely dilated and dysfunctioning left ventricle and the second had severe pulmonary hypertension. They were induced into premature labor but recovered uneventfully. Both still have their homograft in situ without signs of valve deterioration. No woman died during pregnancy or within the first year postpartum.

3.3.2 Long term clinical outcome

Median follow-up length from operation to last follow-up was 18.0 years (mean 17.4 years; range 2.0-30.0 years, total patient-years 887) and 13.7 years (mean 14.3 years; range 0.01-28.6 years, total patient-years 1784) for parous and nulliparous women,

Table 3.1: Perioperative characteristics of 176 female allograft recipients

	Total	Nulliparous	Parous	P-value
Allografts n(%)	176	125 (71)	51 (29)	
Aortic allograft	18 (10)	16 (13)	2 (4)	.078
Pulmonary allograft	158 (90)	109 (87)	49 (96)	
Pregnancies n (%)		0	84	NA
1			26	
2			20	
≥ 3			5	
Age at valve replacement (years)	22.2± 12.5	22.7± 14.1	21.4± 7.3	.467
Age at first pregnancy (years)		NA	29.1± 3.9	NA
Time of pregnancy since PVR (years)		NA	8.1± 6.1	NA
Height at valve replacement (m)	151±31	147±34	159±17	0.16
Weight at valve replacement (kg)	56±18	56 ±19	56±15	.925
Creatinine	59±18	58±19	61±15	.341
Right ventricular hypertrophy n(%)	38 (22)	32 (26)	6 (12)	.046
Left ventricular hypertrophy n(%)	27 (15)	22 (18)	5 (10)	.251
Diagnosis n(%)				
TOF	72 (41)	49 (39)	23 (45)	.235
Aortic Pathology*	42 (24)	27 (22)	15 (29)	
PA + VSD	19 (11)	16 (13)	3 (6)	
TA	12 (7)	11 (9)	1 (2)	
TGA + PA/PS	5 (3)	4 (3)	1 (2)	
PA-VSD	5 (3)	3 (2)	2 (4)	
Discordant	5 (3)	5 (4)	0 (0)	
Tricuspid Atresia	1 (1)	0 (0)	1 (2)	
Other	15 (9)	10 (8)	5 (10)	
Donor sex (male) n (%)	89 (51)	65 (52)	24 (47)	.619
Allograft size (mm)	23 (11 - 30)	23 (11 - 30)	24 (16 - 28)	.206
Perfusion time (min) (n = 161)	145 (35-465)	143 (35-465)	151 (39-295)	.691
Pulmonary valve replacement	27	20 (16)	7 (14)	.332
Severe stenosis	14	12 (60)	2 (29)	
Severe regurgitation	6	4 (20)	2 (29)	
Mixed stenosis and regurgitation	7	4 (20)	3 (43)	

NYHA: New York Heart Association, PA: Pulmonary Atresia, PS: Pulmonary Stenosis, TA: Truncus Arteriosus, TGA: Transposition of the Great Arteries, TOF: Tetralogy of Fallot, VSD: Ventricular Septal Defect.

*Primary aortic valve pathology for which a pulmonary autograft ('Ross') procedure was performed

respectively. Thirteen women died during follow up (0.73%/patient-year), all nulliparous, with 10 (0.56%/patient-year) cases of cardiac death and 3 cases (0.17%/patient-year) of non-cardiac related death. Among the cardiac related deaths there was 1 (0.06%/patient-year) case of valve related death, 4 (0.22%/patient-year) cases of sudden unexplained death and 5 (0.28%/patient-year) cases of non-valve related cardiac death all comprising end-stage heart failure. One nulliparous woman died during an attempt to percutaneously implant a Melody valve indicated by severe stenosis 23.0 years after initial allograft implantation. All other reinterventions were performed successfully. Following allograft implantation, there were 4 (3.2%) percutaneous balloon dilatation in the nulliparous, and 2 (3.9%) in the parous women. In the parous group there were 7 (0.8%/patient-year) PVR after 14.3 ± 4.9 years after initial surgery. Six were surgically (4 allografts, 1 mechanical valve, 1 bioprosthesis (Medtronic Freestyle® valve)) and 1 was percutaneously (Melody® valve). Among the nulliparous 20 (1.24%/patient-year) underwent PVR after 14.1 ± 5.5 years of which 13 surgically (all allografts) and 7 transcatheter Melody® valve implantations. All PVR were indicated by structural valve deterioration. Freedom from valve replacement after 20 years was $78 \pm 16\%$ for parous and $66 \pm 14\%$ for nulliparous women (Figures 3.1 and 3.2).

3.3.3 Echocardiographic outcome

There were 1395 serial echocardiograms available for all included patients (mean 7, range 1-26) serial echocardiograms/patient). For women with multiple pregnancies, only the effect of the first pregnancy on the allograft hemodynamics were analyzed. Measurements in those cases were censored from the onset of the second pregnancy. The median time for women to have their first pregnancy after allograft implantation was 8 years. Figure 3.3 present the longitudinal evolutions of pulmonary gradient and regurgitation for scenarios with and without pregnancy. Figure 3.4 present both longitudinal evolutions along with the influence of pregnancy on the hazard of PVR.

The analyses of the association between both gradient and regurgitation, and the hazard of PVR showed that an 1 mmHg increase in the pulmonary gradient, increases the instantaneous risk of PVR by a ratio of 1.051 ($p < .001$). Similarly, an increase in the probability of significant regurgitation increases the instantaneous risk of PVR by a ratio of 1.209 ($p = 0.038$). Pregnancy was, however, not associated with an increased hazard of PVR ($p = 0.796$, Table 3.2). The interaction between the longitudinal pulmonary gradient and regurgitation grade with pregnancy was non-significant ($p = 0.258$ and $p = 0.774$, respectively), indicating that pregnancy did not change the association between the hemodynamic outcomes and the hazard of valve replacement.

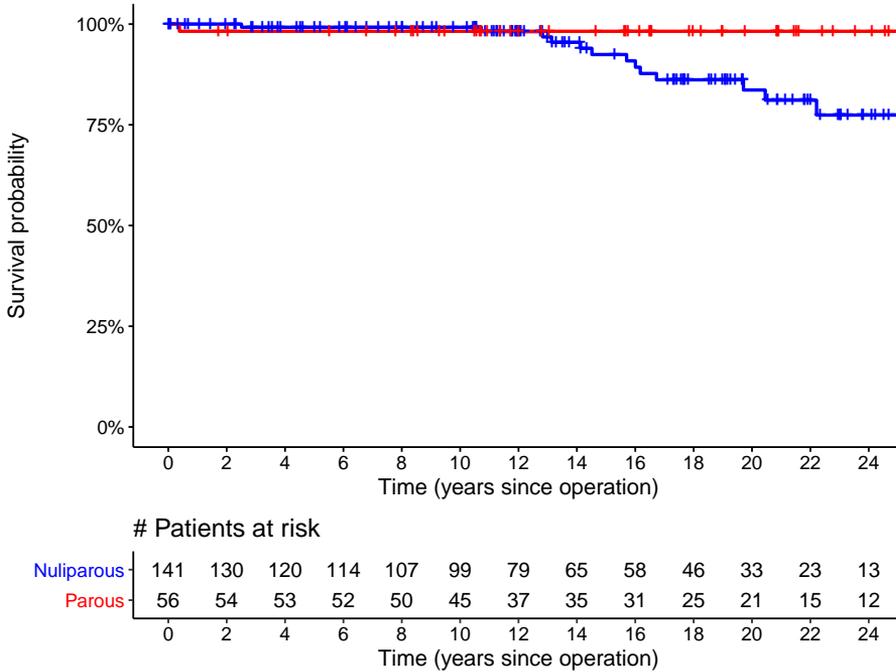


Figure 3.1: Kaplan-Meier curves of overall survival after allograft replacement

3.4 Discussion

We described the long term effect of pregnancy on the clinical and longitudinal echocardiographic outcome of allografts in RVOT position. The results show that the occurrence of pregnancy at any moment after allograft implantation is not associated with an increased hazard of PVR. Therefore, there is no evidence to support that pregnancy negatively influences allograft function over time.

Increased rates of complications during pregnancy like premature labor, fetal demise, severe bleeding and heart failure have been reported among a wide spectrum of corrected CHD, compared to the general population (Romeo et al., 2018a; Trigas et al., 2014; Balci et al., 2011; Bédard et al., 2009; Yap et al., 2010; Grewal et al., 2009)[20-25]. Much less is known about cardiac outcome late after pregnancy and impact of pregnancy on cardiac function. As life expectancy among practically all ACHD has substantially improved during the last decades, the number of pregnancies will likely increase as well (Gilboa et al., 2016; O’Leary et al., 2016)[2, 3]. Multiple studies have demonstrated mechanical prostheses to carry extensive risks of pregnancy

3. INFLUENCE OF PREGNANCY ON LONG-TERM DURABILITY OF ALLOGRAFTS IN RIGHT VENTRICULAR OUTFLOW TRACT

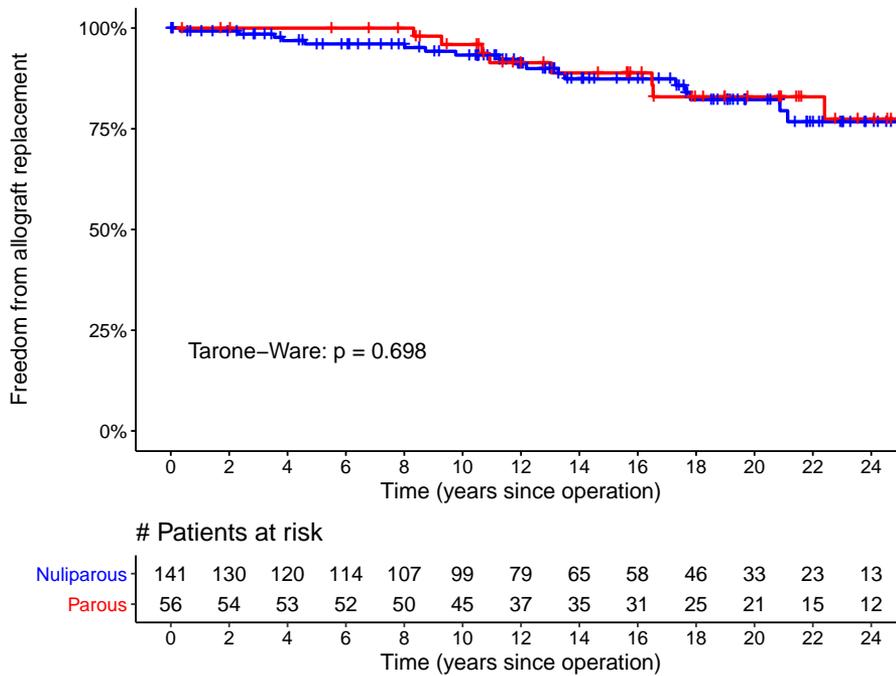


Figure 3.2: Kaplan-Meier curves of freedom from allograft replacement

related complications (Steinberg et al., 2017; van Hagen et al., 2015; Ayad et al., 2016)[9, 10, 26]. Previous studies on pregnancy have mainly focused on bioprostheses and mechanical prostheses in the aortic position (Arabkhani et al., 2012; Doer and Somerville, 1997; North et al., 1999; Basude et al., 2014)[27-30]. In their study on allografts and autografts in the aortic position, Arabkhani et al. described the influence of pregnancy on the longitudinal evolution of gradient, sino-tubular junction diameter, annulus diameter and regurgitation grade. They reported no significant influence of pregnancy on all mentioned evolutions with a comparable freedom from valve reoperation between parous and nulliparous (Arabkhani et al., 2012)[27]. In another report on allografts in aortic position North et al. reported a 10 year freedom from valve loss defined as allograft replacement or valve-related death of 72%, an no influence of pregnancy (North et al., 1999)[29].

Although allografts and bioprostheses are less thrombogenic and therefore independent from anticoagulation, they suffer from structural deterioration (Romeo et al., 2018b; Christenson et al., 2010)[11, 31]. The outcome of parous women with RVOT allograft conduits has been reported earlier in smaller (Avila et al., 2002; Cleuziou

Table 3.2: Joint model estimates of the association with pulmonary valve replacement

	HR	95% CI	P
Occurrence of first pregnancy	0.726	(0.049 - 4.482)	0.796
Age	1	(0.951 - 1.030)	0.890
Current value of gradient	1.051	(1.030 - 1.062)	<0.001
Current value of regurgitation	1.209	(1.010 - 1.537)	0.038
Interaction with occurrence of first pregnancy:			
Current value of gradient	1.030	(0.980 - 1.105)	0.258
Current value of regurgitation	1.030	(0.844 - 1.391)	0.774

CI = Credible interval, HR = Hazard Ratio

et al., 2010; Eric Jamieson et al., 1995; Sadler et al., 2000) cohorts [32-35]. However, these studies only focused on complications during or directly after pregnancy without reporting the longitudinal allograft function over time and the effect of pregnancy on this outcome. These studies have generally reported positive clinical outcomes (Avila et al., 2002; Cleuziou et al., 2010; Eric Jamieson et al., 1995; Sadler et al., 2000) [32-35]. Cleuziou et al. studied the rate of degeneration of 45 bioprostheses and 42 allografts, of which 40 in RVOT position. Pregnancy was not a risk factor for accelerated valve failure with freedom from valve replacement at 10 years of 73% and 52% ($p=0.2$) for patients with and without pregnancy, respectively (Cleuziou et al., 2010) [33]. Oosterhof et al. studied the risk of allograft failure and dysfunction after repair of Tetralogy of Fallot. Data from the Zahara study were included and indicated no effect of pregnancy on allograft durability (Oosterhof et al., 2006) [36]. Metz et al. were the only authors to report a negative influence of pregnancy on general cardiac health in patients after pulmonary valve surgery. Among women who underwent PVR or pulmonary repair, 33 women with 95 completed pregnancies were compared to 20 nulliparous. A higher incidence rate of the composite outcome of unanticipated cardiac surgery, heart failure and death was reported in the parous group compared to nulliparous women. However, when the authors looked closely at this group of patients they found that adverse cardiac outcome after pregnancy was more prevalent in patients with pulmonary valve surgery (not replacement) compared to those did

had undergone PVR. (Metz et al., 2013)[37]. The mixed cohort of Metz et al. including a modest proportion of patients with replaced valves can potentially explain their findings. In general however, research about the influence of pregnancy on prosthetic valve durability is limited and even though in line with our results, often lack statistically robust methodology (Arabkhani et al., 2012; Avila et al., 2002; Cleuziou et al., 2010; Eric Jamieson et al., 1995; Sadler et al., 2000; Oosterhof et al., 2006; Heuvelman et al., 2013)[27, 32-36, 38].

In our cohort, parous women differed in baseline characteristics only with regard to right ventricular hypertrophy. Other baseline characteristics were comparable. However, cardiac and general health, other than allograft function alone, might have influenced the desire, ability and advise from consulting cardiologists to become pregnant. In parous women, pregnancy did not influence allograft function and hazard of PVR. However, the results and, therefore, conclusions are restricted to parous women and are therefore more likely to be in better cardiac health. Only two women could be identified who became pregnant despite explicit contraindications on cardiac grounds.

This study shows that longitudinal allograft function over time is unaffected by the occurrence of pregnancy. Therefore, pregnancy does not influence durability of allografts as demonstrated by using a novel and advanced biostatistical framework (Papa-georgiou et al., 2019)[39]. The use of mixed and joint modelling has been limited in Cardio-Thoracic research even though it has been recommended by the 2008 guidelines for reporting mortality and morbidity after cardiac valve interventions (Akins et al., 2008; Arabkhani et al., 2012; Mokhles et al., 2014)[16, 27, 40]. Combining serial measurements of any biomarker with a time dependent event is a statistically robust method to test the potential influence of the latter, by more optimally utilizing available data.

3.4.1 Strength and Limitations

We assessed the effect of pregnancy on RVOT allograft durability was longitudinally assessed using innovative statistical methods. Furthermore, follow-up completeness was high and a large number of standardized echocardiograms were available for the analyses. In contrast to earlier studies, innovative statistical methods were used to analyze the data. Because pregnancy is ethically and practically impossible to randomize, future research should combine these type of innovative statistics with data from prospectively followed cohorts.

The exact potential mechanism through which pregnancy could influence long term allograft function is largely unknown. As the change in hemodynamics are transitory

during pregnancy, it would be more clinically accurate to model a temporary effect of pregnancy which fades of after labor. However, this approach would require an extensive amount of measurements before, during and after pregnancy to reliably estimate the temporal effect and was therefore impossible in the current analysis. Furthermore, while the effect of pregnancy on pulmonary gradient and pulmonary regurgitation was not found to substantially alter their evolutions, a small change was detected. Taking into account that only 13.7% of the subjects experienced pregnancy, results should be interpreted with care since power is low.

3.5 Conclusion

The occurrence of pregnancy at any moment during at least the first 15 years after RVOT reconstruction with an allograft conduit does not influence allograft durability.

3. INFLUENCE OF PREGNANCY ON LONG-TERM DURABILITY OF ALLOGRAFTS IN RIGHT VENTRICULAR OUTFLOW TRACT

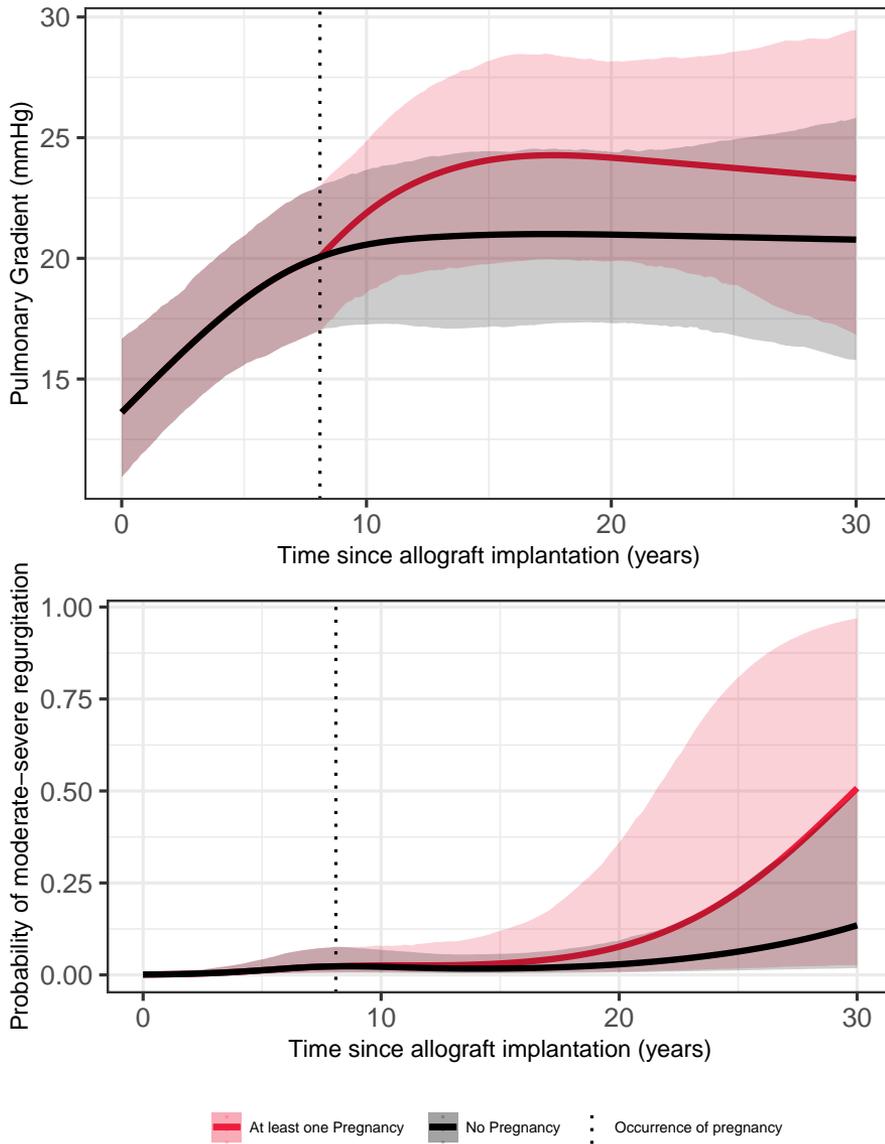


Figure 3.3: Mixed-effects models of transpulmonary peak gradient (mmHg) and moderate-severe regurgitation

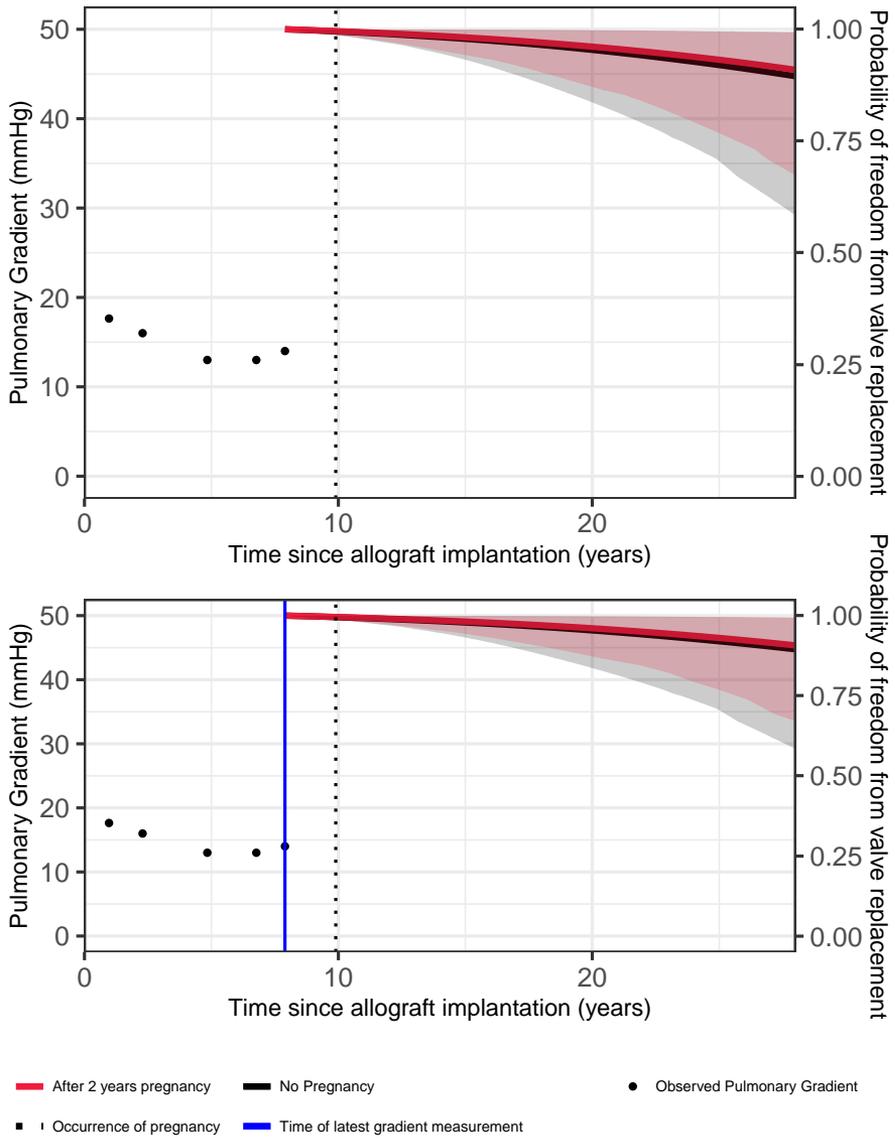


Figure 3.4: Influence of pregnancy on freedom from valve replacement

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Part II

Multi-state Models & Shrinkage

Feature Selection of Longitudinal Biomarkers in Multivariate Joint Models for Longitudinal and Multi-State Processes

This chapter is based on:

Papageorgiou, G, Mokhles, M.M., Muslem, R., Brugts, J., Manintveld, O.C., Constantinescu, A.A., Bekkers, J., Takkenberg, J.J.M., Rizopoulos, D. (2021) Feature Selection of Longitudinal Biomarkers in Multivariate Joint Models for Longitudinal and Multi-State Processes *Manuscript in Preparation*

Abstract

This work is motivated by a study at the Erasmus University Medical Center in the Netherlands on patients who received a Left Ventricular Assist Device (LVAD) after heart failure. These patients may experience multiple and potentially successive complications during follow-up, such as thrombosis and embolism which may increase their risk of dying. To reduce these risks, treating physicians follow these patients closely and collect repeated marker measurements for their liver and kidney function, both before and after LVAD intervention. Their primary research goals are to understand better how these biomarkers are associated with the risk of each complication and how LVAD intervention changes the dynamics between these associations, to better guide their decision making with respect to LVAD intervention.

In this context, the joint modeling framework is a popular choice in addressing such objectives. However, while there has been a lot of work towards extensions of the classic joint modeling framework, such as multivariate joint models, joint models for a longitudinal outcome and a multi-state process and Bayesian shrinkage selection for the association structure in joint models, a united approach allowing for all these features simultaneously has yet to be studied. Furthermore, investigating the performance of Bayesian shrinkage methods in terms of feature selection in highly correlated settings has not received a lot of attention.

We therefore propose a flexible multivariate joint model for longitudinal and multi-state processes that includes LVAD intervention as a time-varying covariate in both the multivariate longitudinal and multi-state sub-models. We further allow for different association structures between the longitudinal markers and the transition-specific intensities, while allowing for baseline characteristics' effects to differ for each transition. To determine the most appropriate functional forms we use informative global-local shrinkage priors on the regression coefficients that correspond to the covariates of the transition-specific intensities.

The results suggest that the use of the global-local shrinkage priors may improve the estimation and identification of association parameters and functional forms respectively. However, the impact of the correlation among features and the number of observed transitions needs to be further investigated.

The clinical impact of tricuspid regurgitation in patients with a biatrial orthotopic heart transplant

This chapter is based on:

Veen, K.M.* , Papageorgiou, G*, Zijderhand, C., Mokhles, M.M., Brugts, J., Mantveld, O.C., Constantinescu, A.A., Bekkers, J., Takkenberg, J.J.M., Bogers A.J.J.C. and Kaliskan, C. (2020) The clinical impact of tricuspid regurgitation in patients with a biatrial orthotopic heart transplant *Submitted to The Journal of Thoracic and Cardiovascular Surgery*

* both authors contributed equally

Abstract

Introduction

Tricuspid regurgitation (TR) is common in patients with after biatrial orthotopic heart transplant (OHT). Nevertheless, the clinical impact and long-term sequel of TR remains unclear. In this study, we aim to elucidate the clinical impact and long-term course of TR, taking into account its dynamic nature.

Methods

All consecutive adult patients undergoing biatrial OHT (1984-2017) and with an available follow-up echocardiogram were included in this study. Mixed-models were used to model the evolution of TR. Thereafter, the estimated trajectory was inserted into a Cox model, under the joint-model framework, in order to address the association of the dynamic TR with mortality.

Results

In total, 572 patients were included (median age: 50 years, males:74.9%). Approximately 32% of patients had moderate-to-severe TR immediately after surgery. However, this declined to approximately 11% on 5 years and 9% on 10 years after of surgery, adjusted for survival bias. Pre-implant mechanical support was associated with less TR during follow-up, whereas concurrent LV dysfunction was significantly associated with more TR during follow-up. Survival at 1, 5, 10, 20 years was $97\pm 1\%$, $88\pm 1\%$, $66\pm 2\%$ and $23\pm 2\%$, respectively. The presence of moderate-to-severe TR during follow-up was associated with higher mortality (HR:1.07,95%CI[1.02-1.12], $p=0.006$). The course of TR was positively correlated with the course of creatinine ($R=0.45$).

Conclusion

TR during follow-up is significantly associated with higher mortality and worse renal function. Nevertheless, probability of TR is the highest immediately after OHT and decreases thereafter. Therefore, it may be reasonable to refrain from surgical intervention for TR during earlier phase after OHT.

Part III

Missing Data

An alternative characterization of MAR in shared parameter models for incomplete longitudinal data and its utilization for sensitivity analysis

This chapter is based on:

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Abstract

Dropout is a common complication in longitudinal studies, especially since the distinction between random (MAR) and non-random (MNAR) dropout is intractable. Consequently, one starts with an analysis that is valid under MAR and then performs a sensitivity analysis by considering MNAR departures from it. To this end, specific classes of joint models, such as pattern-mixture models (PMMs) and selection models (SeMs), have been proposed. On the contrary, shared-parameter models (SPMs) have received less attention, possibly because they do not embody a characterisation of MAR. A few approaches to achieve MAR in SPMs exist, but are difficult to implement in existing software. In this paper, we focus on SPMs for incomplete longitudinal and time-to-dropout data and propose an alternative characterisation of MAR by exploiting the conditional independence assumption, under which outcome and missingness are independent given a set of random effects. By doing so, the censoring distribution can be utilised to cover a wide range of assumptions for the missing data mechanism on the subject-specific level. This approach offers substantial advantages over its counterparts and can be easily implemented in existing software. More specifically, it offers flexibility over the assumption for the missing data generating mechanism that governs dropout by allowing subject-specific perturbations of the censoring distribution, whereas in PMMs and SeMs dropout is considered MNAR strictly.

6.1 Introduction

Follow-up studies that include human subjects are known to be highly susceptible to dropout. The extent to which dropout will complicate the subsequent analysis depends on how the missingness is associated with the observed and unobserved longitudinal outcomes. According to the taxonomy introduced by Rubin (1976) and Little and Rubin (2002) this may happen according to three distinct missing data mechanisms: missing completely at random (MCAR), missing at random (MAR) and missing not at random (MNAR). Under MCAR, the missingness depends on neither observed nor unobserved outcomes. If the missingness is independent of the unobserved outcomes after conditioning on the observed outcomes, then the missing data mechanism is considered to be MAR. Conversely, under MNAR, conditioning on the observed outcomes cannot disentangle the dependence between the missingness process and the unobserved outcomes.

What separates MNAR from its counterparts in applied practice, though, is the concept of ignorability. That is under the (Bayesian) likelihood framework, one does not need to consider a model for the missingness process and hence 'ignore' it. Ignorability holds under the assumption that the process that generates the missing data is MAR and that the missingness and measurement processes depend on independent sets of parameters. While the innate convenience of ignorability popularized MAR models, one needs to consider if such an assumption holds carefully. That is especially the case since the distinction between MAR and MNAR is intractable as for every MNAR model, there exists a MAR counterpart with the same fit to the observed data (Molenberghs et al., 2008). Hence, one should start with an analysis that is valid under MAR and then perform a sensitivity analysis considering plausible MNAR departures from it.

To showcase the importance of such sensitivity analysis, consider the illustrative example in Figure 6.1 which is based on simulated data. The data were simulated assuming a joint model for longitudinal and survival data. To mimic MAR missingness, censoring was based on the value of previous repeated measurements and therefore the missing longitudinal trajectories (depicted with dotted gray) consist of the subjects that fulfilled the MAR criterion or experienced the event. We then fitted a model to the complete data whereas for the incomplete data we fitted an MAR and an MNAR model. All three models resulted in different fits to the data, which consequently lead to different subject-specific predictions as shown in the lower panel of Figure 6.1. Therefore, sensitivity analysis is necessary to be able to investigate the robustness of the model and the plausibility of the assumptions concerning the mechanism that generated the missing data.

To this purpose, three well established general frameworks exist, distinguished by their approach in factoring the joint distribution of the outcome and missingness processes to conditionally independent components. In a pattern mixture model (PMM), the joint distribution is expressed as the product of the marginal distribution of the missingness process and the conditional distribution of the outcome given the missingness process. Contrariwise, in a selection model (SeM), the joint distribution is expressed as the product of the marginal distribution of the outcome and the conditional distribution of the missingness process given the outcome. Alternatively, in a shared-parameter model (SPM), the outcome and the missingness processes are assumed to be driven by a set of unobserved variables, the so-called random effects. The use of latent variables gives rise to the conditional independence assumption under which the outcome and the missingness processes are independent, given the set of random effects.

The SeM framework naturally encompasses MAR while Molenberghs et al. (1998) provided a characterization of MAR under the PMM setting, specifically for the case of longitudinal data with dropout. As a result, sensitivity analysis is well-developed in the SeM and the PMM frameworks (Molenberghs and Vereke, 2005; Molenberghs and Kenward, 2007), whereas the SPM has received less attention. More specifically, Creemers et al. (2011) provided a characterization of MAR for the SPM case, by introducing the general SPM (GSPM) and then proposed a sensitivity analysis approach utilizing this framework (Creemers et al., 2010). Later, Njagi et al. (2014) proposed a characterization of MAR for the case of shared-parameter models for longitudinal and time-to-event data under the GSPM.

In this paper, we introduce an alternative characterization of MAR in SPMs for longitudinal and time-to-event data by exploiting the conditional independence assumption and utilizing the censoring distribution. By doing so, we cover a wide range of assumptions for the missing data mechanism on the subject-specific level. Previous work on the topic focused on the GSPM, which includes potentially a broad set of random effects. Here we focus on the standard SPM (Wu and Carroll, 1988; Wu and Bailey, 1988,9; Hogan and Laird, 1997,9), a particular case of the GSPM, that is most commonly encountered in practice. The benefit of doing so is that our approach is intuitively appealing and can be easily implemented in existing software. Furthermore, it allows for subject-specific perturbations of the censoring distribution, concerning the missing data generating mechanism, whereas in PMMs and SeMs dropout is considered MNAR strictly.

The rest of the paper is structured as follows. In Section 2, we propose an alternative characterization of MAR for the SPM model. In Section 3, we discuss its estimation under the Bayesian framework. In Section 4, we illustrate with an application how

the SPM can be used for sensitivity analysis with existing software. In Section 5, we present a simulation study to assess the behavior of the proposed sensitivity analysis under different scenarios with respect to the amount of MAR and MNAR missingness. Discussion follows in Section 6.

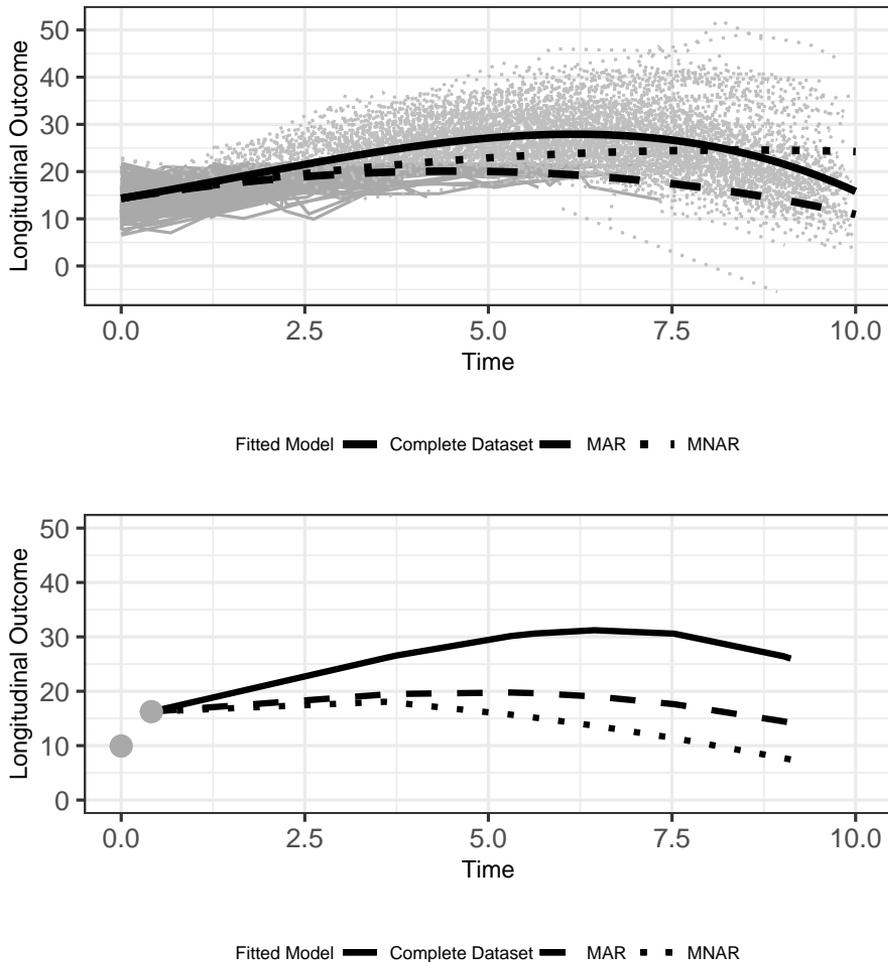


Figure 6.1: Illustrative Example: (Upper panel) observed longitudinal trajectories (black lines), missing longitudinal trajectories (gray) and fitted models using complete data and using incomplete data under MAR and MNAR. (Lower Panel) observed longitudinal measurements of a new subject and subject-specific predictions based on the three different models.

6.2 A Characterization of MAR for the Shared Parameter Model

For each subject i out of a sample of size N from the target population, let $\mathbf{y}_i = (y_{i1}, \dots, y_{in_i})^\top$ denote the vector of size $n_i \times 1$ of planned repeated measurements, with y_{ij} being the value of the longitudinal outcome at time point t_{ij} , $j = 1, \dots, n_i$, out of a set of \mathcal{J} planned measurement occasions. The vector of planned repeated measurements may further be partitioned into two vectors: $\mathbf{y}_i = (\mathbf{y}_i^o, \mathbf{y}_i^m)$, of observed and missing repeated measurements, respectively. Next, let T_i^* be the true dropout time, C_i the censoring time and $T_i = \min(T_i^*, C_i)$ the observed dropout or censoring time. Furthermore, let $\boldsymbol{\theta}$ and $\boldsymbol{\psi} = \{\boldsymbol{\psi}^{T^*}, \boldsymbol{\psi}^C\}$ be the vectors of parameters for the measurement, dropout and censoring processes respectively. Under these settings, the vectors of observed and missing repeated measurements can be expressed as $\mathbf{y}_i^o = \{y_{ij}; t_{ij} < T_i, \forall j \in \mathcal{J}\}$ and $\mathbf{y}_i^m = \{y_{ij}; t_{ij} > T_i, \forall j \in \mathcal{J}\}$. In other words, the vector of observed measurements includes all the observations which were recorded before neither dropout nor censoring occurred. On the contrary, the vector of missing measurements includes the observations which were not recorded due to either dropout or censoring. Note that we regard dropout and censoring as different causes of missingness, a distinction that we will exploit to achieve MAR characterization of SPMs.

What differentiates dropout from censoring in such a setting, pertains to the causes of leaving the study. As an example, consider the case of a study, with death as the main outcome and where a longitudinal outcome is also planned to be recorded for a time period. The planned longitudinal outcome measurements will be missing for both the subjects that died during the study but also for subjects that dropped out from the study due to any other reason (e.g. they moved to another country). Depending on the information available and the research setting, one may define death as the only cause of dropout and assume all the other reasons are non-informative and therefore record them as censoring. In the case where no information is available for the cause of dropout, then one would consider only those who completed the study as censored.

Under this framework and with covariate vectors suppressed from the notation, the shared parameter model can be specified as:

$$p(\mathbf{y}_i^o, \mathbf{y}_i^m, T_i^*, C_i; \boldsymbol{\theta}, \boldsymbol{\psi}) = \int p(\mathbf{y}_i^o, \mathbf{y}_i^m, T_i^*, C_i, \mathbf{b}_i; \boldsymbol{\theta}, \boldsymbol{\psi}, \mathbf{D}) d\mathbf{b}_i, \quad (6.1)$$

where $\mathbf{b}_i \sim \mathcal{N}(0, \mathbf{D})$ is a vector of shared random-effects assumed to induce the dependence between the processes involved in the joint density of the SPM. That is by

conditioning on the random effects the joint density of the SPM can be decomposed to the following product of conditional densities

$$\int p\left(T_i^* \mid \mathbf{b}_i; \boldsymbol{\psi}^{T^*}\right) p\left(C_i \mid \mathbf{y}_i^o, \mathbf{y}_i^m, \mathbf{b}_i; \boldsymbol{\psi}^C\right) p\left(\mathbf{y}_i^o, \mathbf{y}_i^m \mid \mathbf{b}_i; \boldsymbol{\theta}\right) p\left(\mathbf{b}_i; \mathbf{D}\right) d\mathbf{b}_i, \quad (6.2)$$

which brings to light the core assumption of conditional independence in SPMs, under which the measurement and the dropout processes are independent conditional on the random effects. Note that the conditional independence assumption commonly does not imply independence of the censoring and the measurement processes. More specifically, in the general case censoring is allowed to depend on the measurement process. Note that the conditional independence assumption may be extended to allow for independence of the censoring and the measurement processes as well. Finally, the assumption of non-informative censoring, which we discuss later, may be used to relax both these assumptions and allow for independence between the censoring and measurement processes.

Model (6.2) is a conventional SPM for longitudinal and time-to-event data. The term conventional here is in reference to the GSPM framework in the sense that a single common underlying random-effects structure is used, instead of multiple random-effects structures. Another important note for model (6.1) is that by definition, it allows for dependence between the dropout process T_i^* and the censoring process C_i . When there is no information from the data on the joint distribution of (T_i^*, C_i) , the assumption of non-informative censoring may be utilized (Tsiatis, 1975) to further simplify the model. Under both the assumptions of non-informative censoring and conditional independence, (6.2) further simplifies to

$$\int p\left(T_i^* \mid \mathbf{b}_i; \boldsymbol{\psi}^{T^*}\right) p\left(C_i \mid \mathbf{y}_i^o; \boldsymbol{\psi}^C\right) p\left(\mathbf{y}_i^o, \mathbf{y}_i^m \mid \mathbf{b}_i; \boldsymbol{\theta}\right) p\left(\mathbf{b}_i; \mathbf{D}\right) d\mathbf{b}_i, \quad (6.3)$$

which, in other words, means that the censoring process no longer depends on the random-effects and the missing observations. It should be noted that the assumption of non-informative censoring while commonly applicable, may not always be a reasonable choice depending on the setting under study. Nevertheless, it is a necessary condition for achieving an MAR characterization in SPMs without introducing more latent variables as in Creemers et al. (2011).

Note that by definition a subject may either be classified as a dropout or as censored and never both. This means that the decomposition of the joint density as described in (6.3) is, on a subject-specific level, further decomposed to

$$\begin{cases} \int p(T_i^* | \mathbf{b}_i; \psi^{T^*}) p(\mathbf{y}_i^o, \mathbf{y}_i^m | \mathbf{b}_i; \boldsymbol{\theta}) p(\mathbf{b}_i; \mathbf{D}) d\mathbf{b}_i, & i : \text{dropout} \\ \int p(C_i | \mathbf{y}_i^o; \psi^C) p(\mathbf{y}_i^o, \mathbf{y}_i^m | \mathbf{b}_i; \boldsymbol{\theta}) p(\mathbf{b}_i; \mathbf{D}) d\mathbf{b}_i, & i : \text{censored.} \end{cases} \quad (6.4)$$

The decomposition in (6.4) reveals that SPMs encompasses MAR on the subject-specific level. That is for a subject who dropped out from the study, the model is MNAR because both the dropout, $p(T_i^* | \mathbf{b}_i; \psi^{T^*})$, and measurement, $p(\mathbf{y}_i^o, \mathbf{y}_i^m | \mathbf{b}_i; \boldsymbol{\theta})$ processes depend on the missing observations through the random-effects \mathbf{b}_i . For a censored subject, though, the model is MAR since the random-effects and the missing observations appear only in factor $p(\mathbf{y}_i^o, \mathbf{y}_i^m | \mathbf{b}_i; \boldsymbol{\theta})$. Moreover, due to ignorability, the joint density reduces to the density of the observed measurement process $\int p(\mathbf{y}_i^o | \mathbf{b}_i; \boldsymbol{\theta}) p(\mathbf{b}_i) d\mathbf{b}_i$. Ignorability is a key consequence of MAR in SPMs. It entails that there are not any information to be gained from either the dropout or the censoring processes with respect to the measurement generating process and therefore MAR can be explored within the SPM framework. This is achieved without broadening the definition of the conventional SPM by introducing additional random-effects. Furthermore, the fact that MAR in SPMs is achieved on the subject-specific level allows for the potential of a subject- or cause-specific MAR sensitivity analysis. This is in contrast to the SeM and PMM frameworks which are MNAR or MAR for all the individuals under study. Finally, as we are going to illustrate in the upcoming Section, this decomposition allows exploiting existing software for its estimation.

6.3 Estimation of SPM under MAR

Estimation of the SPM under MAR follows from the conventional joint model for longitudinal and time-to-event data, which exploits the decomposition of the full joint-likelihood function to conditional independent components given the random effects. More specifically the likelihood contribution of the i^{th} subject is given by:

$$\int p(T_i^* | \mathbf{y}_i, \mathbf{b}_i; \psi^{T^*}) p(C_i | \mathbf{y}_i; \psi^C) p(\mathbf{y}_i | \mathbf{b}_i; \boldsymbol{\theta}) p(\mathbf{b}_i; \mathbf{D}) d\mathbf{b}_i, \quad (6.5)$$

The form of the conditional densities depends then on the model specification of each component. Let the risk of dropout for subject i depend on a function of the true underlying subject-specific trajectory $\eta_i(t)$. Then the instantaneous risk of dropout can be expressed as

$$\begin{aligned}
 h_i(t \mid \mathcal{H}_i(t), \mathbf{b}_i, \mathbf{w}_i) &= \lim_{\Delta t \rightarrow 0} \frac{1}{\Delta t} \Pr \{t \leq T_i^* < t + \Delta t \mid T_i^* \geq t, \mathcal{H}_i(t), \mathbf{w}_i\} \\
 &= h_0(t) \exp \left[\boldsymbol{\gamma}^\top \mathbf{w}_i + f \{ \eta_i(t), \mathbf{b}_i, \boldsymbol{\alpha} \} \right], \quad t > 0,
 \end{aligned} \tag{6.6}$$

where $\mathcal{H}_i(t) = \{ \eta_i(s), 0 \leq s \leq t \}$ denotes the history of the true underlying longitudinal process up to time t (and therefore depends on the random-effects as well), $h_0(\cdot)$ is the baseline hazard function and \mathbf{w}_i is a vector of baseline covariates with corresponding regression coefficients $\boldsymbol{\gamma}$. The association between the features of the longitudinal measurement process, $p(\mathbf{y}_i^o, \mathbf{y}_i^m \mid \mathbf{b}_i; \boldsymbol{\theta})$, and the instantaneous risk for dropout, $h_i(t \mid \mathcal{H}_i(t), \mathbf{b}_i, \mathbf{w}_i)$, is quantified by parameter vector $\boldsymbol{\alpha}$. Function $f(\cdot)$ may take various forms but for the remainder of the paper we will assume that $f(\eta_i(t), \mathbf{b}_i, \boldsymbol{\alpha}) = \alpha \eta_i(t)$, the so-called current value association, which postulates that the risk of dropout at time t depends only on the current value of the true underlying subject-specific trajectory at the same time $\eta_i(t)$. Let \mathbf{u}_i be a vector of baseline covariates with corresponding regression coefficients $\boldsymbol{\gamma}_C$ and $g(\mathbf{y}_i^o)$ a function of the observed measurements. Then, analogously, the instantaneous risk to be censored can be expressed as

$$\begin{aligned}
 \lambda_i(t \mid \mathbf{y}_i^o, \mathbf{u}_i) &= \lim_{\Delta t \rightarrow 0} \frac{1}{\Delta t} \Pr \{t \leq C_i < t + \Delta t \mid C_i \geq t, \mathbf{y}_i^o, \mathbf{u}_i\} \\
 &= h_0(t) \exp \left[\boldsymbol{\gamma}_C^\top \mathbf{u}_i + g(\mathbf{y}_i^o) \right], \quad t > 0,
 \end{aligned} \tag{6.7}$$

since based on the assumption of non-informative censoring, it cannot depend on the missing observations and the random-effects.

The probability of not dropping out from the study can then be obtained by:

$$\begin{aligned}
 S_i(t \mid \mathcal{H}_i(t), \mathbf{b}_i, \mathbf{w}_i) &= \Pr(T_i^* > t \mid \mathcal{H}_i(t), \mathbf{w}_i) \\
 &= \exp \left(- \int_0^t h_0(s) \exp \{ \boldsymbol{\gamma}^\top \mathbf{w}_i + \alpha \eta_i(s) \} ds \right),
 \end{aligned} \tag{6.8}$$

which means that unlike the instantaneous risk of dropout, the probability of remaining in the study depends on the whole true underlying subject-specific trajectory up to time t . Let $\mathcal{Y}_i^o(t) = \{ \mathbf{y}_i^o(l), 0 \leq l \leq t \}$ denote the history of the observed repeated measurements. Then, analogously, the probability of not being censored can be expressed as

$$\begin{aligned} V_i(t | \mathcal{Y}_i^o(t), \mathbf{u}_i) &= \Pr(C_i > t | \mathcal{Y}_i^o(t), \mathbf{u}_i) \\ &= \exp\left(-\int_0^t \lambda_0(s) \exp\{\gamma_C^\top \mathbf{u}_i + g(\mathbf{y}_i^o)\} ds\right), \end{aligned} \quad (6.9)$$

omitting the conditioning on missing values and the random-effects due to the non-informative censoring assumption. Finally, to distinguish between censored subjects and dropouts, let δ_i be an indicator variable which takes the value 1 if a subject dropped out from the study, that is $T_i^* < C_i$ and 0 otherwise.

Under these assumptions and suppressing covariates \mathbf{w}_i and \mathbf{u}_i from the notation, the conditional density of the dropout process can be expressed as

$$p(T_i^* | \mathbf{b}_i; \boldsymbol{\psi}^{T^*}) = \begin{cases} h_i(t | \mathcal{H}_i(t), \mathbf{b}_i) S_i(t | \mathcal{H}_i(t), \mathbf{b}_i), & \delta_i = 1 \\ S_i(t | \mathcal{H}_i(t), \mathbf{b}_i), & \delta_i = 0, \end{cases} \quad (6.10)$$

while the conditional density of the censoring process is given by

$$p(C_i | \mathbf{y}_i^o; \boldsymbol{\psi}^C) = \begin{cases} \lambda_i(t) V_i(t), & \delta_i = 0 \\ V_i(t), & \delta_i = 1, \end{cases} \quad (6.11)$$

Depending on the dropout and censoring status of the i^{th} individual, the joint-likelihood in (6.5) can be written as:

$$\begin{cases} V_i(t) \int h_i(t | \mathcal{H}_i(t), \mathbf{b}_i) S_i(t | \mathcal{H}_i(t), \mathbf{b}_i) p(\mathbf{y}_i | \mathbf{b}_i; \boldsymbol{\theta}) p(\mathbf{b}_i; \mathbf{D}) d\mathbf{b}_i, & \delta_i = 1 \\ V_i(t) \lambda_i(t) \int S_i(t | \mathcal{H}_i(t), \mathbf{b}_i) p(\mathbf{y}_i | \mathbf{b}_i; \boldsymbol{\theta}) p(\mathbf{b}_i; \mathbf{D}) d\mathbf{b}_i, & \delta_i = 0. \end{cases} \quad (6.12)$$

Under (6.12) the model is MNAR for both uncensored and censored subjects. The latter is because even for censored subjects the term $S_i(t | \mathcal{H}_i(t), \mathbf{b}_i)$ still appears in the likelihood decomposition. However, for the case that a subjects is censored, this term equals to 1 reducing (6.12) to

$$V_i(t) \lambda_i(t) \int p(\mathbf{y}_i | \mathbf{b}_i; \boldsymbol{\theta}) p(\mathbf{b}_i; \mathbf{D}) d\mathbf{b}_i, \quad (6.13)$$

which due to ignorability further reduces to

$$\int p(\mathbf{y}_i | \mathbf{b}_i; \boldsymbol{\theta}) p(\mathbf{b}_i; \mathbf{D}) d\mathbf{b}_i, \quad (6.14)$$

an MAR model for the observed longitudinal measurements. The transition from equation (6.13) to (6.14) holds due to the fact that the instantaneous risk to be censored $\lambda_i(t)$ and the probability of not being censored $V_i(t)$ are ignorable, since they strictly depend on the history of the observed repeated measurements and not the missing ones (see equations (6.7) and (6.9)). Then when a subject is censored, instead of dropout, he/she is considered MAR allowing for straightforward sensitivity analysis since it can be achieved with existing software just by doing a data manipulation step and changing all the dropout indicators to zero.

As far as the true underlying longitudinal trajectory is concerned, let $\mathbf{y}_i(t)$ be the contaminated, with measurement error $\boldsymbol{\epsilon}_i$, observed values of the true longitudinal trajectory, $\boldsymbol{\eta}_i$. Then the longitudinal process can be expressed using a mixed-effects model defined as

$$\begin{cases} \mathbf{y}_i(t) = \boldsymbol{\eta}_i + \boldsymbol{\epsilon}_i(t), \\ \boldsymbol{\eta}_i(t) = E[\mathbf{y}_i(t) | \mathbf{b}_i] = \mathbf{x}_i^\top(t) \boldsymbol{\beta} + \mathbf{z}_i^\top(t) \mathbf{b}_i, \\ \boldsymbol{\epsilon}_i \sim \mathcal{N}(\mathbf{0}, \boldsymbol{\Sigma}_i), \\ \mathbf{b}_i \sim \mathcal{N}(\mathbf{0}, \mathbf{D}), \\ \mathbf{b}_i \perp \boldsymbol{\epsilon}_i, \end{cases} \quad (6.15)$$

where the true longitudinal trajectory $\boldsymbol{\eta}_i$ is assumed to be a function of some general time-dependent design vectors $\mathbf{x}_i^\top(t)$ and $\mathbf{z}_i^\top(t)$ which are associated with a set of fixed-effects $\boldsymbol{\beta}$ and a set of subject-specific random effects \mathbf{b}_i respectively. The errors are typically assumed to be normally distributed with mean zero and a general variance-covariance matrix $\boldsymbol{\Sigma}_i$ which is commonly specified as $\mathbf{I} \times \sigma^2$. The random effects \mathbf{b}_i are also assumed to be normally distributed with mean zero and a general variance-covariance matrix \mathbf{D} , and they are also assumed to be independent from the errors.

The conditional density for the longitudinal responses is then given by

$$p(\mathbf{y}_i | \mathbf{b}_i; \boldsymbol{\theta}) = (2\pi\sigma^2)^{n_i/2} \exp\left\{-\|\mathbf{y}_i - \mathbf{x}_i\boldsymbol{\beta} - \mathbf{z}_i\mathbf{b}_i\|^2/2\sigma^2\right\},$$

with $\|x\| = \sum_i \{x_i^2\}^{1/2}$ denoting the Euclidean vector norm. The density of the random-effects is, then, given by

$$p(\mathbf{b}_i; \mathbf{D}) = (2\pi)^{-q/2} \det(\mathbf{D})^{-1/2} \exp\left(-\mathbf{b}_i^\top \mathbf{D}^{-1} \mathbf{b}_i/2\right). \quad (6.16)$$

Under the Bayesian framework, estimation of the parameters of the SPM is achieved using Markov chain Monte Carlo (MCMC) algorithms. Let $\Theta = \{\beta, \Sigma_i, \psi^{T*}, \psi^C, \mathbf{D}\}$ be a vector of unknown parameters, then the posterior distribution is proportional to:

$$p(\Theta, \mathbf{b}) \propto \prod_i p(\mathbf{y}_i | \mathbf{b}_i; \theta) p(T_i^* | \mathbf{b}_i; \psi^{T*}) p(C_i | \mathbf{y}_i^o; \psi^C) p(\mathbf{b}_i; \mathbf{D}) p(\Theta). \quad (6.17)$$

The computation of the integrals involved in $p(T_i^* | \mathbf{b}_i; \psi^{T*})$ and $p(C_i | \mathbf{y}_i^o; \psi^C)$ is achieved using standard Gauss-Kronrod and Gauss-Legendre quadrature rules. For the parameters in Θ standard prior distributions are used. More specifically, for the vector of regression coefficients β of the longitudinal submodel, for the vector of regression coefficients of the dropout submodel γ we use independent univariate diffuse normal priors. For the covariance matrix of the random-effects and inverse Wishart prior is used while for the variance of the error terms σ^2 an inverse-Gamma prior is used. For the baseline hazard we use a B-spline approximation expressed as:

$$h_0(t) = \exp\left(\gamma_{h_0,0} + \sum_{q=1}^Q \gamma_{h_0,q} B_q(t, k)\right), \quad (6.18)$$

with $B_q(t, k)$ denoting the q^{th} basis function of a B-spline with knots k_1, \dots, k_q and γ_{h_0} the vector of coefficient corresponding to the spline terms. To achieve the B-spline approximation to the baseline hazard under the Bayesian framework the following prior is specified:

$$p(\gamma_{h_0} | \tau_h) \propto \tau_h^{\rho(\mathbf{K})/2} \exp\left(-\frac{\tau_h}{2} \gamma_{h_0}^\top \mathbf{K} \gamma_{h_0}\right). \quad (6.19)$$

In the above specification, τ_h is a smoothing parameter with a Gamma(1, 0.005) hyper-prior, \mathbf{K} is a penalty matrix and $\rho(\mathbf{K})$ is its rank. For more details the reader is referred to Rizopoulos (2016).

6.4 The HIV CD4 Data: A Sensitivity Analysis

As an illustrative case study, we will use data from a randomized clinical trial designed to compare the efficacy and safety of Didanosine (ddI) versus Zalcitabine (ddC) in HIV Patients (Abrams et al., 1994; Goldman et al., 1996). In total, 467 advanced HIV patients were included in the study and were randomized to ddI (230; 49.2%) or ddC (237; 50.8%). The primary goal of the trial was to compare survival between

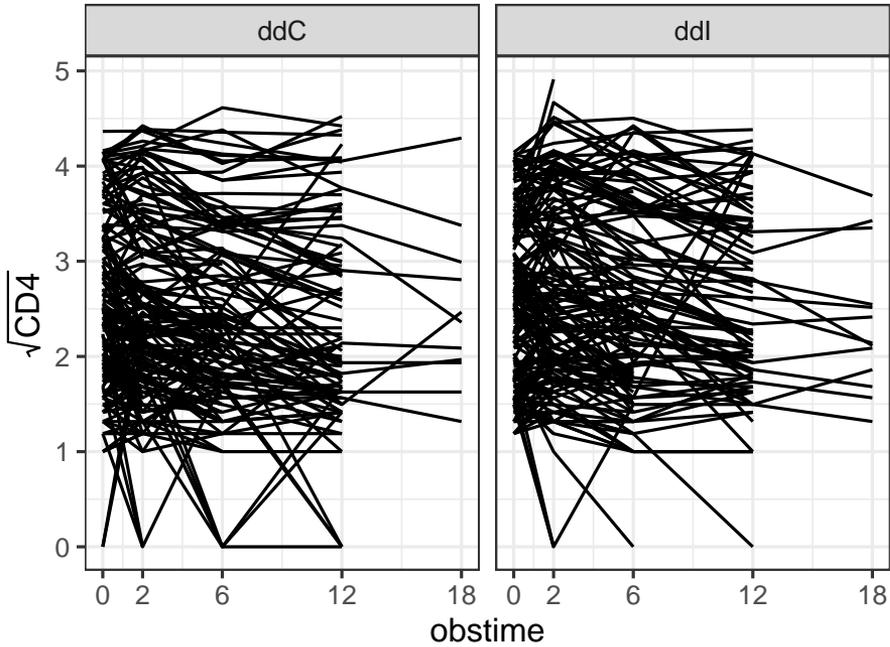


Figure 6.2: Observed longitudinal trajectories of $\sqrt{CD4}$ by treatment arm.

the two treatment arms while a secondary goal of the study was to investigate the association between CD4 cell count (a marker for the strength of the immune system) and the risk of death. For the latter goal, measurements of the CD4 cell count were recorded at scheduled visits at baseline, 2, 6, 12 and 18 months after the start of the study. Figure 6.2 shows the observed trajectories of the square root CD4 cell count. Until the end of the study, 184 (39.4%) died while only 1405 (60.1%) out of the 2335 planned visits were recorded, leading to 930 (39.9%) missing observations. In total, only 24(5.1%) patients were present for all five planned visits, 382(81.8%) dropped out from the study due to death or other reasons, and 61(13.0%) missed at least one planned visit without dropping out though from the remainder of the study. Table 6.1 shows the number of available measurements per dropout pattern per treatment arm, excluding the 61 cases of intermittent missingness.

We observe that dropout rates are similar between the treatment groups, the closer we look at the beginning of the study, but they slightly start to deviate towards the end of the study. Nevertheless, it is not possible to distinguish if the missing data are missing completely at random, missing at random or missing not at random. This

Table 6.1: Number of observed CD4 measurements per dropout pattern and per treatment arm. 'OXXXX' denotes a dropout pattern where only the first planned measurement was obtained (denoted with 'O') while the rest were not (denoted with 'X') whereas 'OOOOO' denotes a pattern for a completer (all planned measurements were obtained).

Dropout Pattern	ddC		ddI	
	N	%	N	%
OXXXX	29	14.4%	32	15.6%
OOXXX	35	17.4%	37	18.0%
OOOXX	41	20.4%	47	22.9%
OOOOX	85	42.3%	76	37.1%
OOOOO	11	5.5%	13	6.3%
Total	201	100%	205	100%

highlights the importance of being able to explore different scenarios with respect to missing data in the SPM framework via sensitivity analysis.

To model the longitudinal measurements of CD4 cell count we used a linear mixed-effects model with an interaction between time and ddI in the fixed-effects structure. We also used random-intercepts and random-slopes to allow for subject-specific deviations. The square root of the CD4 cell count was used in order to meet the normality and homoscedasticity assumptions of the model, which is defined as:

$$\sqrt{y_{ij}^o} = (\beta_0 + b_{i0}) + (\beta_1 + b_{i1}) t_{ij} + \beta_2 \text{ddI} + \beta_3 (t_{ij} \times \text{ddI}) + \epsilon_{ij}, \quad (6.20)$$

where $\mathbf{b}_i \sim \mathcal{N}(0, \mathbf{D})$, independent of $\epsilon_{ij} \sim \mathcal{N}(0, \sigma^2)$.

For the time-to-dropout T_i we assumed a relative risk model of the form:

$$h_i(t | \mathcal{H}_i(t), \mathbf{b}_i) = h_0(t) \exp[\gamma_1 \text{ddI} + \alpha \eta_i(t)], \quad (6.21)$$

where the baseline hazard $h_0(t)$ was approximated using penalized B-splines with 3 internal knots placed at quantiles of the observed event times (Eilers and Marx, 1996). The number of knots was kept small due to the low number of time-points per subject.

These two sub-models define the MNAR joint-model for the CD4 cell count and the dropout. We then assumed two different scenarios with respect to the cause

of dropout. Under Scenario 1, we assume no information concerning the cause of dropout, which means we treat dropout due to death or any other reason the same. Contrariwise in Scenario 2, we consider as dropouts only the subjects who died during the study. Finally, to achieve MAR, we assume that all the subjects are censored instead of dropping out. As shown in Section 3, this reduces the model to the mixed-effects sub-model, which is considered MAR. All models were fitted using **R** version **3.6.1** and package **JMbayes** (Rizopoulos, 2016). Table 6.2 shows the parameter estimates after fitting all three different models.

Table 6.2: Posterior means (standard errors) for an MAR and MNAR analyses.

Effect	Parameter	Scenario 1	Scenario 2	
		MNAR	MNAR	MAR
Intercept	β_0	2.4671 (0.0640)	2.4680 (0.0629)	2.4423 (0.0647)
Time	β_1	-0.0655 (0.1701)	-0.0674 (0.1715)	-0.0399 (0.0050)
ddI	β_2	0.1038 (0.0908)	0.1067 (0.0879)	0.1188 (0.0946)
ddI \times Time	β_3	0.0219 (0.2332)	0.0290 (0.2376)	0.0089 (0.0070)

While the results of all the models are close, there are quantitative differences which indicate that the findings might not be stable. This is especially the case when comparing the MAR model with both MNAR models. In Figures 6.3 and 6.4 the posterior means of the random-effects estimated from the MAR model against the respective estimated random-effects from each MNAR model are shown. Similarly, in Figure 6.5 the posterior means of the random-effects estimated from the MNAR model under the 1st Scenario are plotted against the respective estimated random-effects from the MNAR model under the 2nd Scenario. These plots give insight into the differences between the three models. We see that especially for the slope components, the differences in the random-effects' estimates are more intense between the MAR model and the MNAR models under both Scenarios. These differences become weaker when we compare the MNAR model under the 1st Scenario and the MANR model under the 2nd Scenario, which utilizes the information and distinguishes between dropout due to an event and dropout due to any other reason. This highlights the importance of sensitivity analysis in this context since the differences in the random-effects estimates would translate to differences in the subject-specific predictions based on each of the models. The results are stable under different MNAR scenarios but substantial differences are observed when using an MAR model.

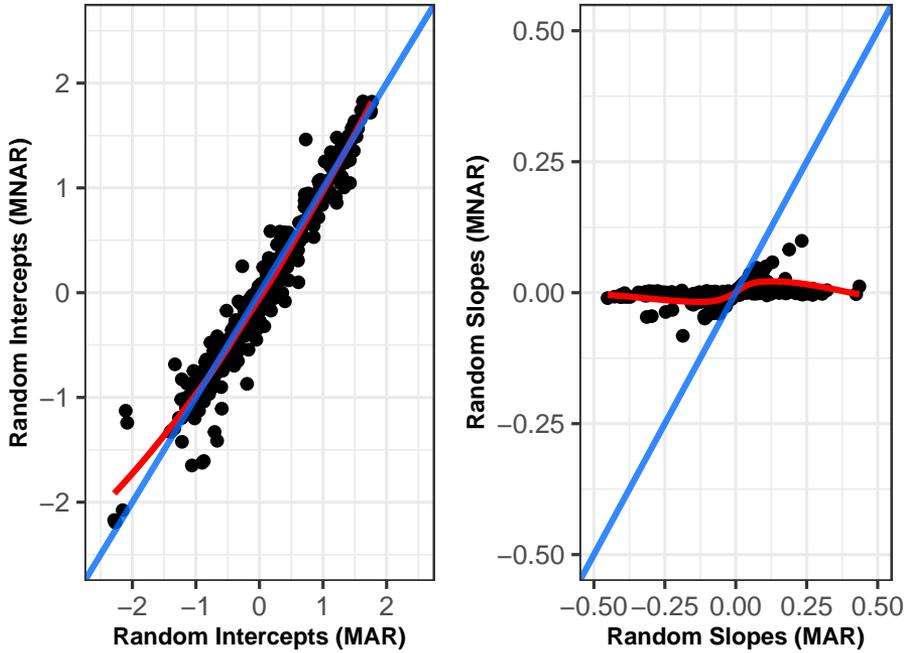


Figure 6.3: Scenario 1: Posterior means of the random-effects under MNAR and MAR.

6.5 Simulation Study

We conducted a simulation study to evaluate the performance of the following three models (used in the analysis of the HIV CD4 data):

- Model 1) all dropout cases considered MNAR (as the MNAR model used under Scenario 1 MNAR in the analysis of the HIV dataset),
- Model 2) all dropout cases considered MAR,
- Model 3) dropout cases considered MNAR if dropout due to the event or MAR otherwise (as the MNAR model used under Scenario 1 MNAR in the analysis of the HIV dataset),

under different scenarios for the amount of MAR and MNAR dropouts. More specifically, assuming a total dropout rate of 50%, we considered three different scenarios concerning the amount of dropout type: 1) 5% MAR dropouts versus 45%

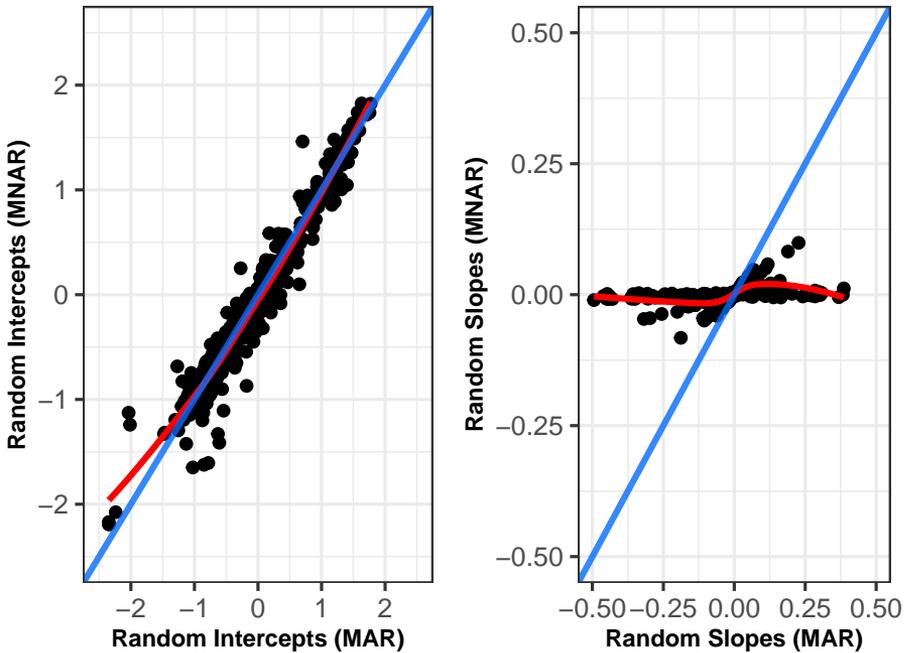


Figure 6.4: Scenario 2: Posterior means of the random-effects under MNAR and MAR.

MNAR dropouts, 2) 25% MAR dropouts versus 25% MNAR dropouts and 3) 45% MAR dropouts versus 5% MNAR dropouts. Our goal is to investigate the behavior between these models under each scenario.

We assumed 600 subjects and then randomly selected follow-up visits, t_{ij} from a uniform distribution between 0 and 10. We set the total number of measurements per subject to 10, but the final number of measurements may vary depending on whether a subject was a dropout or not. The type of dropout was then determined as follows: if the value of the longitudinal trajectory of a subject exceeded a pre-specified value, then the next time point was selected as the candidate MAR dropout time, which was then compared to the candidate MNAR dropout time. We simulated the MNAR dropout time using a joint model. Depending on which of these time points occurred sooner (if occurred), the subject was classified as MAR dropout, MNAR dropout, or completer. The threshold value for MAR varied between the three scenarios in order to attain the target percentages of dropout per type.

For the continuous longitudinal outcome, the data were simulated from a linear

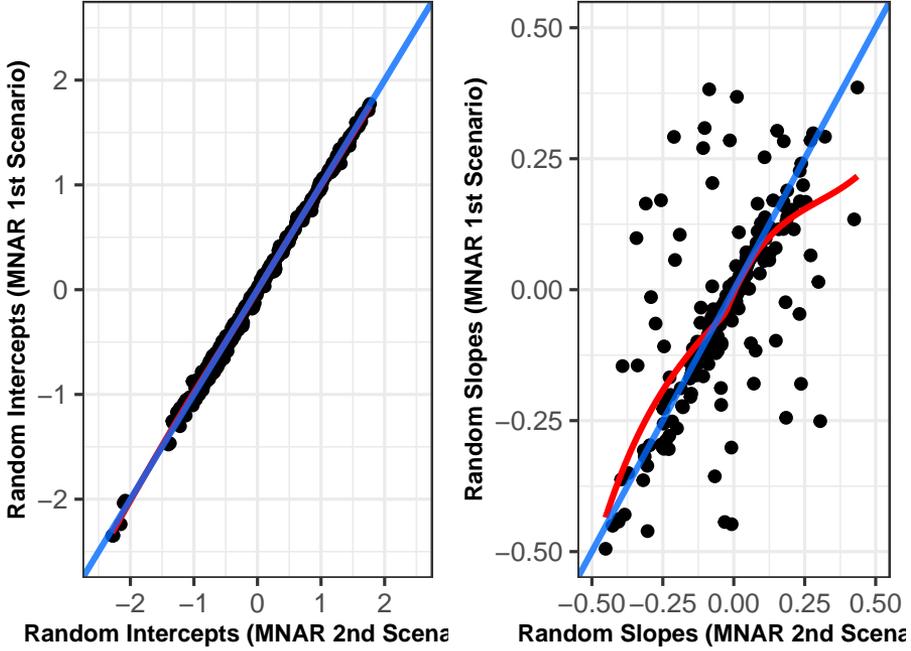


Figure 6.5: Scenario 2: Posterior means of the random-effects under MNAR (1st Scenario) and MNAR (2nd Scenario).

mixed-effects model as follows:

$$y_{ij} = (\beta_0 + b_{i0}) + (\beta_1 + b_{i1}) t_{ij} + \beta_2 \text{Xcov} + \beta_3 (\text{Xcov} \times t_{ij}) + \epsilon_{ij}, \quad (6.22)$$

where Xcov is a categorical variable with two groups, $\epsilon_i(t) \sim \mathcal{N}(0, \sigma^2 I_{n_i})$ and $\mathbf{b} \sim \mathcal{N}(0, \mathbf{D})$. The parameter values used are: $\beta_0 = 2.47$, $\beta_1 = -0.067$, $\beta_2 = 0.107$, $\beta_3 = 0.029$, $\sigma = 1.431$ and for the variance-covariance matrix of the random effects:

$$\mathbf{D} = \begin{bmatrix} d_{11} = 0.765 & d_{12} = -0.038 \\ d_{21} = -0.038 & d_{22} = 4.910 \end{bmatrix}.$$

The values of the parameters were based on the analysis of the HIV CD4 data. For time-to-dropout, we assumed a relative risk model of the form:

$$h_i(t | \mathcal{H}_i(t), \mathbf{b}_i) = h_0(t) \exp [\gamma_1 \text{Xcov} + \alpha \eta_i(t)], \quad (6.23)$$

where the baseline hazard was simulated from a Weibull distribution $h_0(t) = \xi t^{\xi-1}$ with $\xi = 3.765$.

We simulated 500 datasets per scenario, and we fitted each of the three models on each dataset. To assess the behavior of the three models, we calculated the Bias and Root Mean Squared Error (RMSE) for both the regression coefficients and the variance parameter estimates. Table 6.3 summarizes the results for the regression coefficients while Table 6.4 summarizes the results for the variance parameters. The results suggest that when the major cause of missingness is MAR, Models 2 and 3 perform similarly and slightly better than Model 1, as far as the regression coefficients are concerned. As the amount of MNAR dropout increases, the three models seem to have similar performance in the estimation of the regression coefficients with only slight differences.

On the other hand, when looking at the Bias and RMSE for the estimates of variance parameters for the random-effects, there are more distinct differences between the models. More specifically, the results suggest that Models 1 and 3 perform better than Model 2. Moreover, for the variances of the random-effects, under Model 2, the Bias seems to increase as the balance between dropout types moves from MAR dominance to MNAR dominance, whereas the case is the opposite for Model 3. The differences in the variance parameters' estimates of the random-effects between the models also imply that there are considerable differences in the estimated random-effects. The difference in the random-effects means that the subject-specific predictions derived from these models will differ.

6.6 Discussion

In this paper, we have proposed an alternative characterization of MAR for the conventional SPM and proposed its application as a sensitivity analysis tool towards MNAR deviations from the MAR assumption. In doing so, we did not broaden the definition of the SPM by adding additional random-effects structures and hence retaining the computational feasibility of the model.

Furthermore, we argued how the subject-specific nature of the MAR characterization in SPM comes with the advantage of more flexible comparisons regarding the causes of missingness. This is an important advantage over other MNAR frameworks such as the PMM and SeM since it allows distinguishing groups of subjects as MAR or MNAR depending on the information available for the causes of missingness. This was illustrated in the application to the HIV data, where we were able to consider different MNAR scenarios with respect to the information available on the causes of

missingness.

Finally, it should be mentioned that this characterization of MAR in SPMs allows for potential extensions to account for multiple causes of missingness by using for example a multi-state model and/or generalized mixed-effects models for categorical longitudinal outcomes. Dropout is present in most longitudinal studies, and our approach showed how one could perform a sensitivity analysis using standard joint modeling software to explore different causes of missingness. By doing so we do hope that such sensitivity analyses will become standard procedure and will be routinely reported in longitudinal studies with dropout.

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Table 6.3: Mean, Bias and RMSE for the regression coefficients from the three models under different scenarios for the amount of dropout caused by each missing data generating mechanism.

Parameter	Scenario 1: 5% MNAR - 45% MAR			Scenario 2: 25% MNAR - 25% MAR			Scenario 3: 45% MNAR - 5% MAR		
	Mean	Bias	RMSE	Mean	Bias	RMSE	Mean	Bias	RMSE
Model 1									
β_0	2.4532	-0.0147	0.0753	2.4667	-0.0012	0.0715	2.4705	0.0025	0.0711
β_1	0.0166	0.0840	0.1477	-0.0088	0.0585	0.1339	-0.0129	0.0544	0.1322
β_2	-0.0091	-0.1158	0.1819	-0.0109	-0.1176	0.1827	-0.0114	-0.1181	0.1821
β_3	0.1056	0.0766	0.1045	0.1045	0.0755	0.1002	0.1048	0.0758	0.0993
Model 2									
β_0	2.4688	0.0009	0.0738	2.4707	0.0028	0.0716	2.4723	0.0043	0.0712
β_1	-0.0136	0.0538	0.1322	-0.0127	0.0547	0.1322	-0.0139	0.0535	0.1319
β_2	-0.0106	-0.1174	0.1808	-0.0107	-0.1174	0.1825	-0.0116	-0.1183	0.1823
β_3	0.1060	0.0770	0.1043	0.1051	0.0761	0.1002	0.1046	0.0756	0.0994
Model 3									
β_0	2.4680	0.0001	0.0738	2.4687	0.0007	0.0717	2.4694	0.0014	0.0713
β_1	-0.0129	0.0545	0.1325	-0.0115	0.0558	0.1328	-0.0121	0.0553	0.1323
β_2	-0.0107	-0.1174	0.1810	-0.0105	-0.1172	0.1827	-0.0114	-0.1181	0.1820
β_3	0.1060	0.0770	0.1042	0.1051	0.0761	0.1005	0.1047	0.0757	0.0995

Table 6.4: Mean, Bias and RMSE for the variance parameters from the three models under different scenarios for the amount of dropout caused by each missing data generating mechanism.

Parameter	Scenario 1: 5% MNAR - 45% MAR			Scenario 2: 25% MNAR - 25% MAR			Scenario 3: 45% MNAR - 5% MAR		
	Mean	Bias	RMSE	Mean	Bias	RMSE	Mean	Bias	RMSE
Model 1									
d_{11}	0.7577	-0.0074	0.0910	0.7397	-0.0254	0.0848	0.7394	-0.0257	0.0824
d_{12}	-0.0514	-0.0134	0.1206	-0.0419	-0.0040	0.1132	-0.0265	0.0115	0.1107
d_{22}	4.7665	-0.1439	0.3248	4.6891	-0.2214	0.3543	4.6768	-0.2337	0.3600
σ	1.4318	0.0003	0.0182	1.4314	0.0000	0.0160	1.4293	-0.0022	0.0157
Model 2									
d_{11}	0.1406	-0.6245	0.6258	0.1381	-0.6270	0.6279	0.1381	-0.6270	0.6278
d_{12}	-0.0222	0.0158	0.0742	-0.0208	0.0171	0.0708	-0.0202	0.0178	0.0694
d_{22}	5.4293	0.5188	0.8668	5.4355	0.5251	0.8401	5.4484	0.5380	0.8477
σ	1.4296	-0.0018	0.0180	1.4302	-0.0013	0.0159	1.4301	-0.0014	0.0155
Model 3									
d_{11}	0.7469	-0.0182	0.0908	0.7427	-0.0224	0.0841	0.7392	-0.0259	0.0829
d_{12}	-0.0271	0.0108	0.1184	-0.0321	0.0059	0.1133	-0.0343	0.0037	0.1098
d_{22}	4.6621	-0.2484	0.3817	4.6715	-0.2389	0.3643	4.6798	-0.2306	0.3576
σ	1.4299	-0.0015	0.0181	1.4300	-0.0014	0.0160	1.4299	-0.0016	0.0156

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Statistical Primer: How to deal with missing data in scientific research

This chapter is based on:

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Abstract

Missing data are a common challenge encountered in research which can compromise the results of statistical inference when not handled appropriately. This paper aims to introduce basic concepts of missing data to a non-statistical audience, list and compare some of the most popular approaches for handling missing data in practice and provide guidelines and recommendations for dealing with and reporting missing data in scientific research. Complete case analysis and single imputation are simple approaches for handling missing data and are popular in practice, however, in most cases they are not guaranteed to provide valid inferences. Multiple imputation is a robust and general alternative which is appropriate for data missing at random, surpassing the disadvantages of the simpler approaches, but should always be conducted with care. The aforementioned approaches are illustrated and compared in an example application using Cox regression.

7.1 Introduction

Missing data are a common challenge encountered by researchers while undertaking clinical research. It can occur across all types of studies including randomized controlled trials, cohort studies, case–control studies and clinical registries. The optimum approach to missing data is to ensure that strategies are devised to ensure that the amount of missing data in a study is as small as possible. Such strategies are commonly utilized in prospectively designed clinical trials as if statistical assumptions due to missing data are required, then the protection of randomization will be broken down and unbiased estimates of treatment effect will be lost. Strategies to minimize missing data in large multicentre cohort or registry studies may be employed however, data desired for research purposes may often be missing due to the retrospective nature of the study or because the data fall outside the primary purpose of the registry (Bell et al., 2013; Little et al., 2012).

Dealing with missing data may be low on the list of priorities for a researcher when undertaking a study but it is a vital step in data analysis as inappropriate handling of missing data can lead to a variety of problems. These included a loss of statistical power, loss of representation of key subgroups of the cohort, biased or inaccurate estimates of treatment effects and increased complexity of the statistical analysis.

To ensure that missing data are handled appropriately, there are a number of steps to follow: first, taking any necessary steps to complete or reduce the amount of missing data wherever possible; second, understanding the mechanism behind the remaining missing data; third, handling the missing data using appropriate methodology and finally, performing sensitivity analyses where appropriate. Focusing primarily on the framework of missing covariate data in non-randomized studies, this article introduces the concept behind different types of missing data and compares some of the most popular approaches for handling missing data in practice. Guidelines and recommendations for dealing with and reporting missing data in scientific research are also presented along with a simulated exercise on handling missing data.

7.2 Methodology

7.2.1 Missing data mechanisms

Before discussing methods for handling missing data, it is important to review the types of missingness. Commonly, these are classified as missing completely at random (MCAR), missing at random (MAR) and missing not at random (MNAR) (Little and Rubin, 2002). An analysis of missing data patterns across contributing participants or

centres, over time, or between key treatment groups should be performed to establish the mechanisms behind the missing data (Bell et al., 2013).

Missing completely at random

Observations of all subjects are equally likely to be missing. That is, there are no systematic differences between subjects with observed and unobserved values meaning that the observed values can be treated as a random sample of the population. For example, echocardiographic measurements might be missing due to sporadic ultrasound malfunction.

Missing at random

The likelihood of a value to be missing depends on other, observed variables. Hence, any systematic difference between missing and observed values can be attributed to observed data. That is, the relationships observed in the data at hand can be utilized to ‘recover’ the missing data. For example, missing echocardiographic measurements might be more normal than the observed ones because younger patients are more likely to miss an appointment.

Missing not at random

The likelihood to be missing depends on the (unobserved) value itself, and thus, systematic differences between the missing and the observed values remain, even after accounting for all other available information. In other words, there is extra information associated with the missing data that cannot be recovered by utilizing the relationships observed in the data. For example, missing echocardiographic measurements might be worse than the observed ones because patients with severe valve disease are more likely to miss a clinic visit because they are unable to visit the hospital.

Although there are a few methods proposed to test whether the data are MCAR or MAR, their practical value is dubious (Enders, 2010). On the other hand, test distinguishing between MAR and MNAR always depends on data that are not observed meaning it is not possible to make this distinction based only on the observed data. Therefore, a researcher should always evaluate the plausibility of each missing data mechanism with respect to the method used to analyse the data and importantly on how the data were collected. The missing data mechanism should be regarded as an assumption that either supports an analysis or not rather than as an inherent and identifiable feature of a dataset. If that assumption is false, results may be biased. While under MCAR, most standard statistical tools will lead to valid results, that is

not the case for MAR and MNAR, for which appropriate methods need to be employed. Table 7.1 summarizes the basic differences between the 3 missing data types and lists which of the methods discussed in the following section can be used to draw valid inference with respect to each missing data type.

Table 7.1: Summary of missing data mechanisms.

Missing Data Mechanism	Related to	Not Related to	Probability to be missing	Valid Analysis
MCAR		Observed or missing data	Equal for every point	Complete case analysis, single and multiple imputation
MNAR	Observed data	Missing data	Equal for data points within groups	Multiple imputation
MAR	Missing data		Unequal and unknown	Sensitivity Analysis

7.2.2 Methods for handling missing data

There are various approaches for an incomplete data analysis. Two common approaches encountered in practice are complete case analysis and single imputation. Although these approaches are easily implemented, they may not be statistically valid and can result in bias when the data are not missing completely at random (J. and M.J., 2007; Vach and Blettner, 1991). On the other hand, multiple imputation is a more general approach that overcomes the main disadvantages of the aforementioned approaches when data are missing (completely) at random (van Buuren, 2012; Carpenter and M.J., 2013; Schafer, 1997).

Complete case analysis

The easiest way to deal with missing data is to drop all cases that have one or more values missing in any of the variables required for analysis. Although under MCAR this does not lead to bias of the results, it may result in significant loss of data and associated loss of power (e.g. wider confidence intervals) because the sample size is reduced. The extent of this loss of power is associated with the amount of missing data. If the data are MAR, this approach will lead to biased results. Complete case analysis may be appropriate for missing data related to the primary outcome of the study.

Single imputation

Alternatively, missing values in any variable could be replaced with a single value that is thought to best represent the mechanism of the missing data. This could be the mean of a normally distributed continuous variable, the median/mode of a categorical variable, the predicted value from a regression equation (that is, utilizing the complete observations to predict the values of the missing observations) or the best/worst observation carried forward. There may be cases where the missing risk factor data are believed to be highly likely due to the absence of a risk factor, and in this situation, it may be reasonable to impute the absence of the risk factor.

Although this approach allows the researcher to include all subjects in the analysis, it may lead to biased results. Moreover, the uncertainty of parameter estimates of the imputed variables will not necessarily improve when compared with the complete case analysis because the imputation is not conditional on the values of the outcome variable. How large the induced bias is depends on the variability of the imputed variable and on the proportion of missing values. Single imputation is also invalid under MAR since it does not account for the inter-relationships between the variables of interest. Single imputation may, however, be used to perform sensitivity analyses for missing covariate information or primary outcome data to ensure that the reported results are valid under the worst or best-case scenario.

Multiple imputation

Multiple imputation offers an alternative to overcome the disadvantages of the complete case analysis or single imputation approach. It allows the uncertainty, which is due to missing data, to be appropriately considered and can be thought of in three distinct steps: imputation, analysis and pooling of the results.

At the first step of imputation, multiple copies of the original incomplete dataset are generated. In each dataset, the missing values are replaced by values which are randomly sampled from the predictive distribution of the observed data, conditional on all other variables. The process of sampling induces variation in the imputed values which reflects the uncertainty of those imputed values.

In the analysis step, the model of interest is fitted to each imputed dataset. The results derived from each analysis will differ slightly due to the variability of the imputed values. In the third step, the results are pooled by taking the average of the estimates from the separate analyses to derive the pooled estimate and by applying Rubin's rules, which incorporate the within and between imputation uncertainty, to derive the associated standard errors. More details on Rubin's rules and the formulas that are used to obtain the pooled estimates can be found in Supplementary Material 7.A.

In contrast to the complete case analysis, multiple imputation provides valid results when the data are MAR while avoiding the loss of power due to sample size reduction. However, loss of power may still occur when using multiple imputation if there is high uncertainty in the distributions which are used to impute the missing data. Unlike single imputation, multiple imputation provides valid results if the data are MAR. This is because systematic differences between the missing and the observed values are due to information already present in the data at hand, and this is considered in the predictive distributions utilized in the first step of the multiple imputation procedure. In addition, single imputation does not account for the between-imputation variance that leads to overestimation of accuracy (small standard errors). Table 7.2 briefly summarizes the advantages and disadvantages of each method.

7.2.3 Multiple imputation: considerations and limitations

Multiple imputation is a general approach with numerous applications, and it is easily accessible through standard statistical software packages such as R (R Core Team, 2020), SPSS[®], SAS[®] and STATA[®]. However, it should be highlighted that it is not a panacea for every incomplete data setting (Erler et al., 2016; White et al., 2011). Although multiple imputation is often considered as an out of the box method that can be easily applied in any missing data problem, this is not true. Its application requires the user to carefully consider the plausibility of each of the possible causes of missingness, thoroughly select an appropriate imputation model and choose appropriate variables to include with respect to both clinical relevance and the missing at random assumption.

Some common points and special cases to consider when performing multiple impu-

Table 7.2: Comparison of incomplete data analysis methods.

Methods	Pros	Cons
Complete Case Analysis	Simple to implement	Loss of power and efficiency and invalid under MAR
Single Imputation	Simple to implement and avoids loss of power	Does not appropriately account for uncertainty in results and invalid under MAR
Multiple Imputation	Avoids loss of power, retains efficiency and is valid under MAR	Time consuming and requires more statistical knowledge

MAR: Missing at Random

tation are as follows:

- **Missing outcome information:** It should be noted that up to this point, this article has focused primarily on missing covariate information. That is because when there are missing outcome data, it has been argued that the complete case analysis is more appropriate as imputed outcome data can lead to misleading results (Von Hippel, 2007; Little, 1992). Single imputation of the worst or best-case scenario for missing outcome data may be used as sensitivity analysis to ensure the validity of trial results. Multiple imputation of missing outcome data may also be performed if there are auxiliary variables that are highly correlated with the outcome and the probability that the outcome is missing. However, this can only help in reducing the loss in accuracy of the estimates due to missing data and only if the data are at most MAR. Nevertheless, the complete case analysis should be regarded as the principle analysis in the case of missing outcome data.
- **The number of imputed datasets:** Although 5 imputed datasets are considered adequate, it is always advised to increase the number to improve the efficiency and the reproducibility of the results (White et al., 2011).

- The number of iterations: Since multiple imputation is based on an iterative algorithm, the convergence criteria should always be assessed and if necessary, the number of iterations increased (van Buuren, 2012; van Buuren and Groothuis-Oudshoorn, 2011).
- Inclusion of the outcome in the imputation model: The outcome should be included in the first step of the multiple imputation procedure to take into account the association between outcome and incomplete covariates (Moons et al., 2006).
- Longitudinal studies: Common software packages usually require the transformation of long datasets (a row per measurement) to their wide (a row per subject) counterparts to perform multiple imputation. This implies that current implementation of multiple imputation in longitudinal settings works best in balanced studies (e.g. subjects are measured at the same time points).
- Survival analysis: Because of the complex nature of the outcome variable in such cases (pairing of a binary event indicator variable with a time-to-event variable), several approaches have been proposed on how to include it in the imputation model (Barzi and Woodward, 2004; van Buuren et al., 1999; Clark and Altman, 2003). The most recent research findings, however, propose to use the Nelson–Aalen estimator along with the event indicator in the imputation model rather than the event indicator along the time-to-event variable (White and Royston, 2009).
- Acceptable amount of missingness: There is no standard rule of how much missing data is too much. Theoretically, multiple imputation can handle large amounts of missingness. Nevertheless, the quality of the results is related to the complexity of the imputation model used, whether there are few or many variables with a large amount of missingness, the total sample size and the variability of the variables which are subject to missingness. For example, 50% missingness may be acceptable if the remaining 50% of the data allow accurate estimation of the predictive distribution used to draw imputed values. In settings with a small sample size, large variability and/or a heterogeneous study population, this may not be the case.

Given the potential complexities, it is clear that multiple imputation should be conducted carefully with respect to the challenges of each analysis. Advice from statistical experts is, therefore, highly recommended when considering multiple imputation to address missing data.

7.3 Reporting

Because performing analysis on incomplete data requires a lot of considerations, decisions and assumptions, it is recommended that authors provide a thorough description of the imputation procedure to ensure the transparency and reproducibility of the analysis. Often, such a description can be moved to the Supplementary Material accompanying a manuscript. Table 7.3 provides an extensive list of points that should be included when conducting incomplete data analysis.

7.4 Data Example

To illustrate the above points with a data example, we consider a simple scenario for survival analysis. The data come from a follow-up study of patients with congenital heart disease who received a human tissue allograft in the aortic position. The aim is to investigate the association between postoperative aortic gradient (mmHg) and risk of death while accounting for baseline factors such as age at operation (years), gender, donor age (years) and allograft diameter (mm). An overview of the data for the ‘all cases’ scenario (before excluding any case to artificially generate missing data scenarios) is provided in the Supplementary Material 7.B, Table S4.

To briefly illustrate a few of the points presented throughout this article for dealing with missing data, we artificially generated 40% missingness on the postoperative aortic gradient under the 3 missingness scenarios: MCAR, MAR and MNAR. Under MCAR, randomly chosen values were deleted. Under MAR, the aortic gradient measurements of younger patients (age less than the mean age in the dataset) were deleted. Finally, for MNAR, the missing values were selected to be patients with a high postoperative aortic gradient (higher than the 65th percentile of the postoperative gradient in the dataset) assuming that they are more likely to be unable to go to the hospital. We then applied Cox regression using complete cases, single mean imputation and multiple imputation under each scenario for the mechanism that generated the missing data and compared the corresponding results with those obtained when all the cases were used (no missing data). The analysis was conducted in R (R Core Team, 2020) using the packages **mice** (van Buuren and Groothuis-Oudshoorn, 2011) and **mitools** (Lumley, 2019). A sample R code for conducting multiple imputation in R is given in Supplementary Material 7.C.

The results are summarized in Fig. 1, where the red dot and black lines represent the estimated hazard ratios and their corresponding 95% confidence intervals, respectively. As shown in this figure, under MCAR and MAR, multiple imputation provided results that were slightly closer to those of the complete data (before val-

ues were removed; ‘all cases’) than the results from the simpler approaches for this specific example. Nevertheless, the differences are small, and both the complete case analysis and single mean imputation are theoretically valid under MCAR. The loss in efficiency due to the reduced sample size when using only the complete cases is evident from the wider confidence intervals. Under MNAR, all approaches provided biased estimates. In this situation, further sensitivity analyses or explicit accounting of the missing data mechanism would be required (Carpenter and M.J., 2013).

7.5 Discussion

Missing data are common in clinical research and should be minimized wherever possible through good study design and data collection protocols. However, in most cases, it is not possible to reduce the amount of missing data to zero. As demonstrated in the example presented in this article, inappropriate handling of missing data can potentially lead to biased results or significant loss of power. Although simpler approaches in handling missing data such as the complete case analysis or single imputation may be appropriate if the amount of missing data is small and the mechanisms behind the missing data are clearly understood, in most cases multiple imputation is accepted as the preferred strategy for handling missing data. Although multiple imputation deals with a number of pitfalls related to complete case analysis or single imputation, it does significantly increase the complexity of the analysis and can potentially lead to bias if the data are not missing at random.

It is important to approach the handling of missing data in a systematic manner and clearly report the steps that have been undertaken in the handling of missing data as outlined in the guidelines in Table 7.3. Although this article is intended to give an overview for clinicians on how to handle missing data, it is strongly recommended that complex approaches to handle missing data should be performed under the guidance of a statistician.

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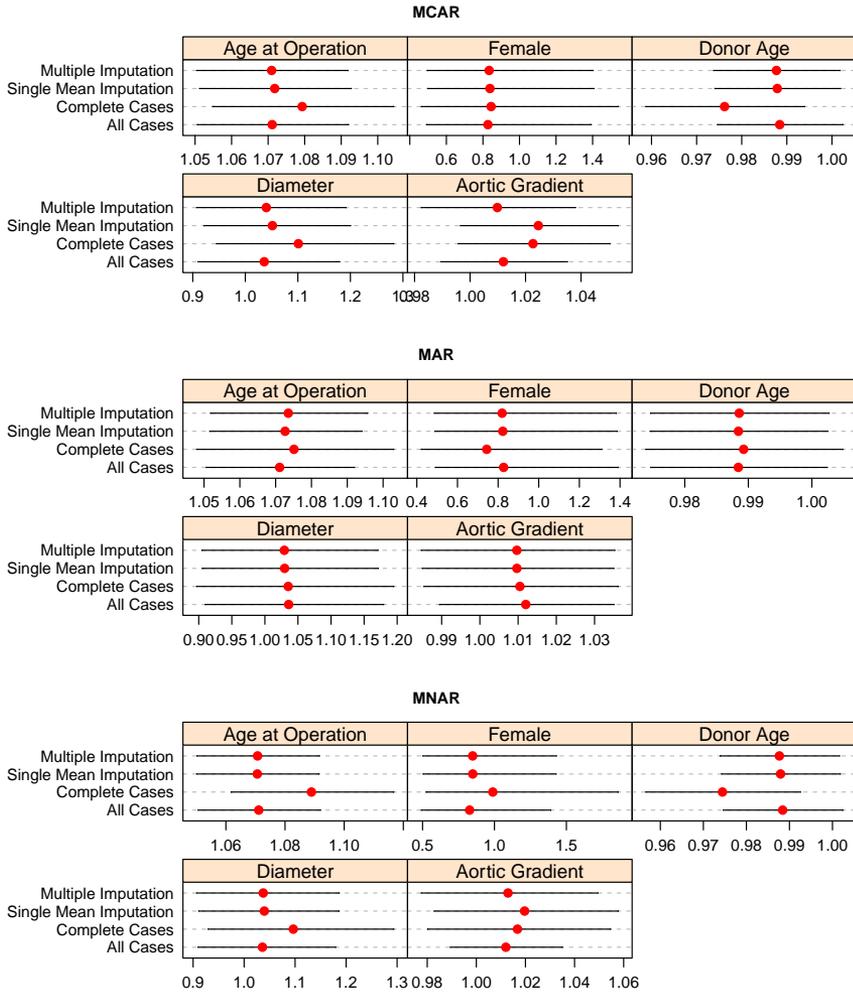


Figure 7.1: Hazard ratios and 95% confidence intervals of ‘all cases’, complete cases, single mean imputation and multiple imputation analyses under 3 missing data mechanisms. MAR: missing at random; MCAR: missing completely at random; MNAR: missing not at random.

Table 7.3: Guidelines for reporting incomplete data analysis in scientific manuscripts

Report the number/proportion of missing values per variable of interest:

- Alternatively/complementary report number of complete cases
- If possible, discuss potential causes for missing data

Provide comparison of complete and incomplete cases:

- Table or figure comparing the distributions of variables of interest

State the methodology used for incomplete data analysis:

- Which one was used: the complete case analysis, multiple imputation, etc.
- Report the assumptions that were made regarding the cause of missingness: MCAR, MAR or MNAR

Indicate the software (including version number) that was used in handling missing data:

- Optionally add any changes to the default settings/features of the software or/and functions which were used

Report the number of imputed datasets and number of iterations**List the variables that were included in the imputation model****Mention any higher order functions of imputed variables:**

- Were higher order terms such as interactions, polynomials or spline transformations of original variables used in the analysis?
- If yes, were these higher order terms included in the imputation model as well?

Assess the robustness of MAR assumption by conducting sensitivity analysis for various MNAR scenarios

MAR: missing at random; MCAR: missing completely at random; MNAR: missing not at random.

Supplementary Material

7.A A

If we denote with $\hat{\theta}_i$ the estimate of the quantity of interest which we obtained from the i^{th} imputed dataset, then the combined estimate $\hat{\theta}$ is simply the average over the imputation-specific estimates:

$$\hat{\theta} = \frac{1}{M} \sum_{i=1}^M \hat{\theta}_i, i = 1, \dots, M$$

Moreover, if we let V_i denote the estimated variance of $\hat{\theta}_i$ then the within imputation variance V is calculated as an average over all the individual variances:

$$V = \frac{1}{M} \sum_{i=1}^M V_i, i = 1, \dots, M$$

while the between-imputation variance Q is calculated based on the squared differences between the individual estimates and the combined estimate:

$$Q = \frac{1}{M-1} \sum_{i=1}^M (\hat{\theta}_i - \hat{\theta})^2, i = 1, \dots, M$$

The total variance of the combined estimate $\hat{\theta}$ is then formed by accounting for both the within- and between-imputation variances as follows:

$$\text{var}(\hat{\theta}) = V + \left(1 + \frac{1}{M}\right) Q$$

7.B B

Table 7.4: Baseline characteristics for “all cases” dataset used in the data example.

Total number of patients (n)	374
Total number of events (n)	72
Follow-Up (median; IQR)	10.95 ; (7.67, 15.35)
Age at Operation (median; IQR)	47.15 ; (34.40, 56.43)
Female Sex (n)	105
Donor Age (median; IQR)	58.79 ; (41.97, 69.53)
Diameter (median; IQR)	23 ; (21, 24)
Post-op Aortic Gradient (median; IQR)	26.94 ; (17.78, 33.80)

MAR: Missing at Random

7.C C

```
#### multiple imputation
# Load 'mice' package
library(mice)

# Load 'mitools' package
library(mitools)

# Generate 40 Imputed datasets
mice.data <- mice(data, m = 40)

# Convert to imputationList (not necessary)
# Note that the code used inside function
# imputationList():lapply(1:40, complete, x = mice.data)
# just converts the mice object to a list of data frames
# where each data frame corresponds
# to one imputed dataset.
mice.data.ImpList <- imputationList(lapply(1:40, complete, x = mice.data))

# Apply Cox regression to each imputed dataset

models.mice <- with(mice.data.ImpList, coxph(Surv(LastFUP, death) ~ AgeatOP + Sex +
DonorAge + diameter + AoGradient))

# Extract pooled estimates using MIcombine() to apply Rubin's Rules
res.mice <- summary(MIcombine(models.mice))
```

7.4 References

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Part IV

Discussion

Chapter **8**

Discussion

In this thesis, we developed extensions for the joint modeling framework for longitudinal and time-to-event data, motivated by various clinical research questions in heart disease. This chapter will discuss these extensions, summarize our findings from their implementation, and discuss possible directions for future work.

In **Part I** we extended the joint modeling framework for cases where intermediate events may occur during follow-up that may alter the course of the disease for a patient. By doing so, we were able to develop subject-specific prediction tools that are dynamic (e.g., can be updated with new information) and adaptive to different scenarios concerning the occurrence of intermediate events in the future. This is not only important because it adds a new dimension to dynamic predictions - adapting to different scenarios with respect to intermediate events, that is - but also because the accuracy of predictions in such settings is substantially influenced by the correct specification of the subject-specific longitudinal profiles (Rizopoulos et al., 2017; Ferrer et al., 2019; Suresh et al., 2017), which is in accordance to our results. Apart from the pure methodological point of view, this can directly improve clinical decision-making and patient prognosis in practice. As we have shown in our simulation study, ignoring the occurrence of the intermediate events leads to worse predictive performance. This highlights the importance of appropriately incorporating information on such intermediate events when developing prediction tools. There are numerous ways in how these intermediate events can influence the subject-specific trajectories. We suggested the use of a general function:

$$g\{R_i(t), t_{i+}\} = \tilde{\mathbf{x}}_i^\top(t) \tilde{\boldsymbol{\beta}} + \tilde{\mathbf{z}}_i^\top(t) \tilde{\mathbf{b}}_i$$

, which is a function of time-varying variables that describe the occurrence of the intermediate event. We then illustrated how one could specify this function to accommodate different situations in two applications. First, for the study on the pulmonary gradient, we encountered a particular and obvious shape for the longitudinal trajectories of the patients who experienced re-intervention (the intermediate event in this case). This allowed us to specify function $g\{R_i(t), t_{i+}\}$ to accommodate this shape of trajectories explicitly. On the other hand, for the SPRINT trial and the occurrence of serious adverse events, this was not the case, and thus, we opted for a flexible specification based on spline functions of the time-varying variables. In practice, cases, where the impact of the intermediate event on the shape of the longitudinal trajectory is so obvious as for the case of re-intervention and the pulmonary gradient might be rare, and therefore the flexible specification based on splines is to be preferred. This was the case for investigating the influence of pregnancy on the long-term durability

of allografts in the right ventricular outflow tract. In that case, the impact of the onset of pregnancy on the shape of pulmonary gradient and pulmonary regurgitation trajectories could not be easily identified. Therefore we opted for a flexible specification based on spline functions of the time-varying variables. By doing so, we were able to quantify the impact of the onset of pregnancy on the risk of valve replacement.

In **Part II** we investigated the use of Bayesian global-local shrinkage priors as a tool to automate feature selection of biomarkers in the context of multivariate longitudinal and time-to-event data. The selection of an appropriate association structure between the longitudinal and the time-to-event outcomes is a complicated task with a substantial impact on the derived predictions' quality. However, in practice, it is often the case that in the absence of previous studies on the matter, the form of this association structure is not straightforward. In such cases, part of the objective of these studies is to identify an appropriate association structure between the outcomes. As we discussed in Chapter 4 this becomes increasingly complicated in settings where the interest lies in the association between multiple longitudinal markers and multi-state data as the number of possible association parameters increases significantly along with the potential issue of collinearity between the parameters. To this end, we developed an extension of the standard joint model that can accommodate multiple longitudinal outcomes and multi-state processes, and we then used global-local shrinkage priors to aid in selecting the appropriate association structure. The two candidates we proposed, the ridge and horseshoe priors, did not show considerable differences between them in the amount of shrinkage applied to the association parameters. That was the case for both the results of our simulation study and the results in the application to the LVAD dataset. Apart from the use in high-dimensional settings where multiple longitudinal outcomes and multi-state processes are considered, the application of the global shrinkage priors can be used in less complex settings. This was the case for the study on the association between tricuspid regurgitation and survival. By applying the global shrinkage priors, we were able to identify the current-value association structure as the best option to capture the relationship between the log-odds of moderate to severe tricuspid regurgitation and survival.

Finally, in **Part III** we worked on the topic of missing data. Missing data is an unavoidable reality in clinical research that can impact patient prognosis, prediction, and clinical decision-making when not accounted for and handled appropriately. Joint models for longitudinal and time-to-event data belong in the broader family of SPMs and are commonly used as MNAR models for dropout in longitudinal studies. If in a longitudinal study there is dropout due to both random censoring and due to an event associated with the longitudinal outcome of interest, simple approaches such as mixed-effects models or time-dependent Cox models will give biased results. When

ignoring the additional information that part of the dropout is due to an informative for the outcome cause, the mechanism that generates the missing data is MNAR, but the mixed-effects model and the time-dependent Cox model treat it as MAR and MCAR, respectively. Joint models solve this by using shared-random effects to explain the association between the two. However, in practice, information about the actual cause of dropout is rarely available. In addition to that, the distinction between MNAR and MAR is intractable. To this end, the standard approach is for one to start with a model valid under MAR and then explore deviations from these assumptions for different MNAR scenarios. An evergrowing significant body of literature with essential contributions during the last two decades created an arsenal of tools for the latter. However, this mainly focused on the use of PMM and SeMs. Our contribution was to add an intuitive and readily available in standard software approach to explore MAR and MNAR scenarios using the joint modeling framework for longitudinal and survival data. An advantage of our approach is that this can be achieved on the subject-specific level in contrast to other approaches, which prospectively allows for exploring subject-specific MAR and MNAR assumptions. Another important result that arose from our simulation study and application to the HIV data was that misspecification of the missing data generating mechanism does not necessarily lead to biased fixed-effect estimates but is absorbed by the random effects in SPMs. This means that while inference on the population parameters remains stable across different assumptions for the data generating mechanism, this is not the case for subject-specific inference and in extent prediction. This is important for practicing researchers as it reflects the importance of exploring MNAR and MAR with sensitivity analysis. Apart from the methodological contribution, there must be a common language between statistical methodologists and clinical researchers in the medical field. Missing data is an example of frequent misinterpretation as it is an active area of research, it is challenging to understand for clinicians, and there is a wide range of methodology available in different software with varying levels of accessibility for clinical researchers. Thus, apart from developing new methods, it is also essential to ensure that clear and practical guidelines are well documented and communicated to aid researchers in handling missing data. In our work, we tried to do so by creating a small overview of the simple approaches to handle missing data with software examples as we believe that good communication of existing methodology is as important in practice as the development of methodology itself.

Future Research

In this thesis we focused on extending the joint modeling framework for longitudinal and time-to-event outcomes in several directions. Specifically, we developed dynamic prediction tools that can be updated as new data are collected and can be adaptive to different scenarios for the future occurrence of intermediate events; we proposed a joint model that can handle multivariate longitudinal data and multi-state processes under the Bayesian framework and explored the use of global-local shrinkage priors in feature selection, and finally, we sketched a framework for sensitivity analysis under different assumptions for missing data generating mechanisms under the joint modeling framework. These three themes were motivated by existing research questions and were applied in heart disease data.

Of course, the role of research is not only to answer questions but to generate new ones to guide future research. Before discussing potential future research directions based on these three main themes, this is a good point to highlight the importance of software in exercising research. The methods presented in this thesis can be implemented using package **JMbayes** (Rizopoulos, 2016) in R (R Core Team, 2020). Package **JMbayes** was the building block upon which we were able to develop, test, and finally apply and make available to practicing scientists the extensions discussed in this thesis. During our research work, we programmed extensions such as dynamic predictions for multivariate longitudinal outcomes and a single survival outcome, joint models for multiple longitudinal and multi-state processes, dynamic predictions with intermediate events, shrinkage priors for selecting association parameters, and sensitivity analysis. This means that these methods are now readily available in standard software and can be easily be implemented in applications by practicing researchers. Most importantly, however, the knowledge and experience we gained during extending the existing **JMbayes** package lead to the birth of its evolution: **JMbayes2**. A new package that can be used to implement joint models to even more types of longitudinal data (e.g., ordinal, beta, etc.), more types of time-to-event outcomes (competing risks, multi-state, recurrent), has improved convergence behavior and diagnostics, is more user friendly and considerably faster. **JMbayes2** not only combines all our existing knowledge and experience both in theoretical and programming terms, but we also do hope that it will serve as the building block for future research as its architecture was built with future extensions in mind.

For the remainder of this section, we will discuss future research concerning each of the main themes covered in this thesis.

In **PART I** we discussed how joint models could be used to develop dynamic prediction tools that are adaptive to the future occurrence (or not) of intermediate events.

While this is a very useful tool that can aid practicing physicians in their decision-making, it can be further improved. More specifically, in our applications, we were only able to show if there was an improvement in the predicted clinical outcome of a patient under a hypothetical future scenario regarding the occurrence of a re-intervention, serious adverse event, and pregnancy. What would be even more interesting, though, especially for re-intervention where the physician drives the decision, is how we can utilize these predictions to inform for the optimal timing of such interventions. To do so, we need in collaboration with the physicians to come up with a benefit-loss function that can aid us in quantifying the impact of the timing of such re-interventions on the clinical outcome of a patient. This is similar to the work that has been done in the field of prostate cancer and personalized schedules (Tomer et al., 2019) where a benefit-loss function was used to detect the optimal timing for future biopsy visits. We believe that utilizing the adaptive dynamic predictions to quantify benefit and risk will allow us to use it as an informative tool for optimal timing of treatments in applications where timing is essential such as the application of pulmonary grafts and re-intervention.

In **PART II** we proposed and explored the use of Bayesian global-local shrinkage priors to aid in the selection of the association structure between longitudinal and multi-state processes. While this showed to work satisfactorily in the applications considered in this thesis, a natural extension would be to assess if the application of such shrinkage priors leads to improved prediction performance. To achieve so, a comprehensive simulation study should be performed comparing different feature selection methods in joint models such as local shrinkage, bayesian global-local shrinkage, bayesian averaging in terms of measures of predictive accuracy such as the AUC the PE. We are already working towards this direction by implementing in **JMbayes2** the capability to derive predictions from joint models for longitudinal and multi-state processes. This will enable us to perform such simulations and further investigate the benefit (or not) of shrinkage selection in the joint modeling framework towards prediction modeling. Such models can translate the complex relationships between multiple outcomes into tools that can aid physicians in everyday practice. While automation of future selection sounds like an elegant tool that can replace biological reasoning and clinical thinking and make model specification an easy task for everyone, this is merely the case. To successfully translate the reality into models, statisticians and clinicians need to communicate and work together to translate years of clinical experience and knowledge into tools that can be used in practice and do not solely rely on automated and data-driven procedures. Automated and data-driven approaches can aid this communication but should not replace critical thinking.

Finally, in **PART III** we discussed how the classic joint modeling framework could

be used to conduct sensitivity analysis under different assumptions with respect to the missing data generating mechanisms. The handling of missing data has become a major topic during the last two decades, and now it is considered necessary (as it should) to conduct sensitivity analysis to explore deviations from standard assumptions about missing data. We endorse this, and we believe that future work on the topic should be focused on making these approaches easy to implement in practice as this will improve the quality of clinical research.

General Conclusion

In this thesis, we developed and applied extensions of joint models for longitudinal and time-to-event data to address different research questions, mainly in the field of heart disease. Our research covered three main themes: the occurrence of intermediate events, feature selection for joint models with multiple longitudinal and time-to-event outcomes, and missing data. The methods extend and improve the existing joint modeling framework by tackling the unique features that were posed by each research question. Dynamic predictions that are adaptive to the occurrence of intermediate events can quantify the effect of the future occurrence of such intermediate events. Bayesian global-local shrinkage priors can be used to aid in feature selection in multicollinear settings with multiple biomarkers and states of interest. Finally, joint models can be used to explore the sensitivity of assumptions with respect to missing data. While these methods might seem complicated at first, their user-friendly implementation in standard software makes its implementation easy. As more and more data are collected continuously on the individual level, the necessity and benefit of such models and prediction tools that can be dynamically updated and provide subject-specific inference will become more and more apparent. Our contribution to the joint modeling framework extends their range of use. It makes their implementation easier, providing practicing researchers with a powerful tool that can be used to derive subject-specific predictions, to understand the inter-relationships between different outcomes, and to investigate the impact of different assumptions regarding missing data. This will eventually lead to prediction models that will allow us to optimize treatment decisions and hopefully translate to improved patient outcomes.

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APPENDIX

Summary

In this thesis, we developed extensions for the joint modeling framework for longitudinal and time-to-event data, motivated by various clinical research questions in cardiothoracic surgery. Heart diseased subjects are commonly followed up over long periods, and multiple outcomes, both longitudinal and clinical, are monitored. The association of these outcomes is of primary interest as its understanding and quantification can lead to prediction models that can help optimize the treatment and the decision-making for these patients. However, such prediction models are difficult to develop as there are several factors that can influence our understanding of the relationship between these outcomes. Intermediate events such as additional treatments and serious adverse events may occur during follow-up and can alter the course of the disease. Specifying the association structure between multiple correlated outcomes is challenging as its form may be unknown. Missing data and dropout can substantially reduce available information and pose additional challenges to our inference depending on the unknown cause of missingness. Motivated by these challenges, we extend the joint modeling framework to try and overcome them.

In **Part I**, Chapter 2, we developed dynamic prediction tools that are adaptive to the future occurrence (or not) of intermediate events. Motivated by two applications in heart disease, we estimated joint models that helped us quantify the impact of re-intervention in CHD patients and SAEs in subjects with increased cardiovascular risk. We then built prediction tools that are adaptive to different scenarios for such intermediate events in the future. We compared the performance of these tools with existing simpler approaches and showed their benefit in predictive performance. In Chapter 3 we used the joint modeling framework to quantify the impact of the onset of pregnancy on biomarkers that describe the function of the pulmonary valve and clinical outcomes for these patients. We then built prediction models that were adaptive to different choices for the timing of the onset of pregnancy in the future and were able to show that there was no expected difference in the clinical outcome of women depending on the onset of pregnancy in the future.

In **Part II**, Chapter 4, we extended the joint modeling framework for the case of multiple longitudinal and multi-state processes. We discussed the challenges in choosing the association structure between these outcomes due to the increased dimensionality of the parameter space and the correlation between these outcomes. We proposed using Bayesian global-local shrinkage priors to aid in selecting relevant features that quantify the association between longitudinal and multi-state outcomes. We showcased the approach using a dataset of patients who received an LVAD after heart failure and were able to identify the association of the current value as the best

candidate for both TB and Cr and the transitions between HF, complications, and death. In Chapter 5, we applied the global-local shrinkage priors in a simpler setting with one longitudinal outcome and one time-to-event outcome to help us identify the stronger association structure. By doing so, we were able to identify the current value association as the stronger one between TR and survival.

In **Part III**, Chapter 6, we proposed an alternative parametrization of MAR for SPMs. We illustrated how this parametrization could be used in practice to perform sensitivity analysis between MAR and MNAR using the joint modeling framework. We showed how MAR and MNAR models may lead to similar effect estimates with an extensive simulation study but can substantially differ in terms of subject-specific prediction. Finally, we provided basic practical guidelines for handling missing data in clinical research to make existing methods more accessible to practicing clinicians.

General Conclusion

In this thesis, we developed and applied extensions of joint models for longitudinal and time-to-event data to address different research questions, mainly in the field of heart disease. Our research covered three main themes: the occurrence of intermediate events, feature selection for joint models with multiple longitudinal and time-to-event outcomes, and missing data. The methods extend and improve the existing joint modeling framework by tackling the unique features that were posed by each research question. Dynamic predictions that are adaptive to the occurrence of intermediate events can quantify the effect of the future occurrence of such intermediate events. Bayesian global-local shrinkage priors can be used to aid in feature selection in multicollinear settings with multiple biomarkers and states of interest. Finally, joint models can be used to explore the sensitivity of assumptions with respect to missing data. While these methods might seem complicated at first, their user-friendly implementation in standard software makes its implementation easy. As more and more data are collected continuously on the individual level, the necessity and benefit of such models and prediction tools that can be dynamically updated and provide subject-specific inference will become more and more apparent. Our contribution to the joint modeling framework extends their range of use. It makes their implementation easier, providing practicing researchers with a powerful tool that can be used to derive subject-specific predictions, to understand the inter-relationships between different outcomes, and to investigate the impact of different assumptions regarding missing data. This will eventually lead to prediction models that will allow us to optimize treatment decisions and hopefully translate to improved patient outcomes.

Nederlandse Samenvatting

In dit proefschrift hebben we uitbreidingen ontwikkeld voor het joint model framework voor longitudinale en overlevingsdata, gemotiveerd door verschillende klinische onderzoeksvragen in de cardiothoracale chirurgie. Patiënten met hartaandoeningen worden vaak gedurende lange perioden gevolgd, hetgeen resulteert in meerdere metingen, zowel longitudinaal als klinisch. De relatie tussen de uitkomsten van deze metingen is van primair belang, omdat het begrip en de kwantificering ervan kan leiden tot voorspelmodellen die kunnen helpen bij het optimaliseren van de behandeling en de besluitvorming bij deze patiënten. Dergelijke voorspelmodellen zijn echter moeilijk te ontwikkelen omdat er diverse factoren zijn die ons begrip van de relatie tussen deze uitkomsten kunnen beïnvloeden. Tussentijdse gebeurtenissen, zoals aanvullende behandelingen en ernstige bijwerkingen, kunnen optreden tijdens de follow-up en mogelijk het verloop van de ziekte veranderen. Het specificeren van de associatiestructuur tussen meerdere gecorreleerde uitkomsten is een uitdaging omdat de vorm ervan onbekend kan zijn. Ook kan er een substantiële afname in beschikbare informatie ontstaan door ontbrekende gegevens of uitval van patiënten. Dit vormt, afhankelijk van de oorzaak van de afwezigheid van data, een extra uitdaging voor onze gevolgtrekking. In ons proefschrift breiden we het joint model framework uit met als doel voor deze uitdagingen een oplossing te vinden.

In **Deel I**, Hoofdstuk 2, hebben we dynamische voorspellingstools ontwikkeld die aangepast zijn aan het toekomstige optreden (of niet) van tussentijdse gebeurtenissen. Gemotiveerd door twee toepassingen bij hartaandoeningen schatten we joint models die ons hielpen de impact te kwantificeren van herinterventie bij CHD-patiënten en SAE's bij personen met een verhoogd cardiovasculair risico. Vervolgens hebben we voorspellingstools gebouwd die zich aanpassen aan verschillende scenario's voor dergelijke tussentijdse gebeurtenissen in de toekomst. We vergeleken de prestaties van deze tools met bestaande eenvoudigere benaderingen en konden hun voorspellende gave aantonen. In Hoofdstuk 3 hebben we het joint modeling framework gebruikt om de impact te kwantificeren van het begin van de zwangerschap op biomarkers die de functie van de longklep en klinische uitkomsten voor deze patiënten beschrijven. Vervolgens hebben we voorspelmodellen gebouwd die zich aanpasten aan verschillende keuzes voor de timing van het begin van de zwangerschap in de toekomst. Tevens konden we aantonen dat er geen verwacht verschil was in de klinische uitkomst van vrouwen afhankelijk van het begin van de zwangerschap in de toekomst.

In **Deel II**, Hoofdstuk 4, hebben we het joint model framework uitgebreid voor het inzetten van meerdere longitudinale en multi-state processen. We zetten de uitdagingen uiteen bij het kiezen van de relatiestructuur tussen deze uitkomsten vanwege de

toegenomen dimensionaliteit van de parameterruimte en de correlatie tussen deze uitkomsten. We stelden voor om Bayesiaanse global-lokale krimpprioriteiten te gebruiken om te helpen de relevante kenmerken te selecteren die de associatie tussen longitudinale en multi-state uitkomsten kwantificeren. We presenteerden de aanpak met behulp van een dataset van patiënten die een LVAD kregen na hartfalen en waren in staat om de associatie van de huidige waarde als de beste kandidaat voor zowel TB als Cr en de overgangen tussen HF, complicaties en overlijden te identificeren. In Hoofdstuk 5 hebben we de global-local shrinkage priors toegepast in een eenvoudigere setting met één longitudinale uitkomst en één uitkomst uit overlevingsdata om ons te helpen de sterkere associatiestructuur te identificeren. Hierdoor konden we de huidige waarde-associatie identificeren als de sterkere van TR en overleving.

In **Deel III**, Hoofdstuk 6, hebben we een alternatieve parametrisering van MAR voor SPM's voorgesteld. We hebben geïllustreerd hoe deze parametrisering in de praktijk kan worden gebruikt om gevoeligheidsanalyses uit te voeren tussen MAR en MNAR met behulp van het joint modeling framework. We hebben laten zien hoe MAR- en MNAR-modellen kunnen leiden tot vergelijkbare effectschattingen met een uitgebreide simulatiestudie, maar aanzienlijk kunnen verschillen in termen van onderwerpspecifieke voorspelling. Ten slotte hebben we praktische basisrichtlijnen gegeven voor het omgaan met ontbrekende gegevens in klinisch onderzoek om bestaande methoden toegankelijker te maken voor praktiserende klinici.

Algemene conclusie

In dit proefschrift hebben we uitbreidingen van gewrichtsmodellen voor longitudinale en overlevingsdata ontwikkeld en toegepast om verschillende onderzoeksvragen te beantwoorden, voornamelijk op het gebied van hartziekten. Ons onderzoek omvatte drie hoofdthema's: het optreden van tussentijdse gebeurtenissen, functieselectie voor joint models met meerdere longitudinale en time-to-event uitkomsten, en ontbrekende gegevens. De methoden verbeteren het bestaande kader voor joint modeling, en breiden deze uit door de unieke kenmerken van elke onderzoeksvraag te onderwerpen. Dynamische voorspellingen die zich aanpassen aan het optreden van tussentijdse gebeurtenissen kunnen het effect van het toekomstige optreden van dergelijke tussentijdse gebeurtenissen kwantificeren. Bayesiaanse global-lokale krimpprioriteiten kunnen worden gebruikt om te helpen bij het selecteren van kenmerken in multicollineaire instellingen met meerdere biomarkers en een verschillende staat van belang. Ten slotte kunnen gezamenlijke modellen worden gebruikt om de gevoeligheid van aannames met betrekking tot ontbrekende gegevens te onderzoeken. Hoewel deze methoden op het eerste gezicht misschien ingewikkeld lijken, maakt hun gebruiksvriendelijke implementatie in standaardsoftware de implementatie ervan een-

voudig. Naarmate doorlopend meer en meer gegevens op individueel niveau worden verzameld, zullen de noodzaak en het voordeel van dergelijke modellen en voorspellingstools die dynamisch kunnen worden bijgewerkt en onderwerpspecifieke gevolgtrekkingen bieden, steeds duidelijker worden. Onze bijdrage aan het joint model framework breidt hun gebruiksbereik uit. Het maakt de implementatie ervan eenvoudiger en biedt praktiserende onderzoekers een krachtig hulpmiddel dat kan worden gebruikt om onderwerpspecifieke voorspellingen af te leiden, de onderlinge relaties tussen verschillende uitkomsten te begrijpen en de impact van verschillende aannames met betrekking tot ontbrekende gegevens te onderzoeken. Dit zal uiteindelijk leiden tot voorspellingsmodellen waarmee we behandelbeslissingen kunnen optimaliseren en deze hopelijk kunnen vertalen naar verbeterde patiëntresultaten.

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PhD Portfolio

PhD Candidate:	Papageorgiou Grigorios
Department:	Department of Biostatistics & Department of Cardio-Thoracic Surgery Erasmus Medical Center Rotterdam
PhD Period:	2015 – 2021
Promoters:	Prof. dr. Dimitris Rizopoulos Prof. dr. Johanna J. M. Takkenberg
co-Promotor:	dr. Mostafa M. Mokhles

Presentations

International Conferences	Year	ECTS
9 th EMR & Italian Region of IBS Conference, Thessaloniki, Greece	2017	1.0
38 th ISCB Conference, Vigo, Spain	2017	1.0
29 th IBS Conference, Barcelona, Spain	2018	1.0
40 th ISCB Conference, Leuven, Belgium	2019	1.0
41 st ISCB Conference, Krakow, Poland	2020	1.0

Other	Year	ECTS
Erasmus Statistics Day, Rotterdam, the Netherlands	2017	1.0
EMC & LUMC Joint Meeting, Leiden, the Netherlands	2020	1.0
CQM Symposium: Prediction to Personalize Medicine, Rotterdam, the Netherlands	2020	1.0

Teaching

Teaching Assistant	Year	ECTS
SPSS Practicals, MSc Medicine, Erasmus MC	2015 - 2020	1.5
Biostatistical Methods II (EP03), NIHES	2015 - 2020	1.5
Repeated Measurements (CE08), NIHES	2015 - 2020	1.5
Missing Data in Clinical Research (EP16), NIHES	2019	0.5

Courses

	Year	ECTS
Scientific Integrity, Erasmus MC	2017	0.5
Multivariate Dimension Reduction for Biological Data Integration, IBC	2018	0.5
Advanced methods for group sequential and adaptive trials, ISCB	2019	0.5
Regression Modeling Strategies, ISCB	2020	0.5

Seminars and Workshops

	Year	ECTS
Erasmus MC bi-weekly Biostatistics CQM Seminar	2015 - 2020	1
Erasmus MC monthly Thorax Journal Club	2017 - 2019	0.5
BMS-ANed Meeting, Leiden, the Netherlands	2017	0.2
BMS-ANed Meeting, Amsterdam, the Netherlands	2017	0.2
BMS-ANed Meeting, Rotterdam, the Netherlands	2018	0.2

Consulting

	Year	ECTS
Statistical Consultant for the Consultation centre for Patient-Oriented research (CPO)	2015 - 2020	20

Other

	Year	ECTS
Organization PhD Day BMS-ANed	2017	3

About the Author

Grigorios Papageorgiou was born in Athens, Greece. He graduated high school in 2005 and enrolled at the University of Piraeus to study towards the BSc in Statistics and Actuarial Science in 2006. After successfully obtaining his bachelor degree, he applied and was accepted to the Masters program in Statistics at the Katholieke Universiteit Leuven in Belgium. During his studies he specialized in Biometrics and graduated with honours in 2015. Immediately after graduation he started his PhD project at the Biostatistics department at Erasmus MC, in Rotterdam under the supervision of prof. dr. Dimitris Rizopoulos, prof. dr. Johanna J. M. Takkenberg and dr. Mostafa Mokhles. Currently he works as a post doc at the department of Biostatistics, as a statistician for the department of Infectious Diseases and as a methodological assessor for CBG-MEB.

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The story of a PhD has as much to do with this thesis's contents as it has to do with the people you meet, you collaborate with, and the relationships you develop with them. And I have been fortunate in that respect.

Dimitris, this is probably version 7.3.8 of this paragraph where I attempt to thank you, and like all the previous versions, it will not be up to the task. Thank you for all your generosity, the guidance and for all the opportunities you have given me. When I first arrived at the department, your first question was what I expected from you as a supervisor. I said I wanted to feel comfortable enough to ask questions frequently and even ask questions I was supposed to know. You replied: "Yes, sure. We can even discuss $1 + 1 = 2$ if you want. Just knock on my door". Indeed, you were always there to answer every knock at your door. And the truth is I did quite some knocking at this door. However, guidance was not the only thing I found there. Because while, at first, a supervisor has been answering the door, with each of these knocks over the years, the projects, the programming, the Crunch challenges, the requests for professional and sometimes even personal advice, there is now a mentor, a colleague and a true friend who answers that door.

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