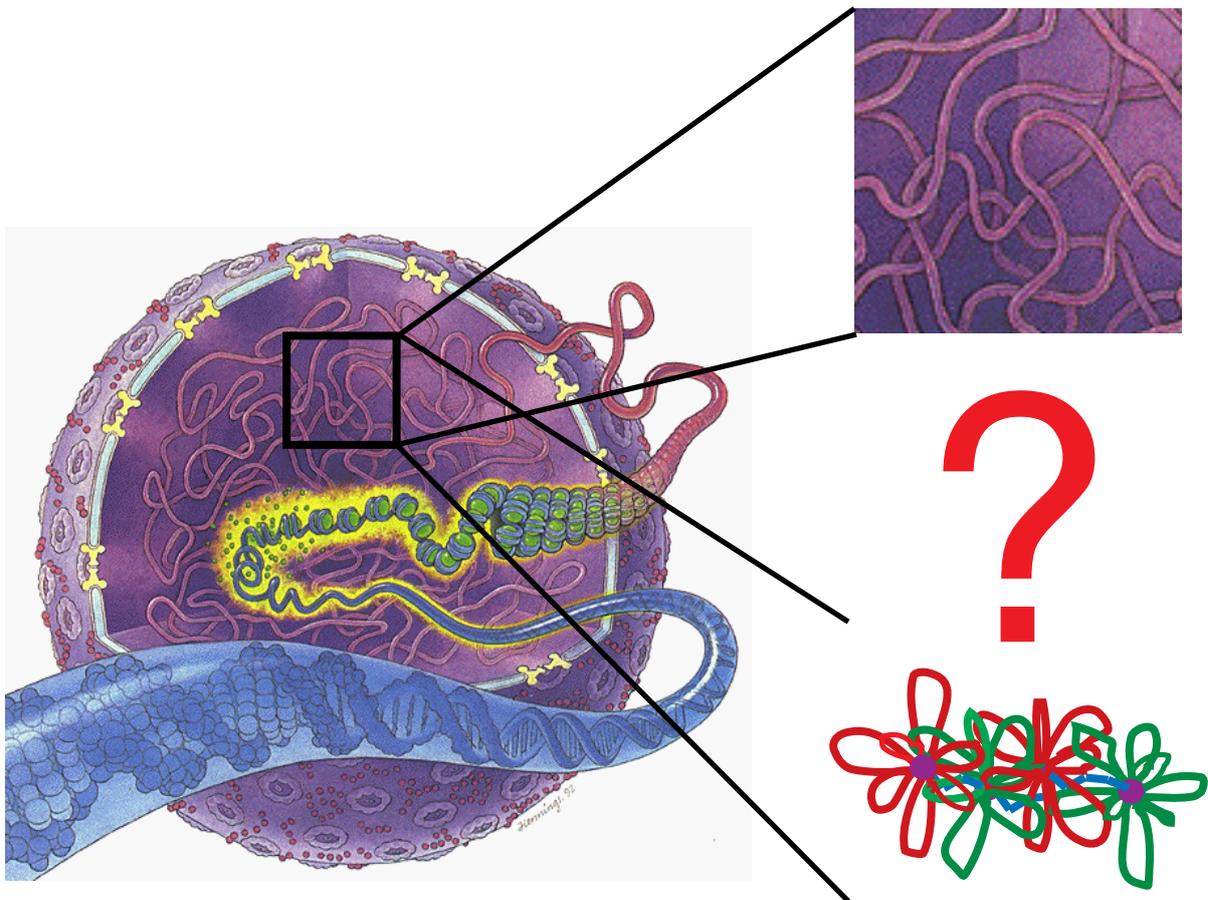
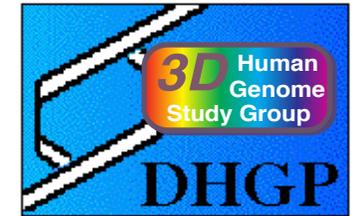


# Three-Dimensional Organization of Chromosome Territories and the Human Cell Nucleus

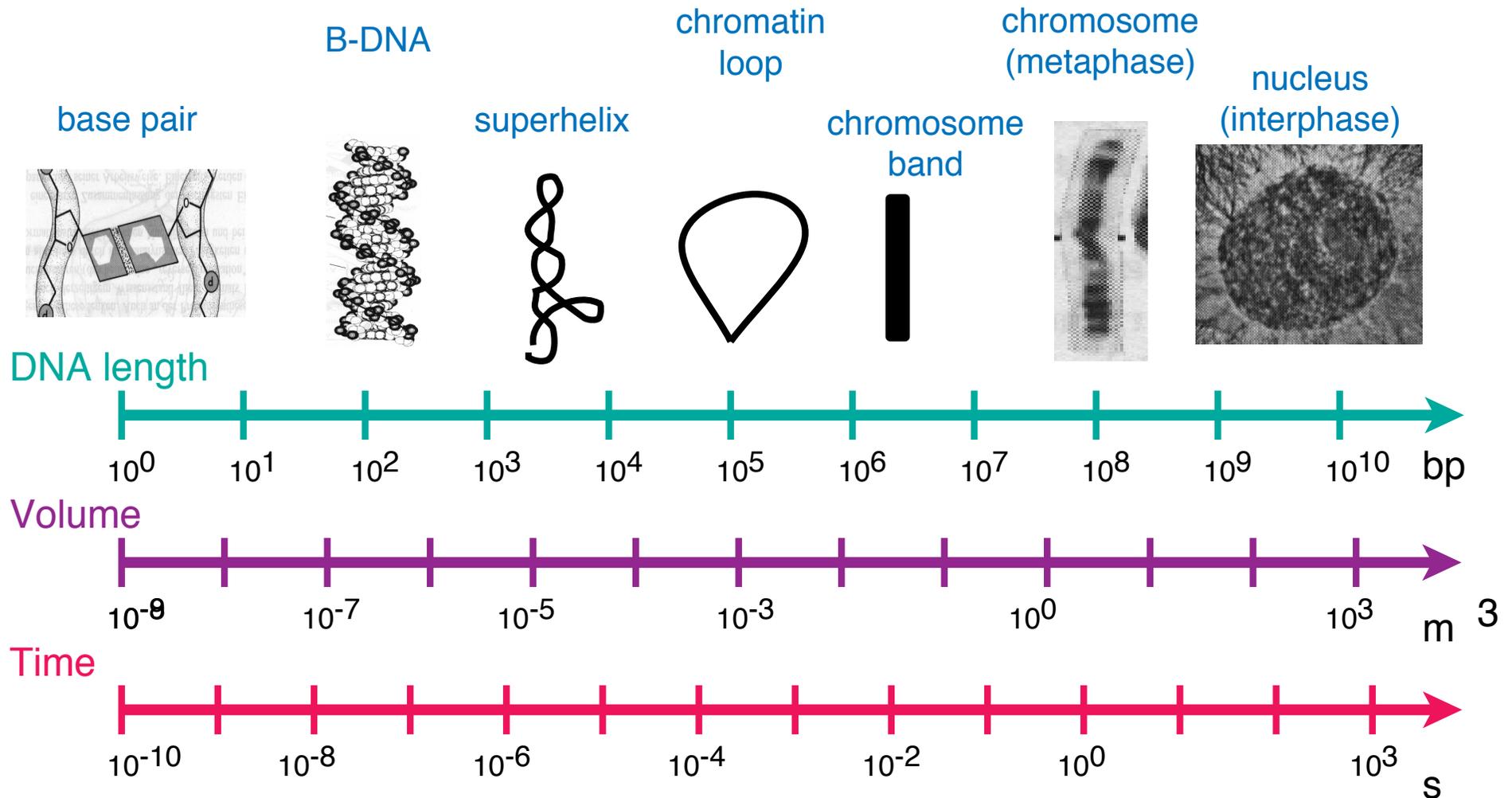


**Tobias A. Knoch, Christian Münkel, Jörg Langowski**  
**Biophysics of Macromolecules**  
**German Cancer Research Center (DKFZ)**  
**Heidelberg - Germany**

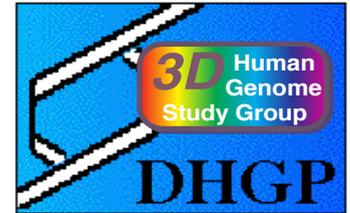
# The dynamic and hierarchical organization of cell nuclei span between 10 and 13 orders of magnitude concerning length and time scales.



Tobias A. Knoch



# Overview



Tobias A. Knoch

## Experiment

Genomic Region  
(Chromosome or Gene)



fluorescence in-situ  
hybridization (FISH)



3D confocal scanning  
microscopy



## Simulation

Multi-Loop-  
Subcompartment  
and  
Random Walk/  
Giant Loop  
model



polymer model  
for simulation of the  
chromatin fiber



## Conclusions for the human cell nucleus

chromosome-, chromosome-arm and subcompartment overlap

3D-distances between genomic markers as function of their  
genomic separation

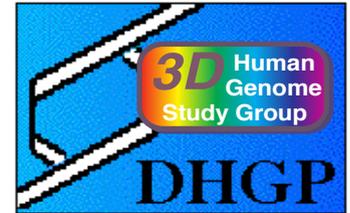
behaviour of marker ensembles and dynamics of structural features

fractal properties of chromosomes

decondensation of chromosomes from metaphase into interphase  
and chromosome stretching

conclusions from simulating whole cell nuclei

# Fluorescence in-situ Hybridization

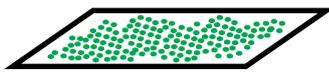


## FISH

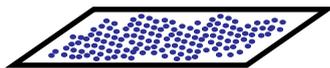
Tobias A. Knoch

### Cell - Preparation

cells on coverslip grown to confluent layer



fixation of cells on coverslip (formaldehyde) and permeabilisation



DNA double strand



### Probe - Preparation

finding of genomic site for marking and cloning of this sequence



labeling of the DNA probe (Nick translation or PCR) with

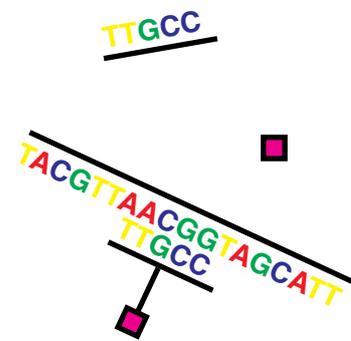
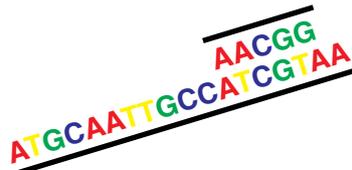
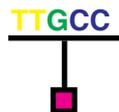
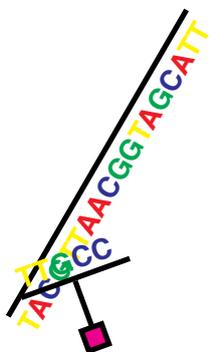
Digoxigenin (indirect)



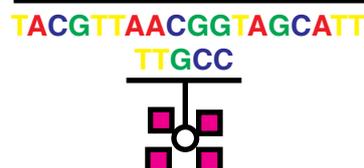
Fluorophor (direct)



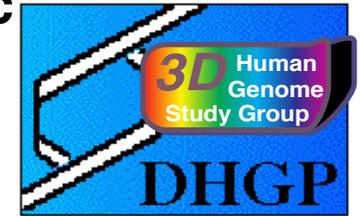
**Hybridization**  
probe is put on coverslip and melting of the double strands at 70C



amplification with fluorescent labeled antibodies



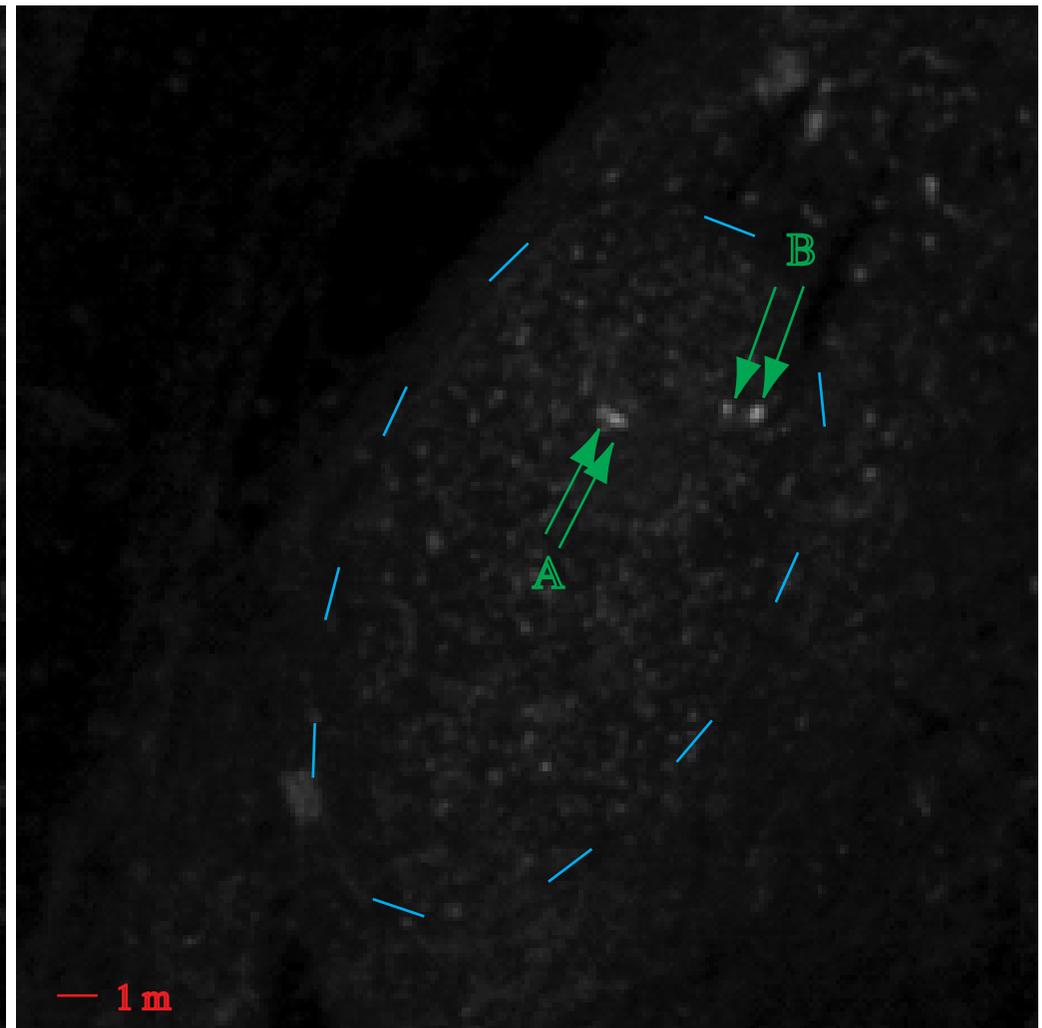
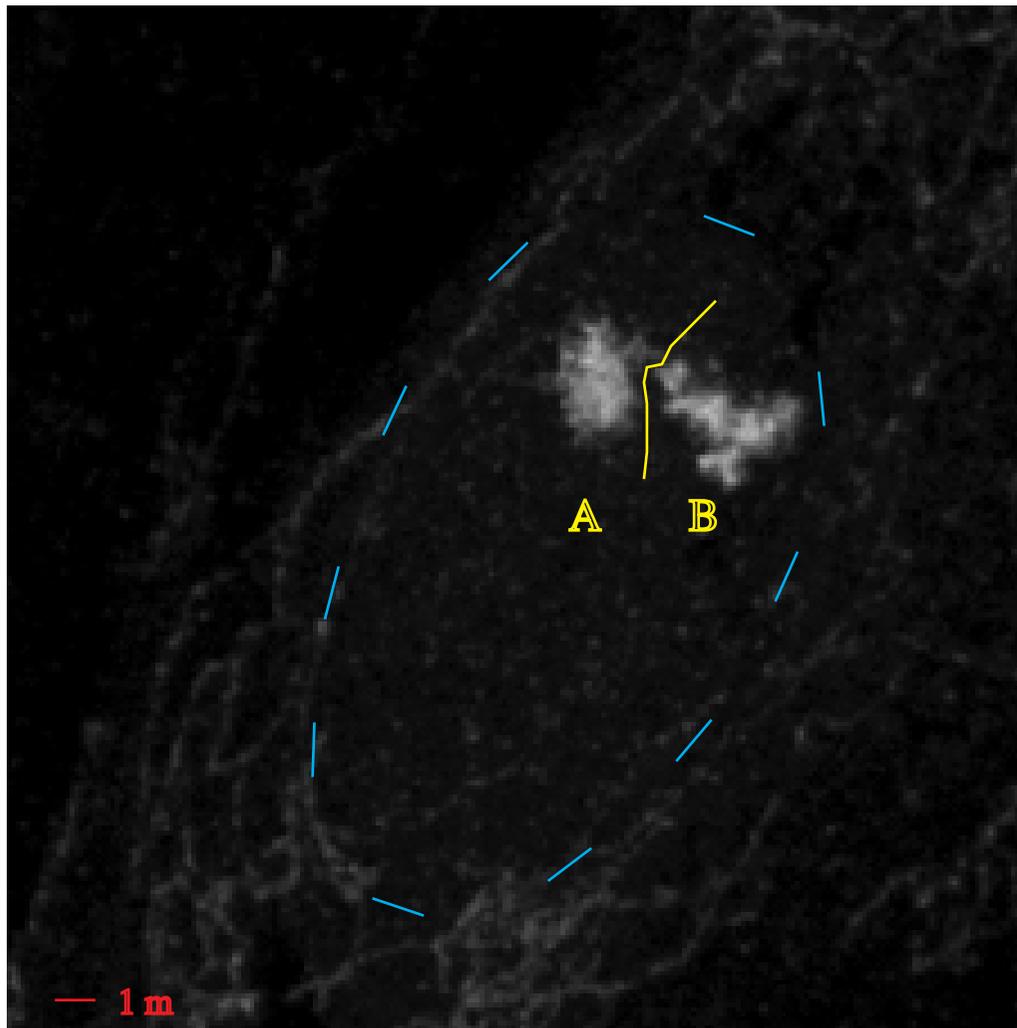
**Chromosomes form distinct territories in interphase and genomic markers lie within the territories and are clearly separable.**



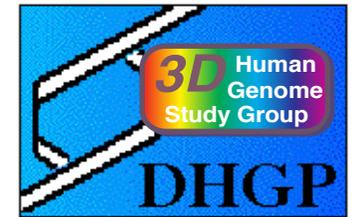
Tobias A. Knoch

Left: Territory painting by FISH of chromosome 15; by chance the two territories neighbour each other.

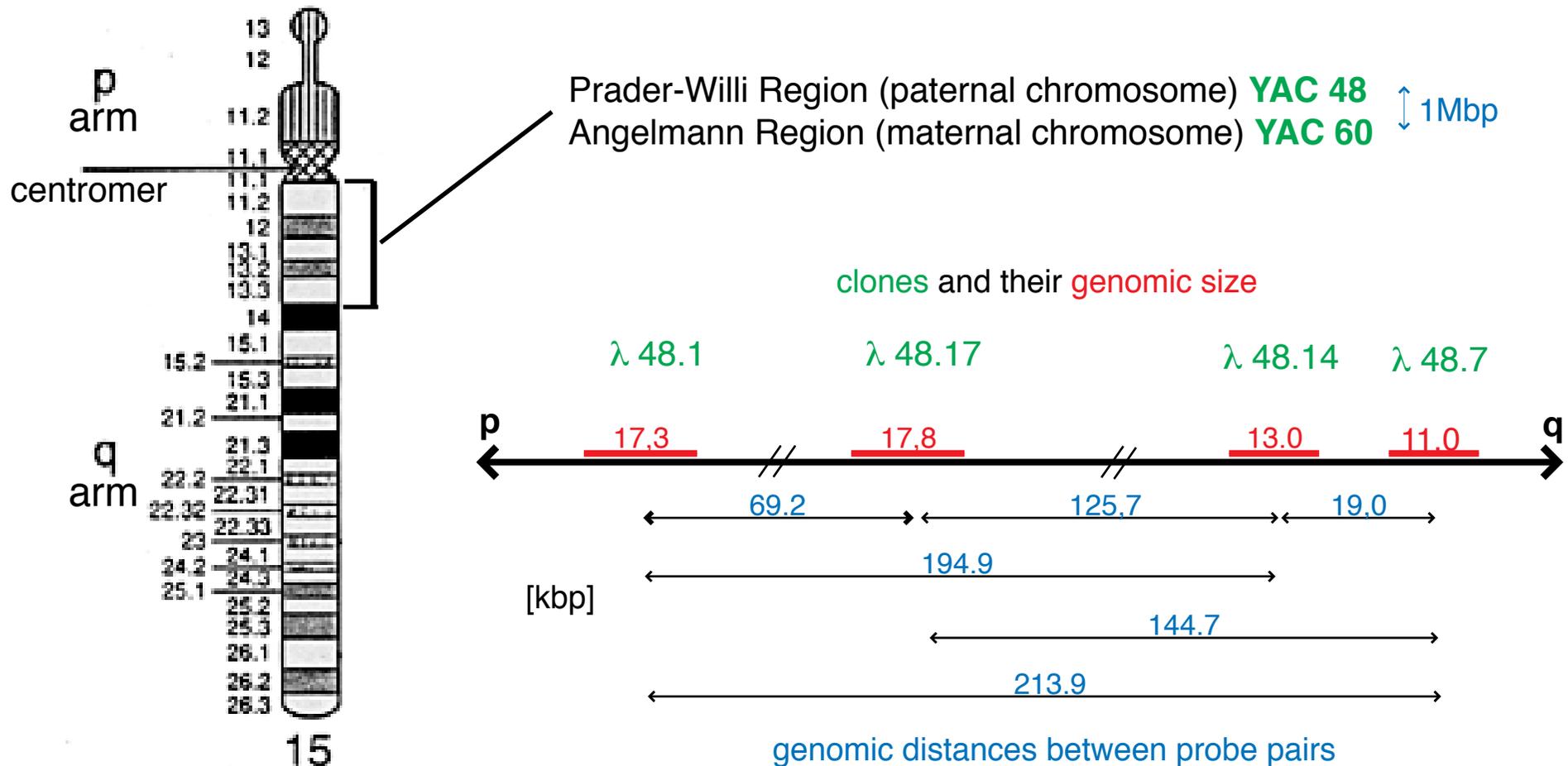
Right: Genomic markers YAC48 and YAC60, genomic separation 1 Mbp.



Ideogram of chromosome 15 with Prader - Willi Region and Angelmann Region. The size and genomic distance of the clones are sufficiently small and well characterized to measure the fine structure and organization of chromosome territories.

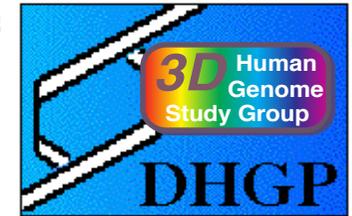


Tobias A. Knoch



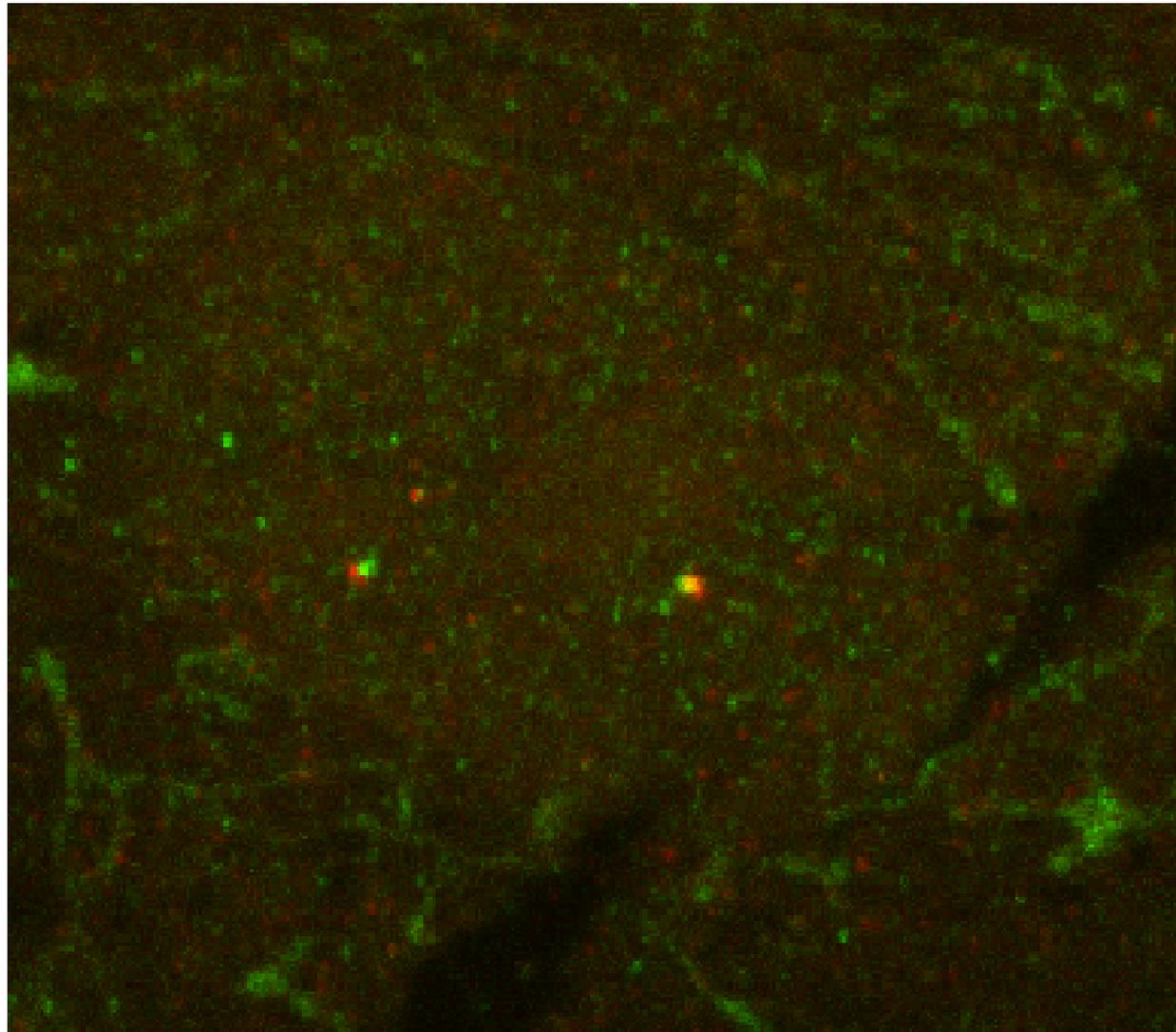
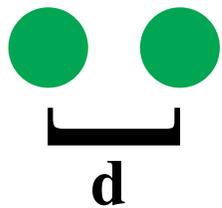
**Dual colour FISH of genomic markers leads to measurements of 3D-distances which are below the resolution of the microscope. Critical signals could also be excluded with higher confidence.**

Genomic marker  $\lambda 48.1$  in red and marker  $\lambda 48.14$  in green, genomic separation 195 kbp.

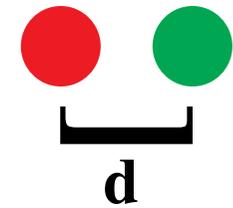


Tobias A. Knoch

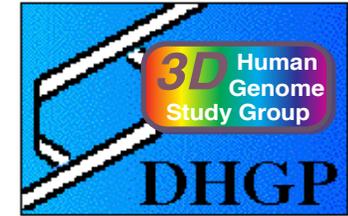
one colour



dual colour

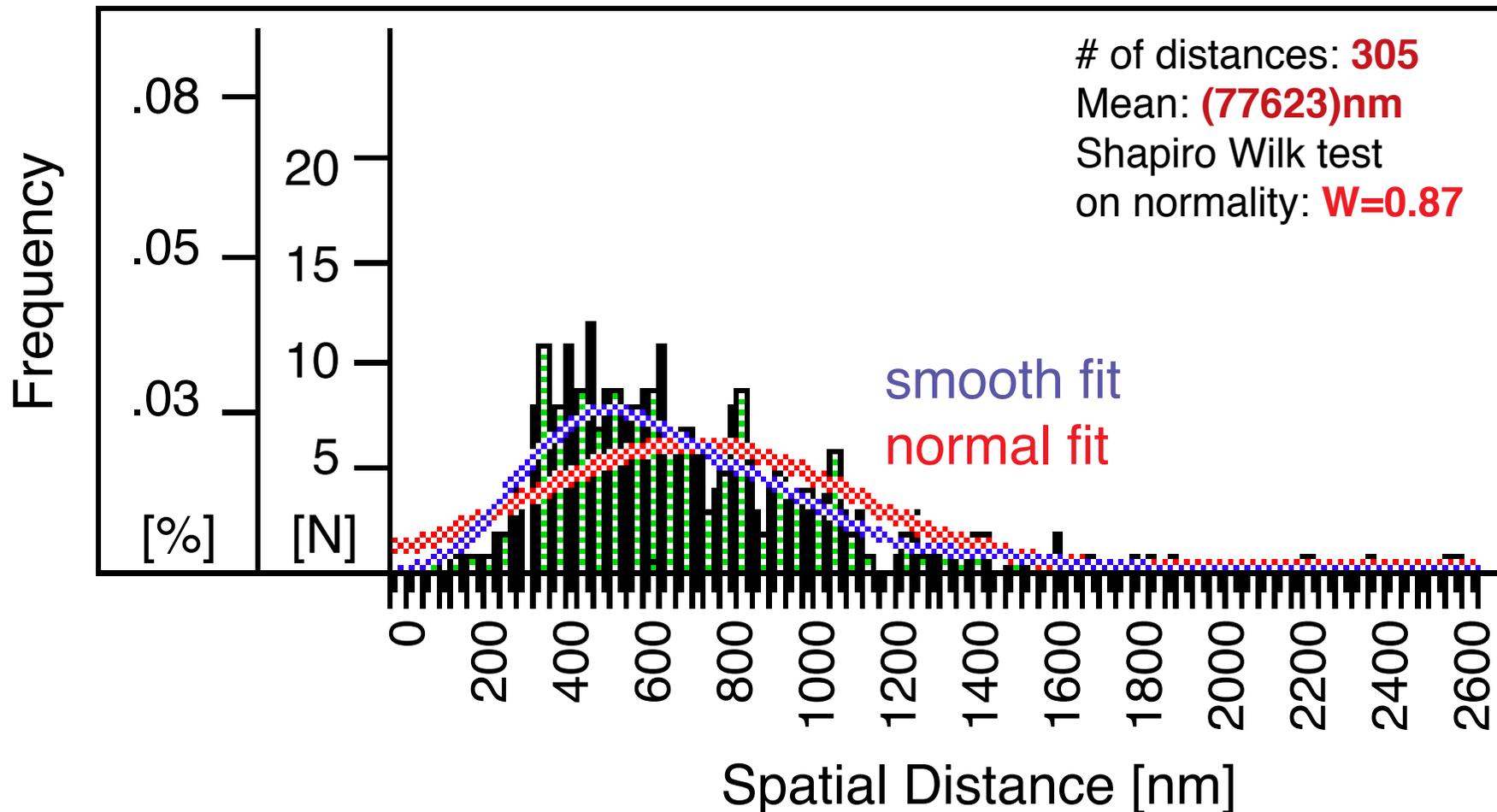


Statistical analysis of the spatial distances between the PWS-Region (YAC48) and AS-Region (YAC60) with a genomic distance of 1Mbp = 10m chromatin fiber.

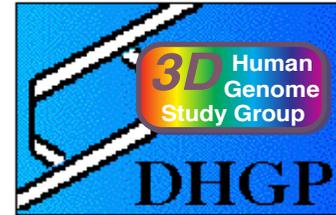


Tobias A. Knoch

### Distance Distribution

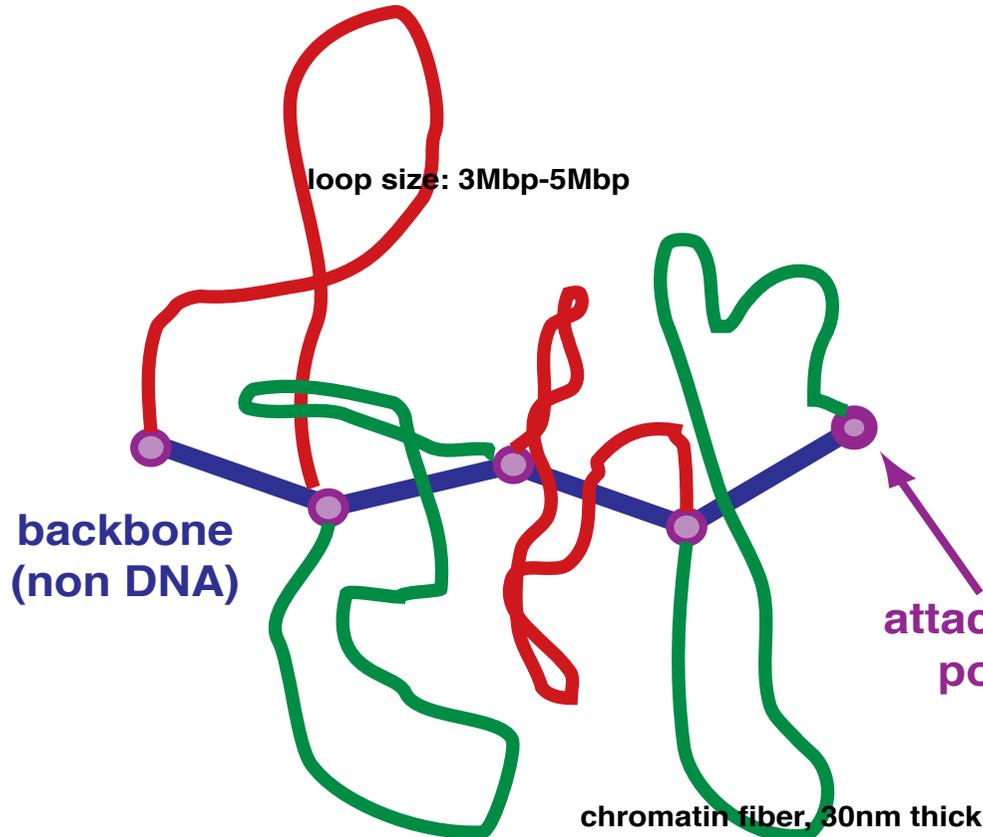


The Multi-Loop-Subcompartment (MLS) and the Random Walk / Giant Loop (RW/GL) Model. Rosettes in the MLS-Model correspond to the size of chromosomal interphase band domains.

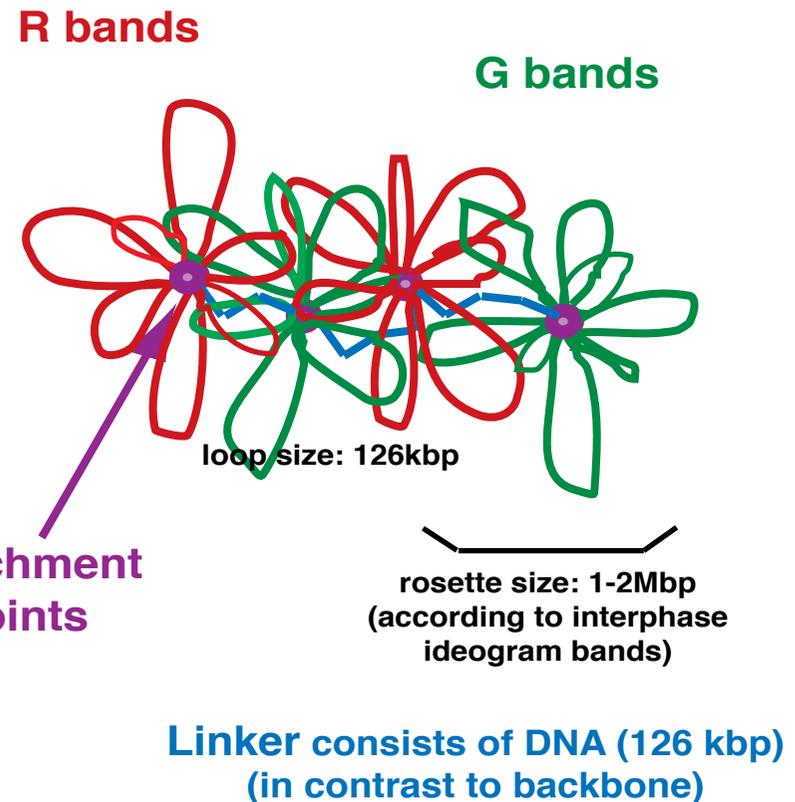


Tobias A. Knoch

**Random Walk / Giant Loop model (RW/GL)**  
Sachs et al. (1995)

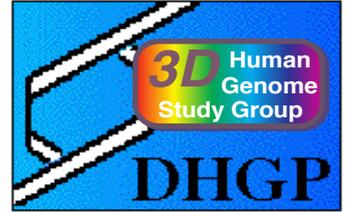


**Multi-Loop-Subcompartment model (MLS)**  
Münkel et al. (1997)

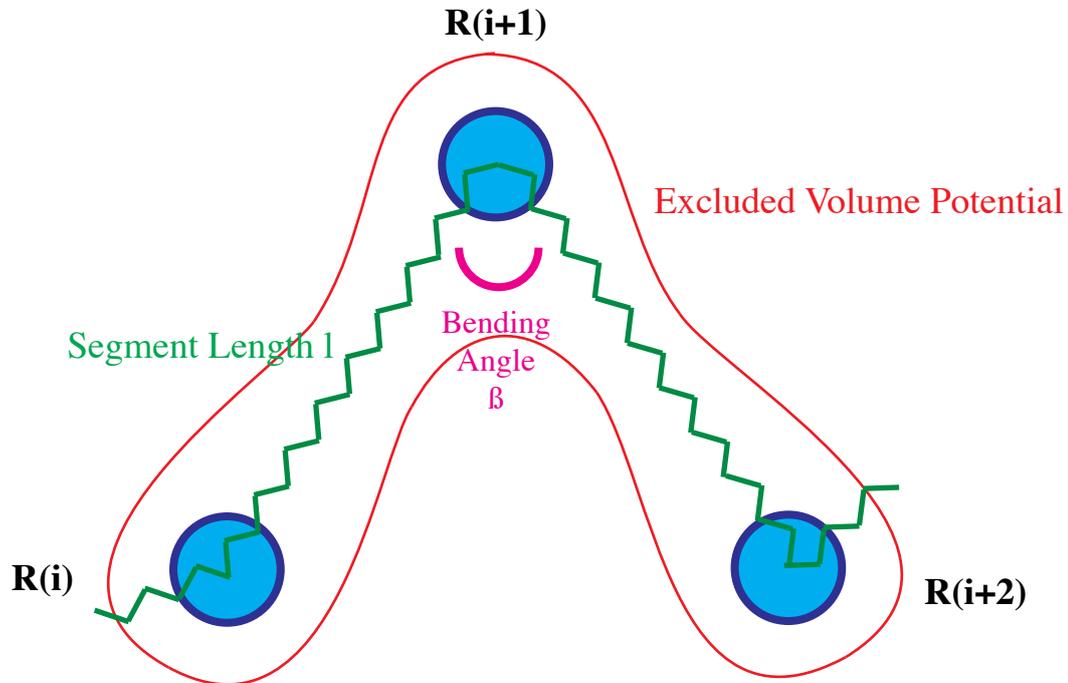


# Polymer Chain and Potentials

The chromosome fiber is simulated assuming a polymer chain and harmonic potentials. No hydrodynamic interaction is used due to hydrodynamic shielding.



Tobias A. Knoch



## Stretching Potential

$$U_s(l) = \frac{k_B T}{2} \left( \frac{l - l_0}{l_0} \right)^2$$

## Bending Potential

$$U_b(\beta) = \frac{k_B T}{2} \beta^2$$

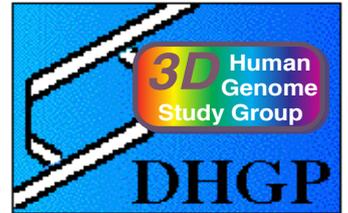
## Excluded Volume Potential

$$U_{ev}(r) = U_{ev}^0 k_B T \left( 1 + \frac{r^4 - 2r_c^2 r^2}{r_c^4} \right)$$

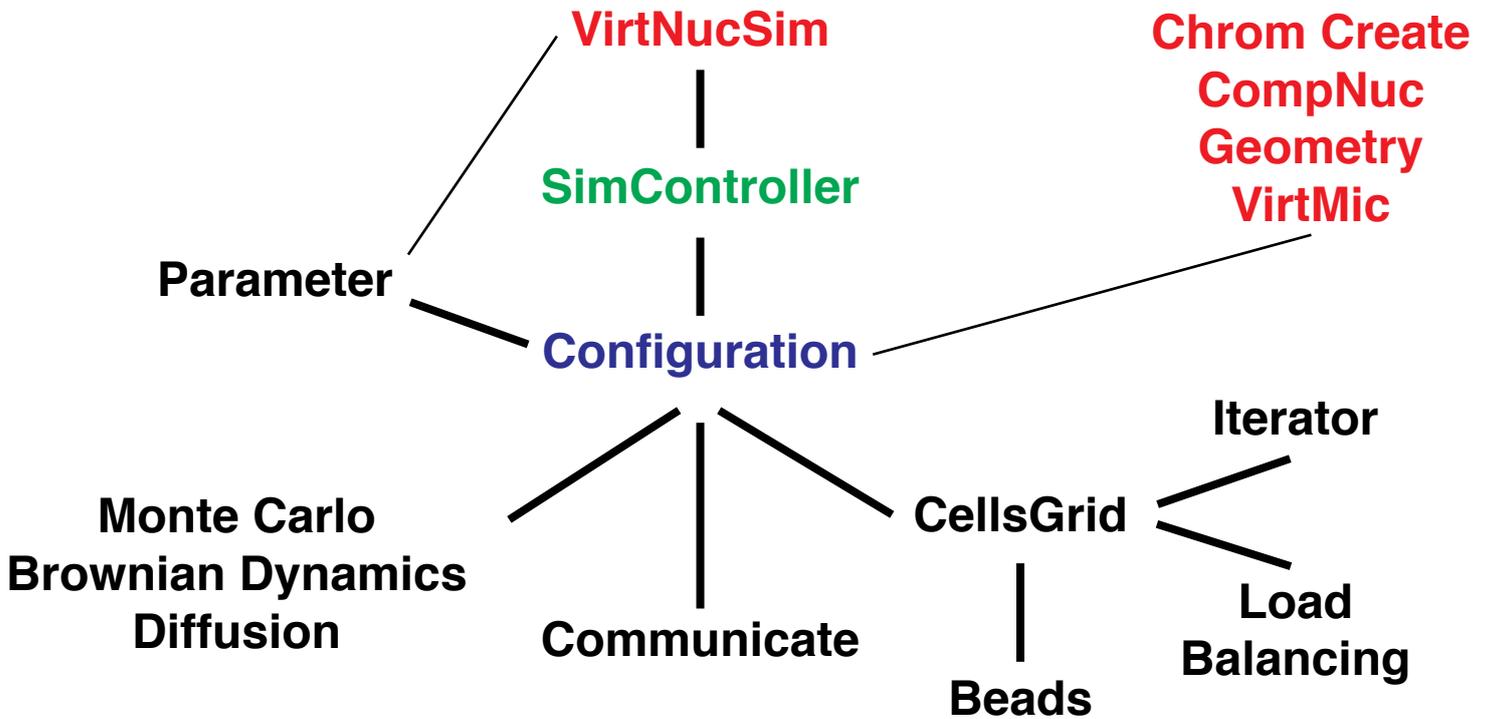
- $k_B$  : Boltzmann constant
- $T$  : Temperature, 310 K
- $\alpha$  : stretching elasticity,  $\alpha = 0.1$
- $\beta$  : bending elasticity
- $r_c$  : minimum distance of segments
- $L_k$  : Kuhn length, 300 nm,  $L_k = b/\alpha^2$

# VirtNucSim

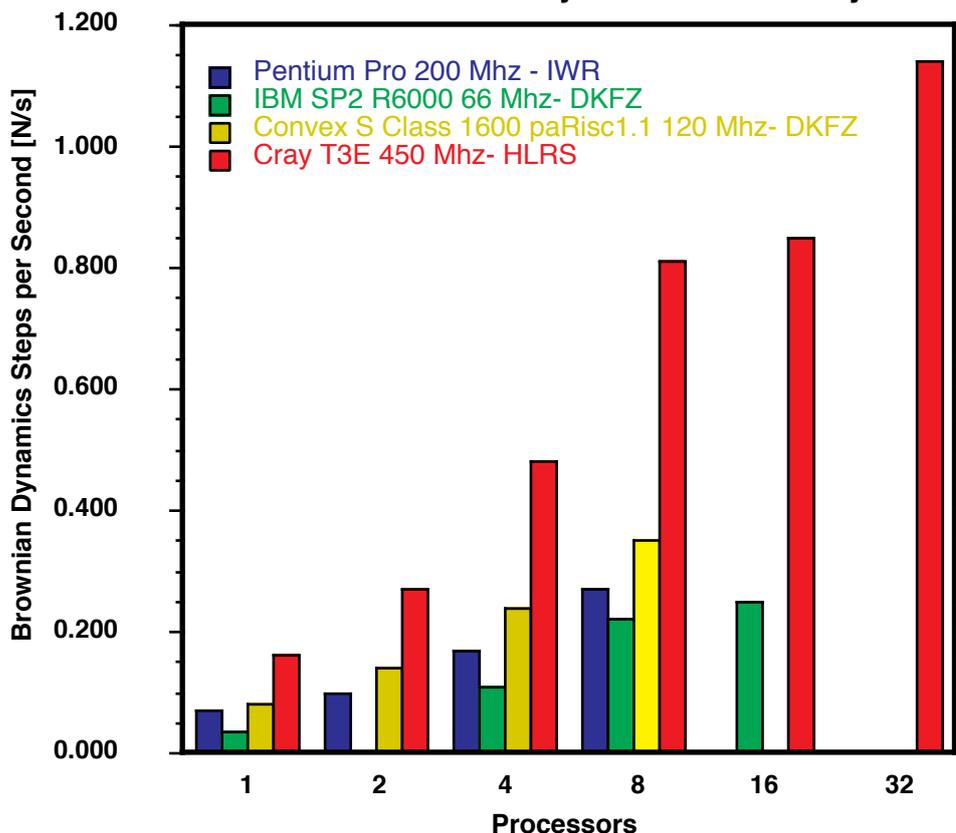
The programme code is written in C++ and uses Message Passing Interface (MPI) for parallelization and scales well at least up to 64 processors depending on compilation.



Tobias A. Knoch



VirtNuc - Brownian Dynamics: Scalability

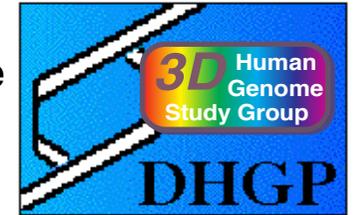


# Linked-Cell Algorithm and Dynamic Load Balancing

A linked-cell algorithm reduces the computation time for the pairwise Excluded Volume interaction using all beads within one cell and half of its 26 neighbour cells.

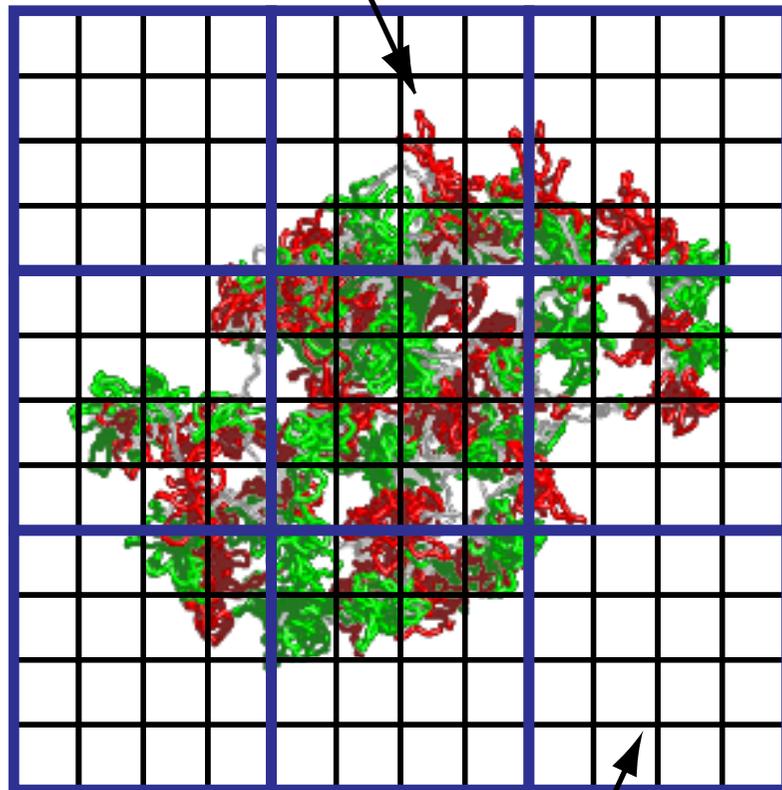
Dynamic Load Balancing reduces the computation time by projecting the 3D cell grid *dynamically* on the 2D processor grid (spherical nucleus time reduction: 1/3).

To avoid communication overhangs asynchronous, buffered communication is used.



Tobias A. Knoch

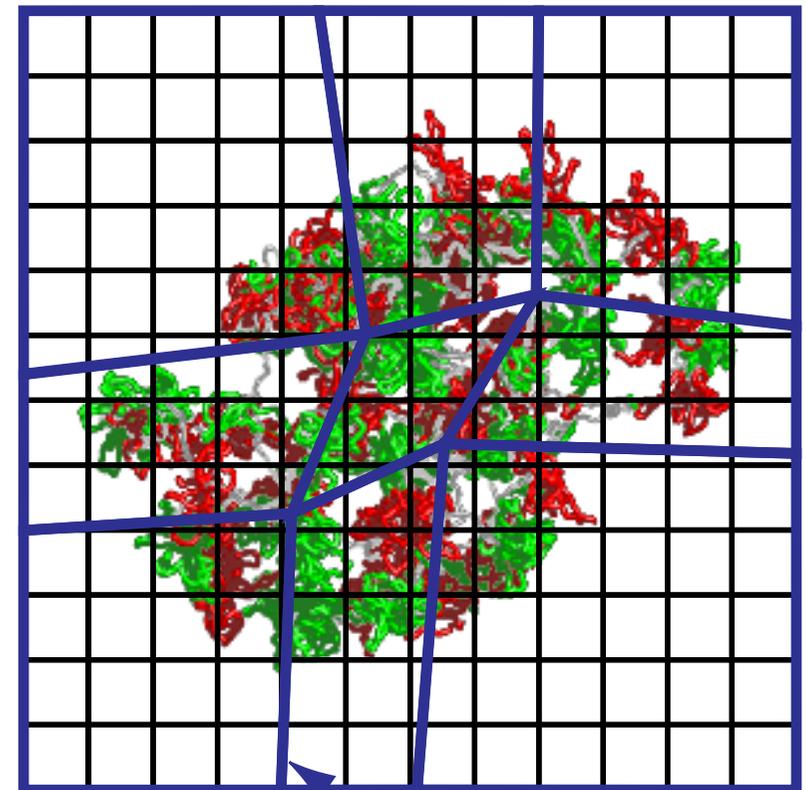
Segments/Beads



3D Cell Grid

(size dynamic, much finer than shown)

DLB

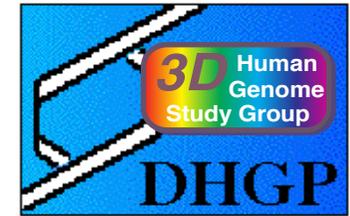


2D Processor Grid

(dynamic)

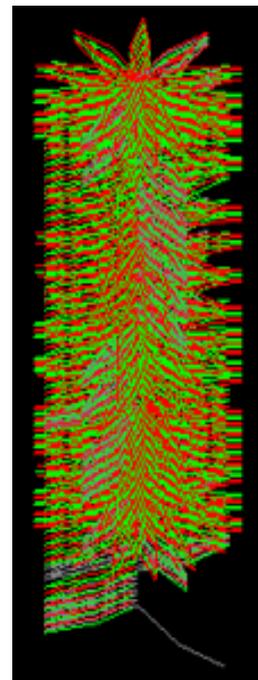
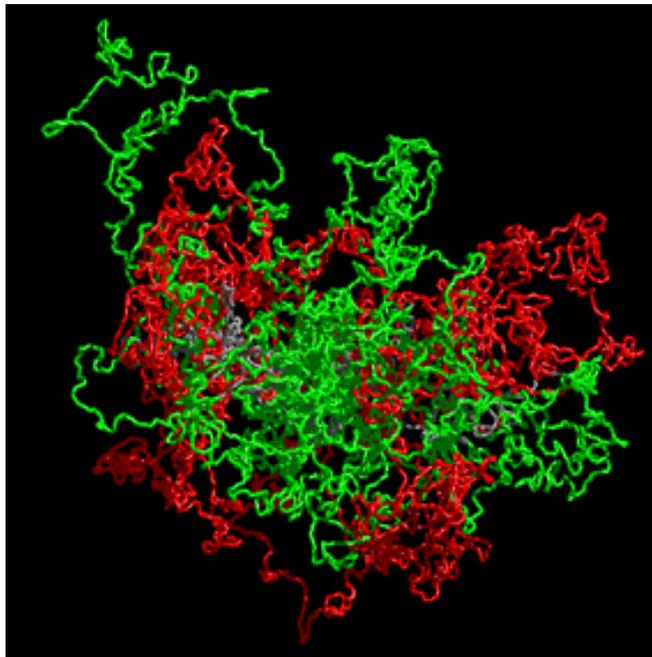
## Random-Walk/Giant-Loop model versus Multi-Loop-Subcompartment model. Simulation results of chromosome 15.

The chromosome is simulated assuming a flexible polymer chain, starting with  $\sim 3500$  segments of  $300\text{nm} = 31\text{kbp}$  and relaxing with  $\sim 21,000$  segments  $50\text{nm} = 5.2\text{kbp}$ . The starting configuration has the approximate form and size of a metaphase chromosome.



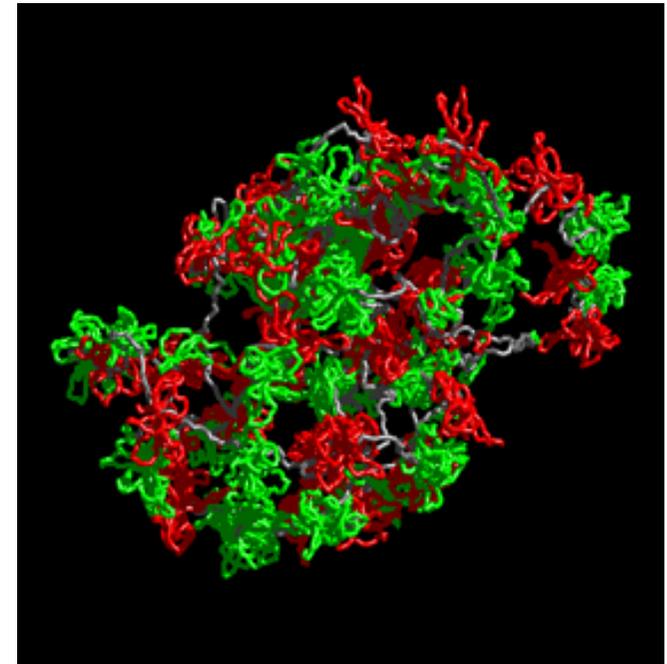
Tobias A. Knoch

Ray traced image of the [Random-Walk/Giant-Loop](#) model, loop size 5Mbp, after  $\sim 80,000$  Monte-Carlo and 1000 relaxing Brownian-Dynamics steps. Large loops intermingle freely thus forming no distinct features like in MLS model.

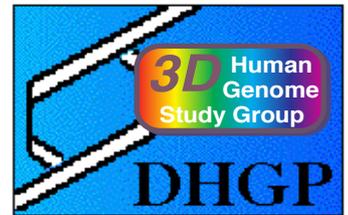


Wire frame image of the starting configuration.

Ray traced image of the [Multi-Loop-Subcompartment](#) model, loop size 126kbp, linker size 126 kbp, after  $\sim 50,000$  Monte-Carlo and 1000 relaxing Brownian-Dynamics steps. Here rosettes form subcompartments as separated organizational and dynamic entities.

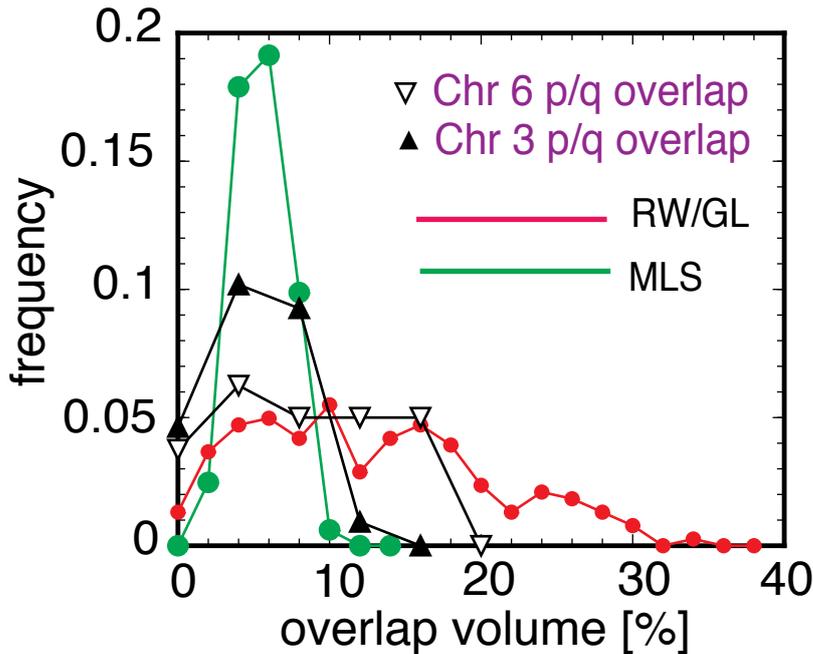


**Chromosome arms and bands do not overlap.  
The MLS-model predicts this behavior.**



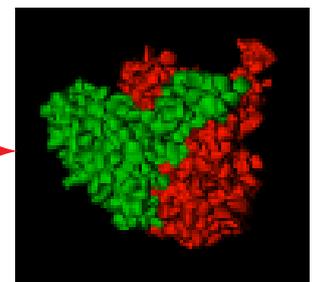
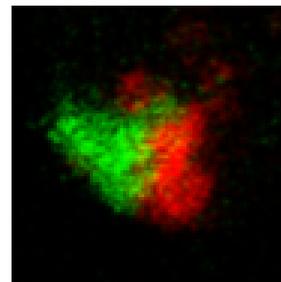
Tobias A. Knoch

### Arm Overlap



Confocal images of interphase p- and q- arms of human chromosome 3

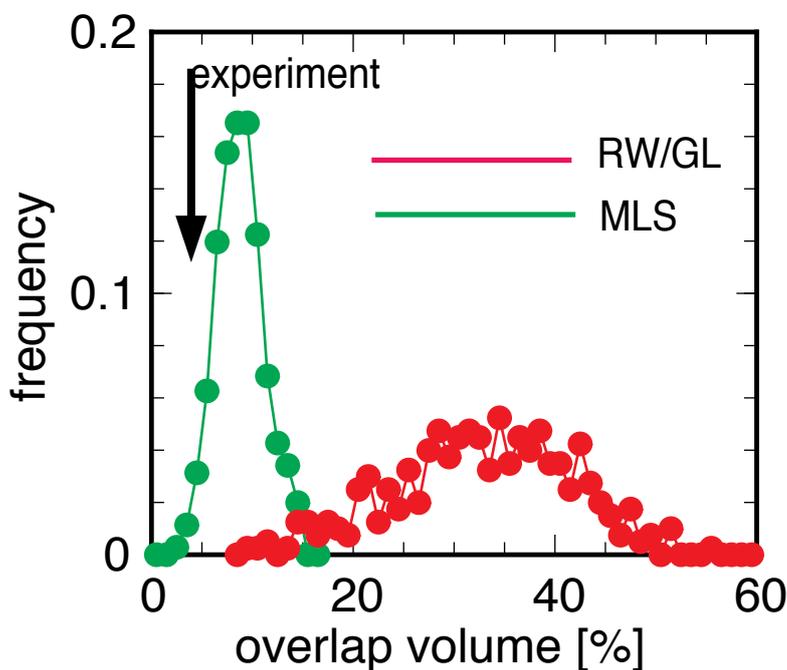
experiment reconstruction



S. Dietzel

R. Eils

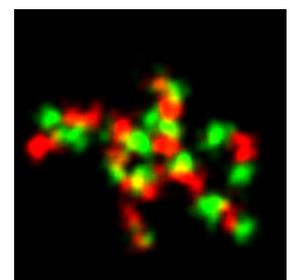
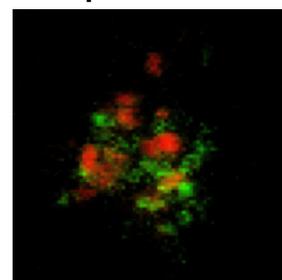
### Subcompartment Overlap



Confocal images of interphase R- and G- bands of human chromosome 15

experiment

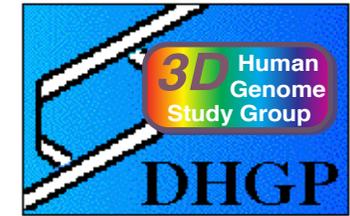
simulation



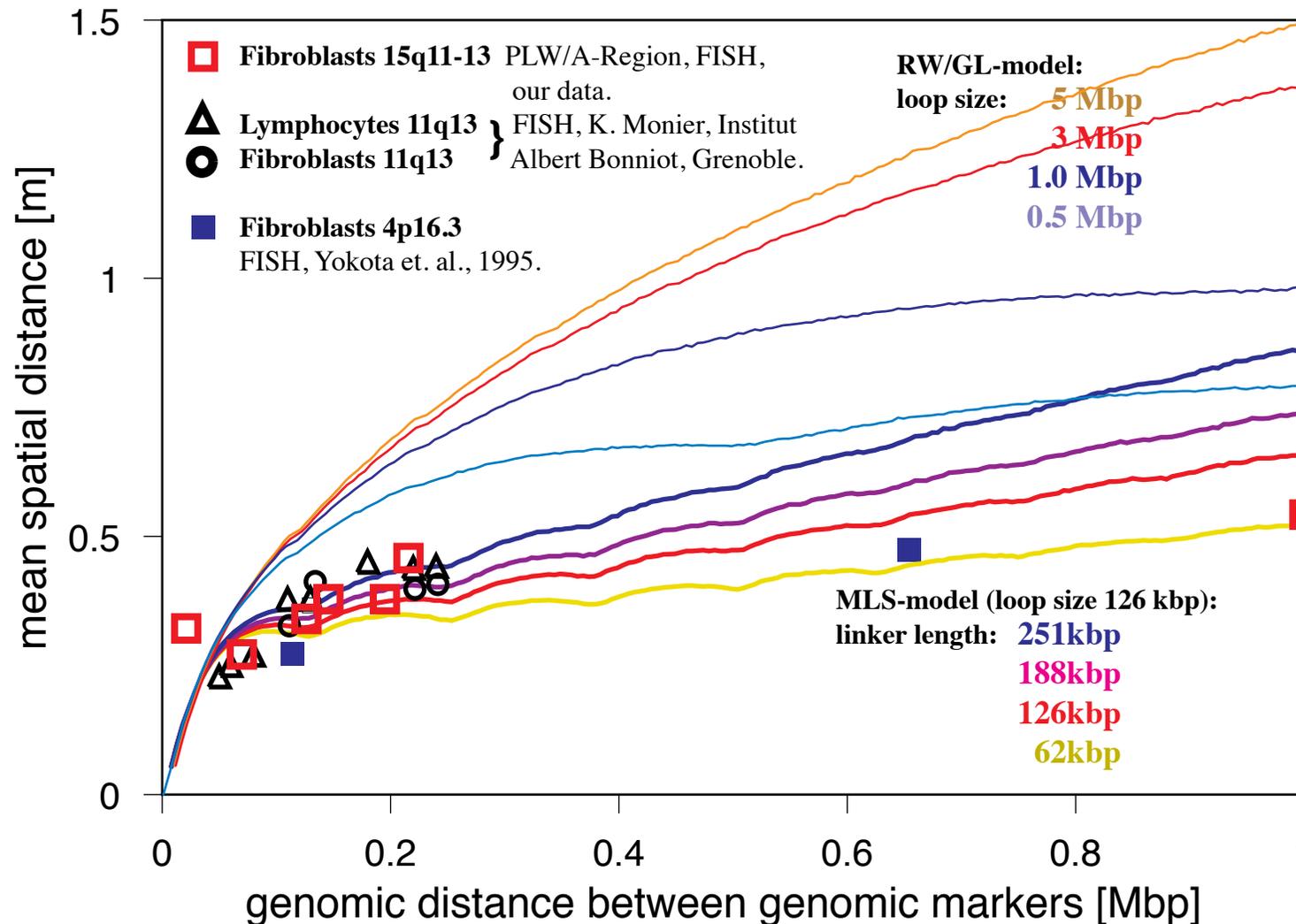
D. Zink

# Comparison of the RW/GL- and MLS model with experimentally determined interphase distances.

Best agreement between simulations and experiments is reached for a MLS-model with a loop size of 126kbp and a linker length of 126kbp.

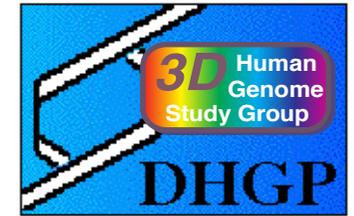


Tobias A. Knoch

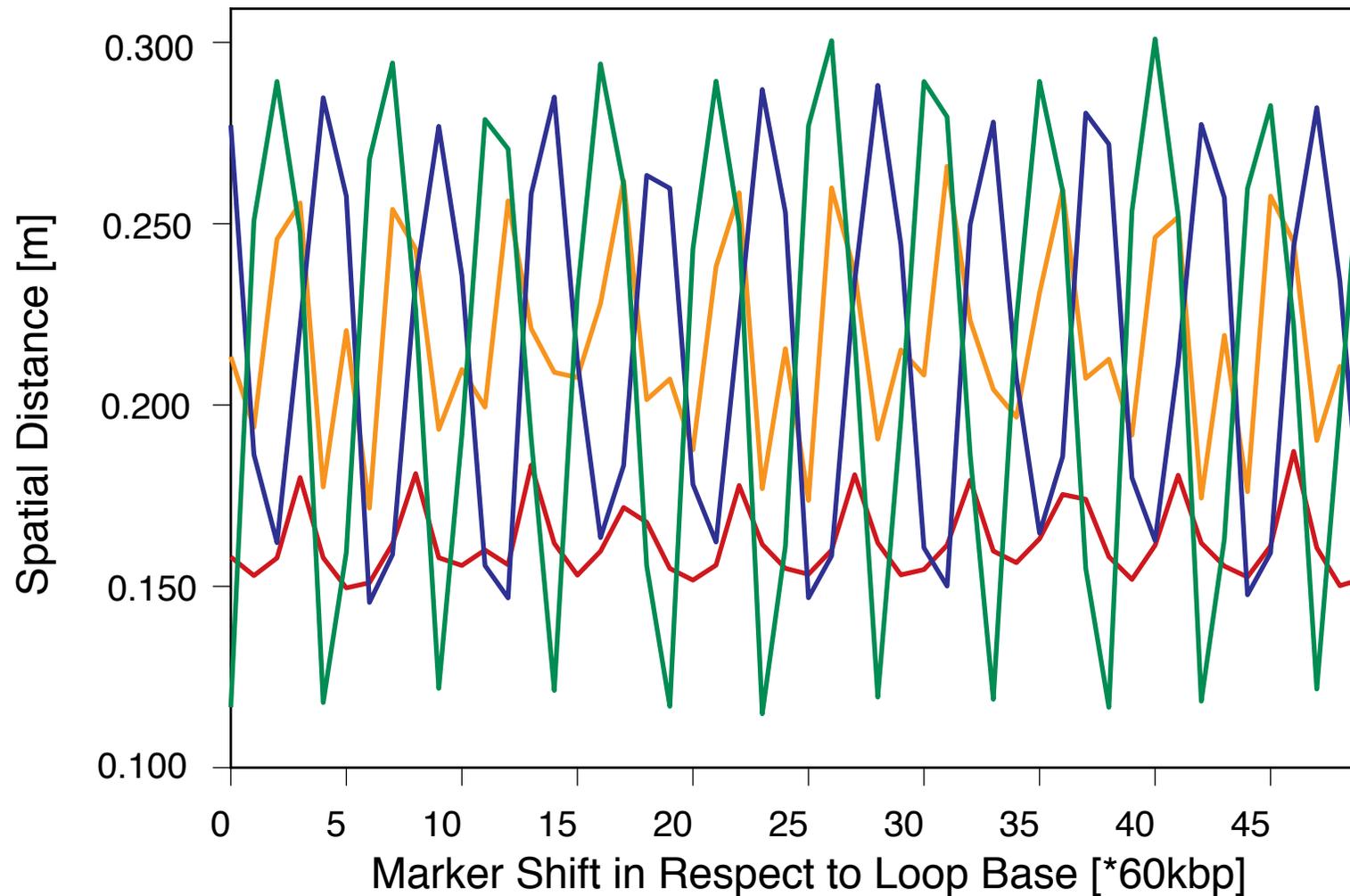


**Shift of a marker ensemble through a rosette in the MLS-model  
in respect to loop bases.**

**This leads to different sets of 3D-distances for every ensemble position.  
Due to the symmetry of the MLS-rosettes periodicities are found.**

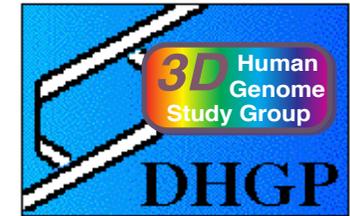


Tobias A. Knoch

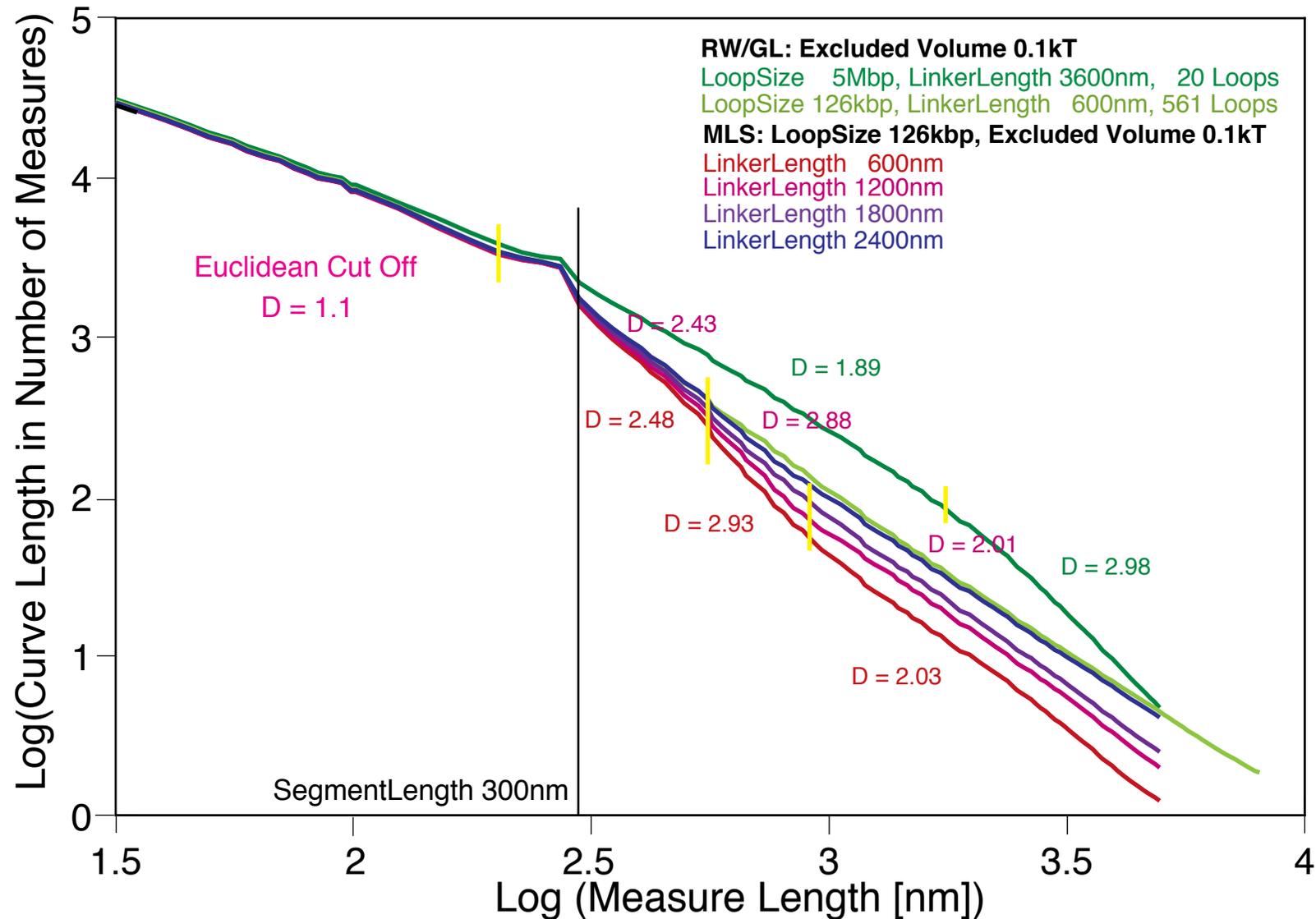


Genomic Marker Distance: — 31kbp — 145kbp — 171kbp — 215kbp

In agreement with porous network research fractal analysis show multifractal behaviour in simulations of chromosome 15. Different fractal dimensions mean different process-dynamics in these spaces. Therefore chromosomal territories show a higher degree of determinism than previously assumed.

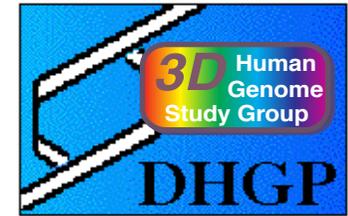


Tobias A. Knoch



**Creation of a 'Virtual Human Cell Nucleus' with  
all 46 chromosomes using the MLS-model.**

- a) 46 metaphase configurations are randomly placed in a spherical potential and dencondensed into interphase by Brownian Dynamic or Monte Carlo methods.
- b) 46 chains of spheres (number of spheres ~ chromosome size) are randomly placed in a spherical potential and relaxed with Simulated Annealing. Then the fine structure is added to receive the same resolution as in a).



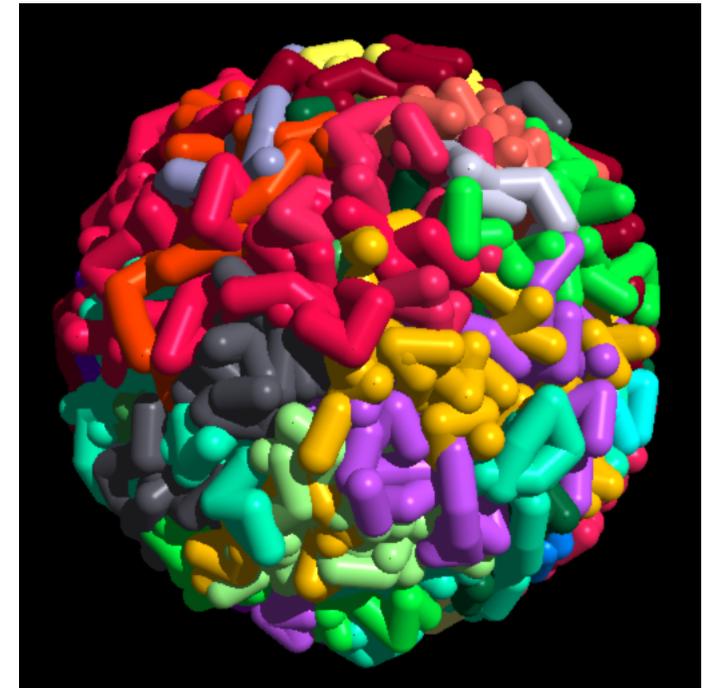
Tobias A. Knoch



0 ms



10 ms

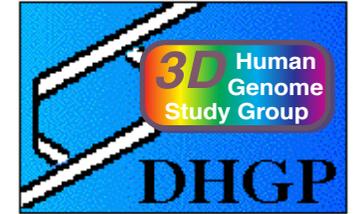


50 ms

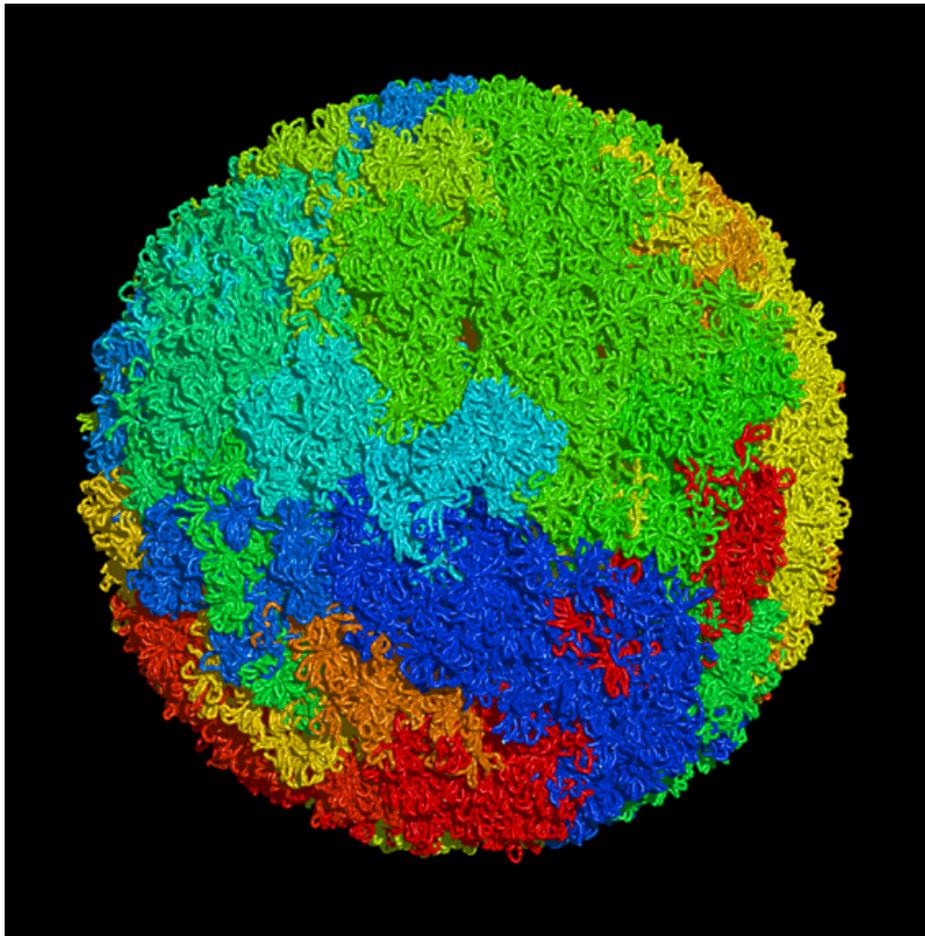
## 'Virtual Human Cell Nucleus'

### Simulation of all 46 chromosomes using the MLS-model.

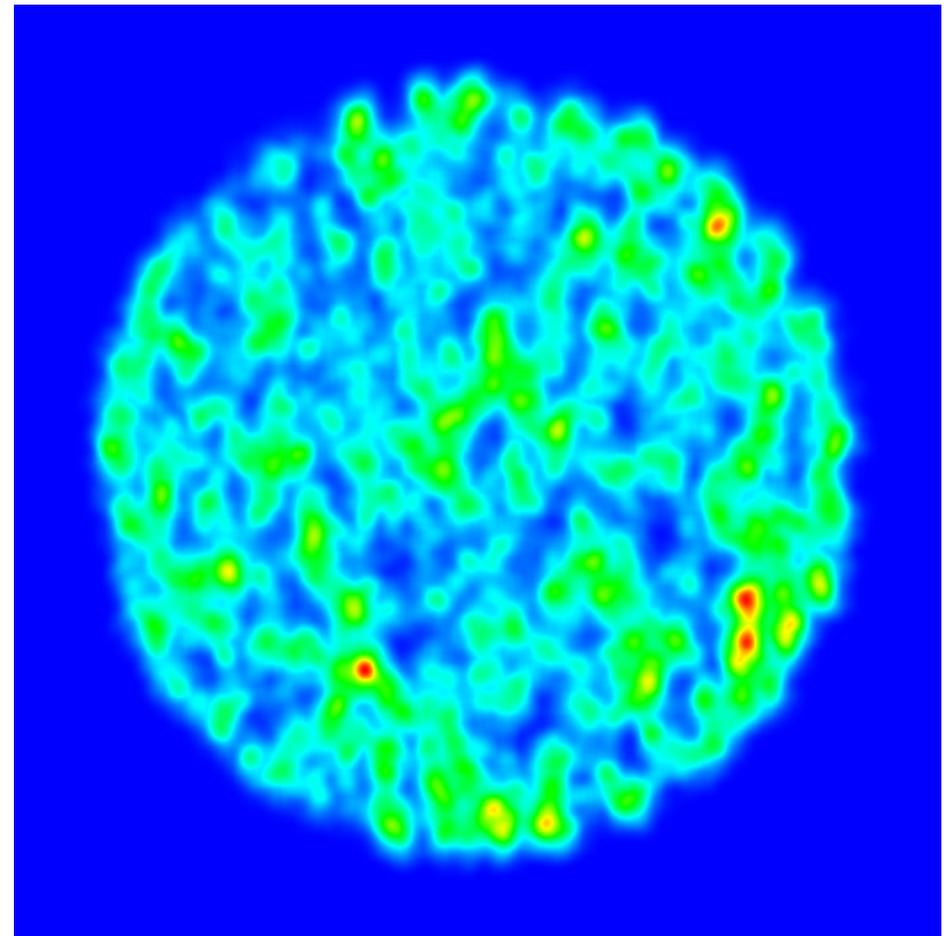
The nucleus is simulated assuming a flexible polymer chain, modelling the 46 chromatin fibers with a total 1,248,794 segments of 50 nm = 5.2 kbp. Pictures are shown after a 0.5 ms Brownian Dynamics simulation, one step taking 10s.



Tobias A. Knoch

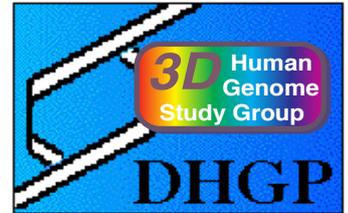


3-D rendering

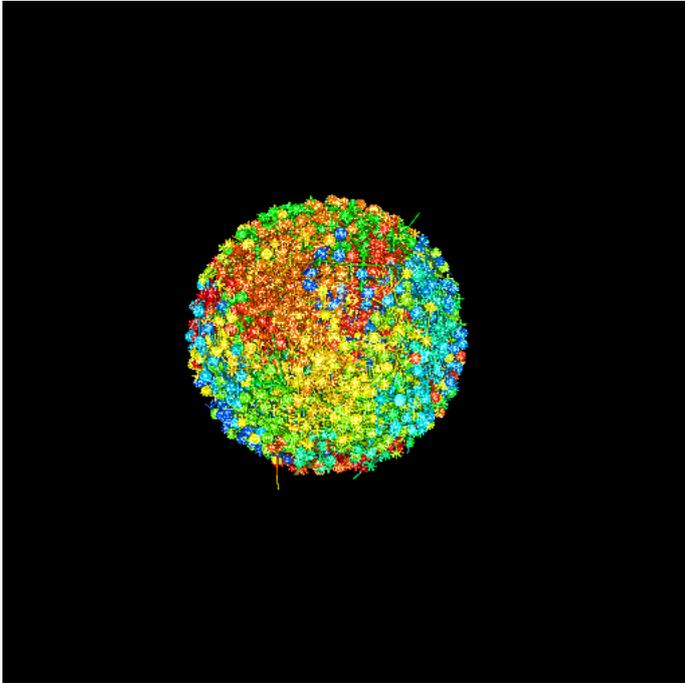


simulated confocal section

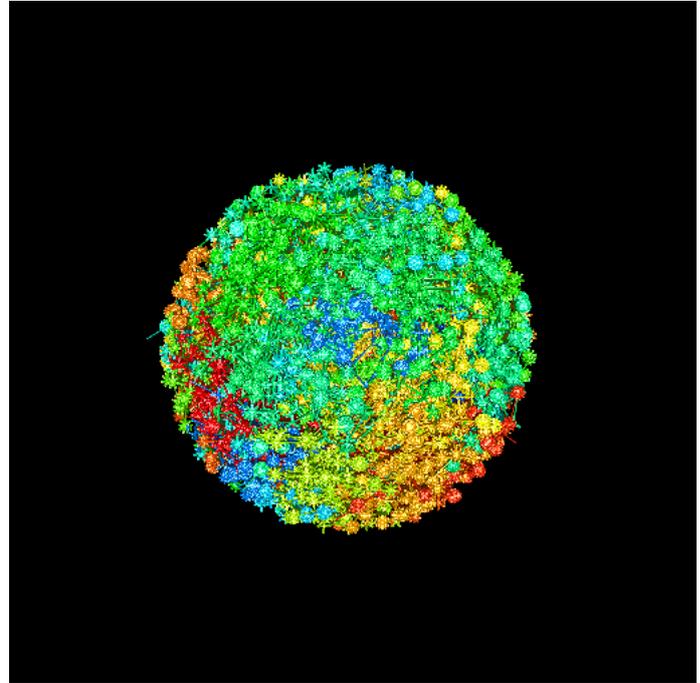
**The MLS-model leads to low overlap of chromosome-arms and subcompartments in contrast to the RWGL-model. This is also seen in experiments.**



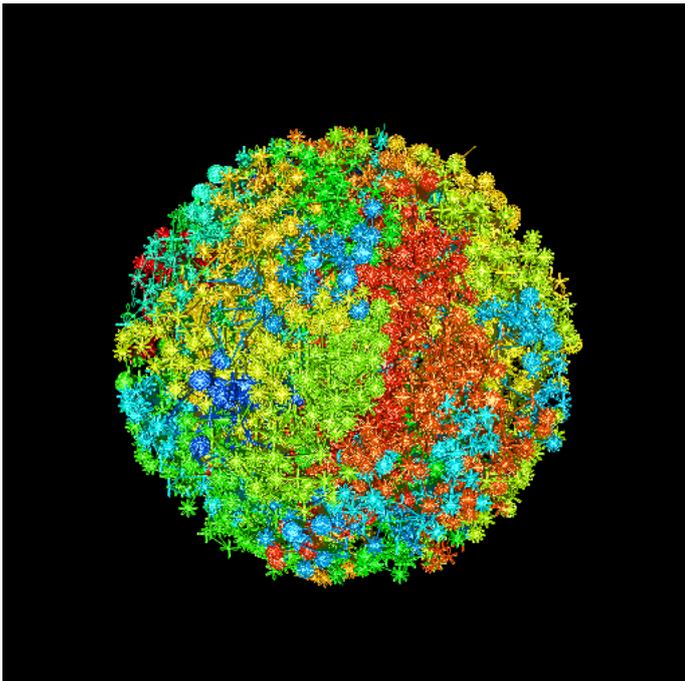
Tobias A. Knoch



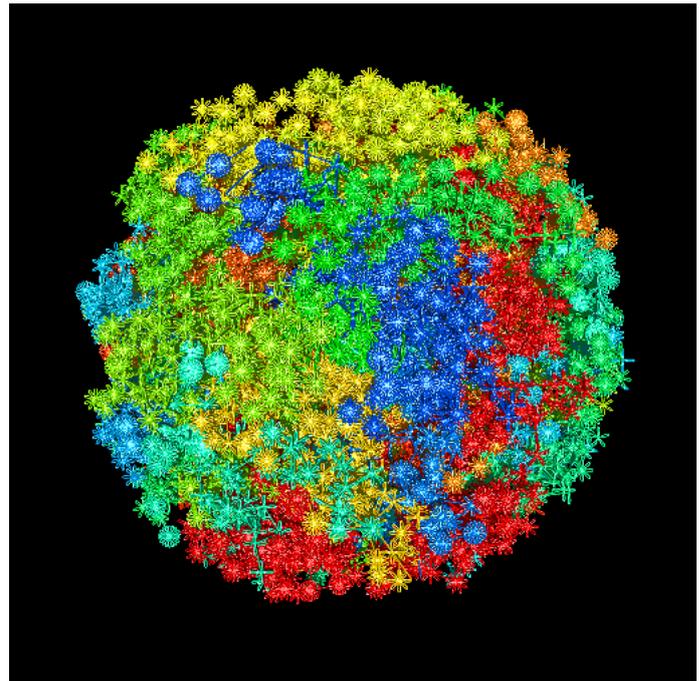
**nucleus  
6 m diameter**



**nucleus  
8 m diameter**



**nucleus  
10 m diameter**



**nucleus  
12 m diameter**

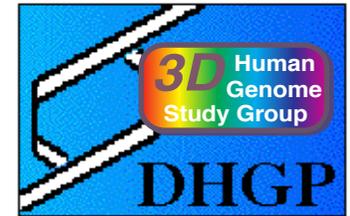
## Mapping of Histone H2B-GFP and H1-GFP distribution in vivo.

The Histone-GFP reflects the distribution of chromatin in interphase.

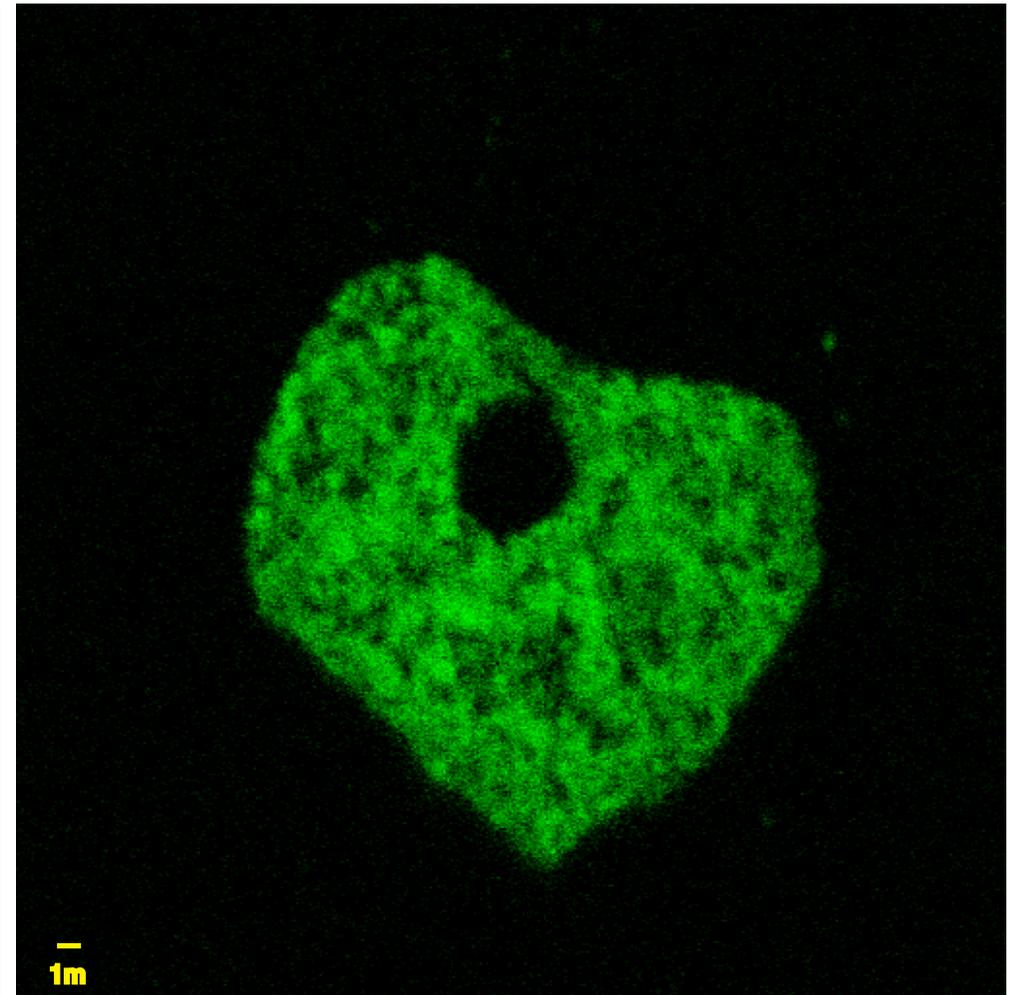
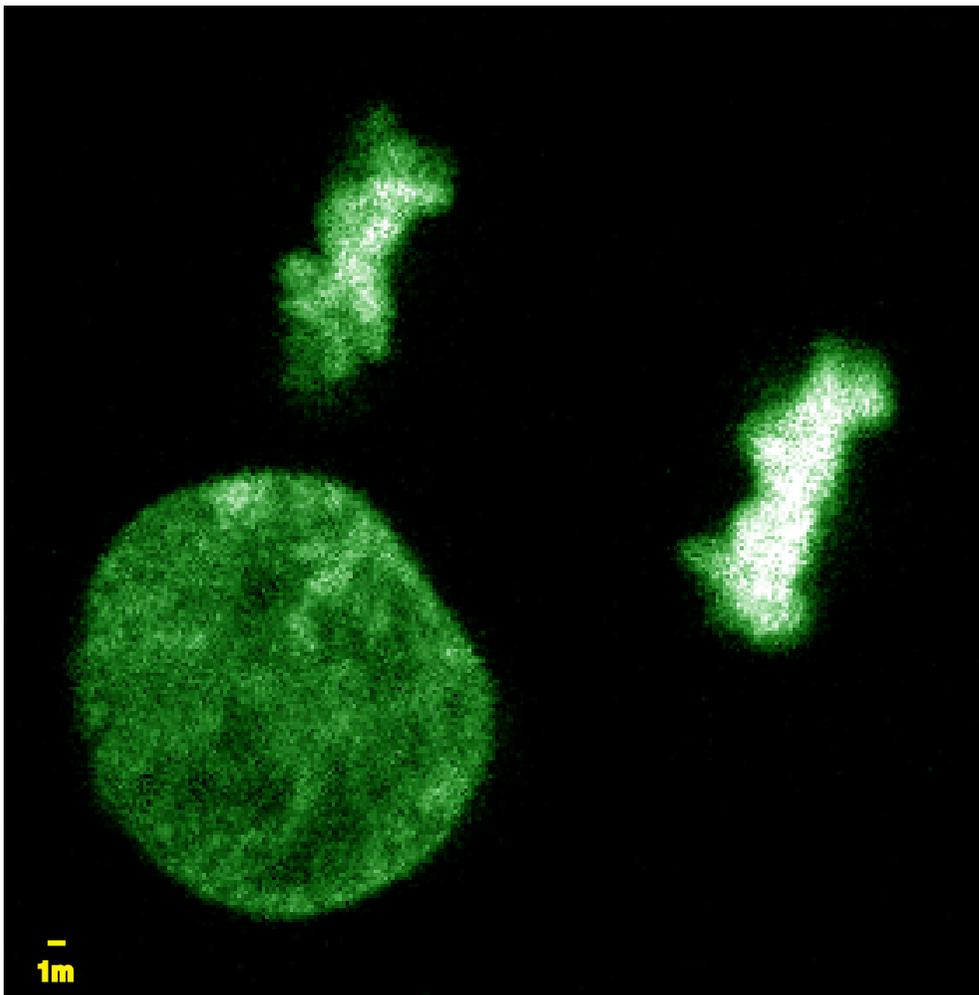
The structure visible in the images is similar to those found in simulations.

Left: HeLa cells stably transfected with H2B-GFP (K. Sullivan, Scripps Institute).  
Confocal in vivo section of a cell nucleus and a mitosis.

Right: Cos7 cell stably transfected with H1-GFP (A. Alonso, DKFZ). Confocal in vivo section.

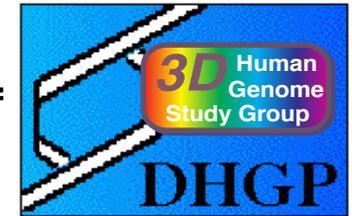


Tobias A. Knoch



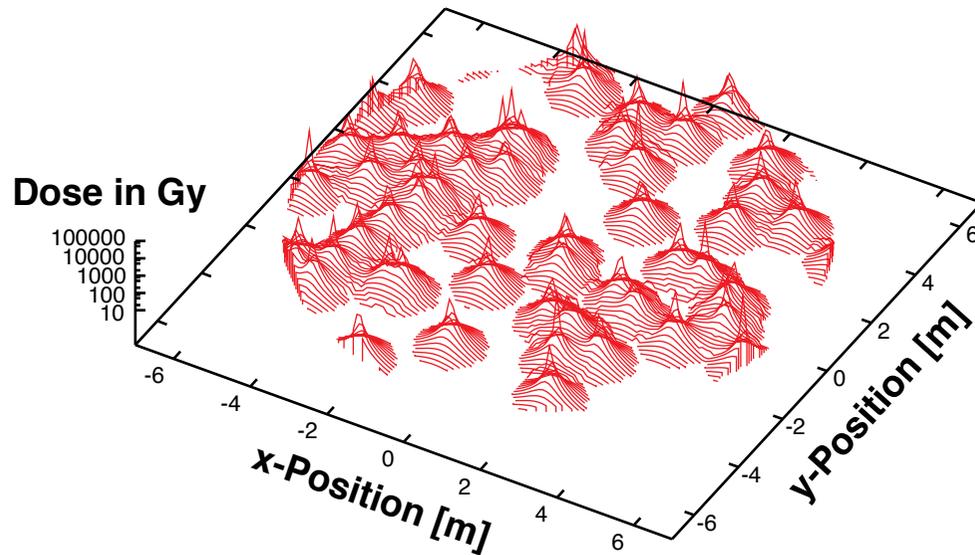
## DNA fragmentation by irradiation with carbon ions.

Irradiation with carbon ions results in DNA double strand breakage. The length of the fragments follow distributions depending on the spatial arrangement of the 30 nm chromatin fiber in the nucleus. Together with P. Quicken, GSF, Munich.

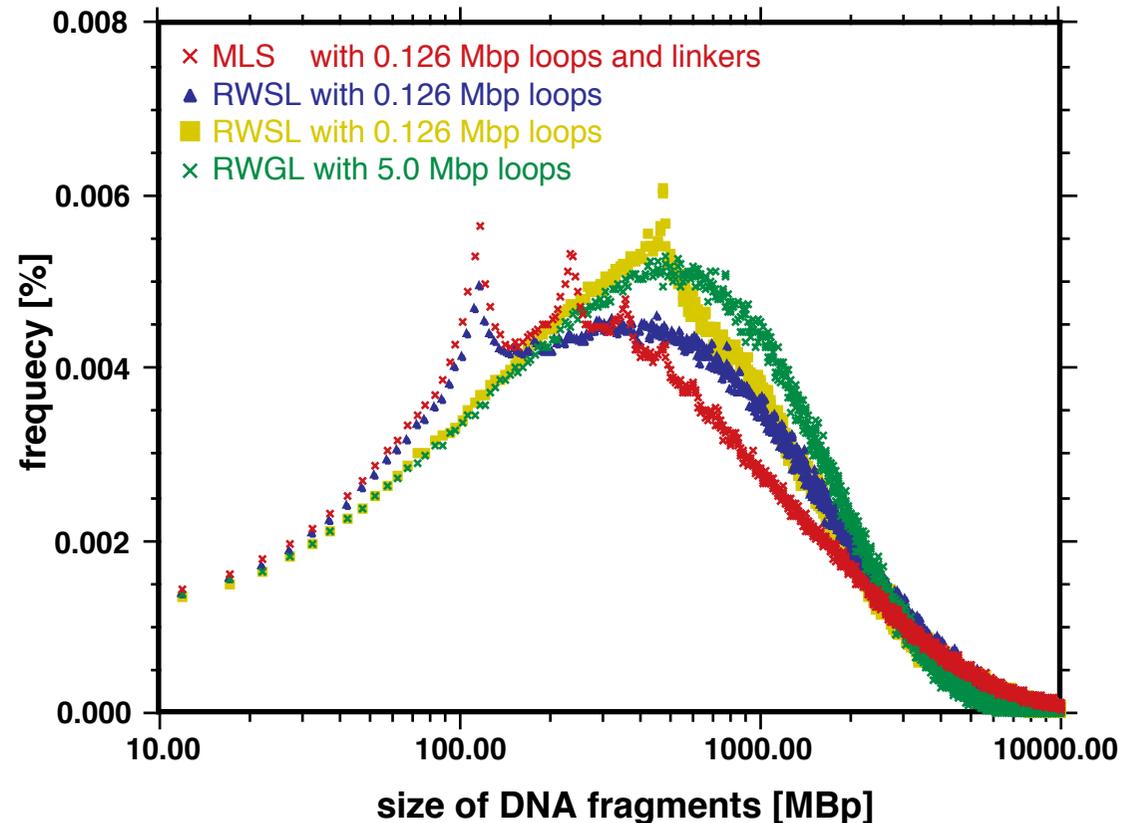


Tobias A. Knoch

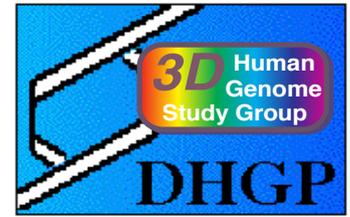
Radiation dose distribution  
in a cell nucleus  
irradiated with carbon ions



Comparison between experimental and simulated  
fragment distributions after carbon irradiation.



# People



**Tobias A. Knoch**

**Tobias A. Knoch  
Carsten Mehring  
Christian Münkel  
Jörg Langowski**

**Biophysics of Macromolecules, German Cancer Research Center, Heidelberg, Germany**

**Steffanie Groß  
Karin Bütig  
Bernhard Horsthemke**

**Institute for Human Genetics, University of Essen, Germany**

**Irina Solovei  
Thomas Cremer**

**Institute for Anthropology and Human Genetics, University of Munich, Germany**

**Joachim Rauch  
Harald Bornfleth  
Christoph Cremer**

**Institute for Applied Physics, University of Heidelberg, Germany**

**Karin Monier  
Kevin Sullivan**

**The Scripps Institute, La Jolla, USA**

**Angel Alonso**

**Applied Tumorvirology, German Cancer Research Center, Germany**

**Peter Lichter**

**Organisation of Complex Genomes, German Cancer Research Center, Germany**

**IBM-SP2, German Cancer Research Centre, Heidelberg  
Cray T3E, High-Performance Computing Center, Stuttgart  
IBM-SP2, Computing Centre, Karlsruhe  
Silicon Graphics-Graphic-Lab, Institute for Scientific  
Computing (IWR), Heidelberg**

**The work is part of the Heidelberg 3D Human Genome Study Group  
which is part of the German Human Genome Project.**

**We would like to thank the German Ministry for Science and Technology (BMFT)  
for financing this project.**

# Computer Modelling of Chromosome Territories

**Knoch, T. A.**

*German Cancer Research Centre (DKFZ), Heidelberg, Germany, February, 1999.*

## *Abstract*

Despite the successful linear sequencing of the human genome its three-dimensional structure is widely unknown. However, the regulation of genes - their transcription and replication - has been shown to be closely connected to the three-dimensional organization of the genome and the cell nucleus. On the bases of polymer physics we have recently developed detailed and quantitative structural models for the folding of the 30 nm chromatin fiber within the human interphase cell nucleus. A quantitative test of several plausible theories resulted in a best agreement between computer simulations of chromosomes, cell nuclei and experiments for the so-called Multi-Loop-Subcompartment (MLS) model. Results concern the following properties: overlap of chromosome territories, -arms, -bands, 3D spatial distances between genomic markers as function of their genomic separation in base pairs, fractal analysis of simulations, mass distribution of chromatin in cell nuclei and the fragmentation distribution of cellular DNA after irradiation with carbon ions. Thus in an analogy to the Bauhaus principle that „form follows function“, analyzing in which form DNA is organized might help us to understand genomic function.

Corresponding author email contact: [TA.Knoch@taknoch.org](mailto:TA.Knoch@taknoch.org)

### Keywords:

Genome, genomics, genome organization, genome architecture, structural sequencing, architectural sequencing, systems genomics, coevolution, holistic genetics, genome mechanics, genome function, genetics, gene regulation, replication, transcription, repair, homologous recombination, simultaneous co-transfection, cell division, mitosis, metaphase, interphase, cell nucleus, nuclear structure, nuclear organization, chromatin density distribution, nuclear morphology, chromosome territories, subchromosomal domains, chromatin loop aggregates, chromatin rosettes, chromatin loops, chromatin fibre, chromatin density, persistence length, spatial distance measurement, histones, H1.0, H2A, H2B, H3, H4, mH2A1.2, DNA sequence, complete sequenced genomes, molecular transport, obstructed diffusion, anomalous diffusion, percolation, long-range correlations, fractal analysis, scaling analysis, exact yard-stick dimension, box-counting dimension, lacunarity dimension, local nuclear dimension, nuclear diffuseness, parallel super computing, grid computing, volunteer computing, Brownian Dynamics, Monte Carlo, fluorescence in situ hybridization, confocal laser scanning microscopy, fluorescence correlation spectroscopy, super resolution microscopy, spatial precision distance microscopy, autofluorescent proteins, CFP, GFP, YFP, DsRed, fusionprotein, in vivo labelling.

## *Literature References*

- Knoch, T. A.** Dreidimensionale Organisation von Chromosomen-Domänen in Simulation und Experiment. (Three-dimensional organization of chromosome domains in simulation and experiment.) *Diploma Thesis*, Faculty for Physics and Astronomy, Ruperto-Carola University, Heidelberg, Germany, 1998, and TAK Press, Tobias A. Knoch, Mannheim, Germany, ISBN 3-00-010685-5 and ISBN 978-3-00-010685-9 (soft cover, 2rd ed.), ISBN 3-00-035857-9 and ISBN 978-3-00-0358857-0 (hard cover, 2rd ed.), ISBN 3-00-035858-7, and ISBN 978-3-00-035858-6 (DVD, 2rd ed.), 1998.
- Knoch, T. A., Münkler, C. & Langowski, J.** Three-dimensional organization of chromosome territories and the human cell nucleus - about the structure of a self replicating nano fabrication site. *Foresight Institute - Article Archive*, Foresight Institute, Palo Alto, CA, USA, <http://www.foresight.org>, 1- 6, 1998.
- Knoch, T. A., Münkler, C. & Langowski, J.** Three-Dimensional Organization of Chromosome Territories and the Human Interphase Nucleus. *High Performance Scientific Supercomputing*, editor Wilfried Jüling, Scientific Supercomputing Center (SSC) Karlsruhe, University of Karlsruhe (TH), 27- 29, 1999.